Face Recognition using Eigenfaces and Neural Networks

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Abstract: In this study, we develop a computational model to identify the face of an unknown person’s by applying eigenfaces. The eigenfaces has been applied to extract the basic face of the human face images. The eigenfaces is then projecting onto human faces to identify unique features vectors. This significant features vector can be used to identify an unknown face by using the backpropagation neural network that utilized euclidean distance for classification and recognition. The ORL database for this investigation consists of 40 people with various 400 face images had been used for the learning. The eigenfaces including implemented Jacobi’s method for eigenvalues and eigenvectors has been performed. The classification and recognition using backpropagation neural network showed impressive positive result to classify face images.

Key words: Feature vector, eigenfaces, eigenvalues, eigenvector

INTRODUCTION

The developing of face recognition system is quite difficult because human faces is quite complex, multidimensional and corresponding on environment changes. For that reason the human machine recognition of human faces is a challenging problem due the changes in the face identity and variation between images of the same due to illumination and viewing direction. The issues are how the features adopted to represent a face under environmental changes and how we classify a new face image based on the chosen representation. Computers that recognize human faces systems have been applied in many applications such as security system, mug shot matching and model-based video coding.


We develop a technique to extract features from an intensity image of human frontal face to represent the features using eigenfaces. Figure 1 shows the block diagram of our system. These advantages no face features being required, the ability to learn and later recognize new faces in an unsupervised manner and that it is easy to implement using neural network architecture.

Eigenfaces method: The basic idea of eigenfaces is that all face images are similar in all configurations and they can be described in its basic face images. Based on this idea, the eigenfaces procedures[3] are as follows:

a. We assume the training sets of images are \( \Gamma_1, \Gamma_2, \ldots, \Gamma_m \) with each image is \( I(x, y) \). Convert each image into set of vectors and new full-size matrix \( (m \times p) \), where \( m \) is the number of training images and \( p \) is \( x \times y \).
b. Find the mean face by:
\[
\Psi = \frac{1}{m} \sum_{i=1}^{m} \Gamma_i
\]  
(1)

c. Calculated the mean-subtracted face:
\[
\Phi_i = \Gamma_i - \Psi, i = 1, 2, \ldots, m
\]  
(2)

and a set of matrix is obtained with
\[
A = [\Phi_1, \Phi_2, \ldots, \Phi_m]
\]  

is the mean-subtracted matrix vector with its size \(A_{mp}\).
d. By implementing the matrix transformations, the vectors matrix is reduced by:
\[
C_{mm} = A_{mp} \times A_{pm}^T
\]  
(3)

where \(C\) is the covariance matrix and \(T\) is transpose matrix.
e. Find the eigenvectors, \(V_{mm}\) and eigenvalues, \(\lambda_m\) from the \(C\) matrix using Jacobi method\(^{[4-7]}\) and ordered the eigenvectors by highest eigenvalues. Jacobi’s method is chosen because its accuracy and reliability than other method\(^{[8,9]}\).
f. Apply the eigenvectors matrix, \(V_{mm}\) and adjusted matrix, \(\Phi_m\). These vectors determine linear combinations of the training set images to form the eigenfaces, \(U_k\) by:
\[
U_k = \sum_{n=1}^{m} \Phi_n V_{kn}, k = 1, 2, \ldots, m
\]  
(4)

Instead of using \(m\) eigenfaces, \(m' < m\) which we consider the image provided for training are more than 1 for each individuals or class. \(m'\) is the total class used.
g. Based on the eigenfaces, each image have its face vector by:
\[
W_k = U_k^T (\Gamma - \Psi), k = 1, 2, \ldots, m'
\]  
(5)

and mean subtracted vector of size \((p \times 1)\) and eigenfaces is \(U_{pmr}\). The weights form a feature vector:
\[
\Omega^T = [w_1, w_2, \ldots, w_m]
\]  

h. A face can reconstructed by using its feature, \(\Omega^T\) vector and previous eigenfaces, \(U_{m'}\) as :
\[
\Gamma' = \Psi + \Phi_f
\]  
(6)

where \(\Phi_f = \sum_{i=1}^{m'} w_i U_i\).

**RESULTS AND DISCUSSION**

The Code for eigenfaces is developed using Visual C++. The eigenvectors and eigenvalues play a major role in producing eigenfaces. The results obtained are compared with MATLAB and eigenvalues and eigenvectors java apple\(^{[10]}\).

The experiments have been conducted using the Olivetti Research Laboratory (ORL) database (Fig. 2). Figure 3 shows the mean image after the transformation of training images. The eigenfaces result has been obtained (Fig. 4-6).

From the Fig. 4-6 each training session shows the variations of eigenfaces. In Fig. 4, 16 images are used (8 classes with 2 images per-class), Fig. 5 used 32 images (8 classes with 4 images per-class) and Fig. 6 used 48 images (8 classes with 6 images per-class). The eigenfaces above shows exactly, if the experiments is conducted using more images, the eigenfaces becomes more whitening. Means, lesser images make the eigenfaces become darker and indistinct. Sirovich and Kirby evaluated a limited version of this framework on an ensemble of 115 images of Caucasian males digitized in a controlled manner, and found that 40 images were sufficient for a very good description of face images.

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Fig. 2: Some example of the ORL face database that has scale, illumination, expression and pose

Fig. 3: Mean image, \(\Psi\)

The eigenfaces used for each training images and unknown images to determine its weight vectors to describe class identity (equation 5). These features are used for classification and recognize the unknown human face.
Table 1: Example the original weight feature vectors, $\Omega^T$

<table>
<thead>
<tr>
<th>$\Gamma_i$</th>
<th>$W_1$</th>
<th>$W_2$</th>
<th>$W_3$</th>
<th>$W_4$</th>
<th>$W_5$</th>
<th>$W_6$</th>
<th>$W_7$</th>
<th>$W_8$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\Gamma_1$</td>
<td>7774753.959189</td>
<td>8002601.177177</td>
<td>6917700.938766</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\Gamma_2$</td>
<td>27859705.231132</td>
<td>32696166.830578</td>
<td>29307673.817428</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\Gamma_3$</td>
<td>-4875383.270625</td>
<td>-6547910.700724</td>
<td>-6594768.822582</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\Gamma_4$</td>
<td>-4820597.908669</td>
<td>-6032421.641661</td>
<td>-6834500.429694</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\Gamma_5$</td>
<td>-6717293.696702</td>
<td>-7592655.784587</td>
<td>-7268246.998013</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\Gamma_6$</td>
<td>-7518927.783058</td>
<td>-9070221.819864</td>
<td>-7926633.853074</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 2: Example normalization feature vectors

<table>
<thead>
<tr>
<th>$\Gamma_i$</th>
<th>$W_1$</th>
<th>$W_2$</th>
<th>$W_3$</th>
<th>$W_4$</th>
<th>$W_5$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\Gamma_1$</td>
<td>0.539188</td>
<td>1.000000</td>
<td>0.154948</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\Gamma_2$</td>
<td>0.010280</td>
<td>1.000000</td>
<td>0.306589</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\Gamma_3$</td>
<td>1.000000</td>
<td>0.162313</td>
<td>0.138844</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\Gamma_4$</td>
<td>1.000000</td>
<td>0.417547</td>
<td>0.032034</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\Gamma_5$</td>
<td>0.647926</td>
<td>0.000000</td>
<td>0.240121</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\Gamma_6$</td>
<td>0.643505</td>
<td>0.000000</td>
<td>0.474381</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 3: Training Result using Backpropagation Neural Network

<table>
<thead>
<tr>
<th>Pattern</th>
<th>Actual Target</th>
<th>Network Output</th>
<th>MSE</th>
</tr>
</thead>
<tbody>
<tr>
<td>s1</td>
<td>0 0 0</td>
<td>0.023054</td>
<td>0.017150</td>
</tr>
<tr>
<td>s1</td>
<td>0 0 0</td>
<td>0.066030</td>
<td>0.008177</td>
</tr>
<tr>
<td>s2</td>
<td>0 0 1</td>
<td>0.006697</td>
<td>0.017725</td>
</tr>
<tr>
<td>s3</td>
<td>0 1 0</td>
<td>0.005084</td>
<td>0.015986</td>
</tr>
<tr>
<td>s4</td>
<td>0 1 0</td>
<td>0.006870</td>
<td>0.013192</td>
</tr>
<tr>
<td>s5</td>
<td>0 1 1</td>
<td>0.001566</td>
<td>0.987113</td>
</tr>
<tr>
<td>s6</td>
<td>1 0 0</td>
<td>0.994456</td>
<td>0.004343</td>
</tr>
<tr>
<td>s7</td>
<td>1 0 1</td>
<td>0.893595</td>
<td>0.002024</td>
</tr>
<tr>
<td>s8</td>
<td>1 1 0</td>
<td>0.988798</td>
<td>0.017077</td>
</tr>
<tr>
<td>s9</td>
<td>1 1 1</td>
<td>0.988189</td>
<td>0.015871</td>
</tr>
<tr>
<td>s10</td>
<td>1 1 0</td>
<td>0.991254</td>
<td>0.978264</td>
</tr>
<tr>
<td>s11</td>
<td>1 1 0</td>
<td>0.983754</td>
<td>0.999764</td>
</tr>
<tr>
<td>s12</td>
<td>1 1 1</td>
<td>0.956998</td>
<td>0.998838</td>
</tr>
<tr>
<td>s13</td>
<td>1 1 1</td>
<td>0.965853</td>
<td>0.999469</td>
</tr>
</tbody>
</table>

Some previous work$^{12,11}$ used these features to recognize unknown human face using euclidean distance. Table 1, shows the example result of weight vectors for 16 images (8 classes with 2 images per-class).

The features vectors used into backpropagation neural network for classification and recognition human faces$^{13,12,13}$. Before the learning phase, the previous feature vectors $\Omega^T$ is normalize to a range (0, 1) to meet the backpropagation neural network requirement, avoid computational problems and to facilitate learning$^{14}$. Table 2 shows the normalizes features (0, 1) from the original features in Table 1.

The backpropagation neural network is used for the classification and recognition purposes. Table 3 shows the training results using neural network. In this experiment, 16 patterns are used, 8 inputs per-pattern, 5 hidden neurons, 3 output neurons, 0.9 for momentum, 0.7 for learning rate and the error were set to 0.001 for stopping condition.

In the recognition step, the identity of human face is determined if any network output error value is less
Eigenfaces; $U_1$ to $U_8$

Eigenfaces; $U_3$ to $U_10$

Fig. 4: The eigenfaces from class $s_1$ to $s_8$ with 2 image per-class

Eigenfaces; $U_1$ to $U_8$

Eigenfaces; $U_{16}$ to $U_{24}$

Fig. 5: The eigenfaces from class $s_1$ to $s_8$ with 4 images per-class

Eigenfaces; $U_{25}$ to $U_{32}$

Fig. 6: The eigenfaces from class $s_1$ to $s_8$, 6 images per-class

than error (0.001). The recognition rate worked perfectly if the entire training pattern used for recognition. The recognition performance is decrease dramatically if only one image per class used in learning phase. However, when face images with different pose are added in learning step, the recognition rate increase.

CONCLUSION

In this study, we used the eigenfaces to represent the features vectors for human faces. The features are extracted from the original image to represents unique identity used as inputs to the neural network to measure similarity in classification and recognition. The eigenfaces has proven the capability to provide the significant features and reduces the input size for neural network. Thus, the network speed for recognition is raise.

REFERENCES