A protection strategy for micro-grids based on positive-sequence component

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Abstract: In recent years, the concept of micro-grid has appeared as an appropriate way for the integration of distributed energy resources (DERs) in the distribution networks. However, micro-grids have encountered a number of challenges from control and protection aspects. One of the main issues relevant to the protection of micro-grids is to develop a suitable protection technique which is effective in both grid-connected and stand-alone operation modes. This study presents a micro-grid protection scheme based on positive-sequence component using phasor measurement units and designed microprocessor-based relays (MBRs) along with a digital communication system. The proposed scheme has the ability to protect radial and looped micro-grids against different types of faults with the capability of single-phase tripping. Furthermore, since the MBRs are capable of updating their pickup values (upstream and downstream equivalent positive-sequence impedances of each line) after the first change in the micro-grid configuration (such as transferring from grid-connected to islanded mode and/or disconnection of a line, bus or DER either in grid-connected mode or in islanded mode), they can protect micro-grid lines and buses against subsequent faults. Finally, in order to verify the effectiveness of the suggested scheme and the designed MBR, several simulations have been undertaken using DlgSILENT PowerFactory and MATLAB software packages.

1 Introduction

The recent progresses in technology and the increasing concerns associated with global warming have motivated researchers to explore cleaner and more efficient systems. To mitigate the negative influences of fossil fuel-based generation on the environment, a novel approach is to produce electricity by cleaner distributed energy resources (DERs) in the vicinity of the customers’ sites [1–3]. For this reason, the utilisation of DERs such as wind turbines, photovoltaic systems, micro gas turbines and fuel cells has attracted more attention in recent years.

One suggested way for the integration of widespread proliferation of DERs is through micro-grids. Micro-grid is substantially defined as a collection of electrical/heat loads, parallel DERs and energy storage devices which can function in grid-connected or islanded mode [4–7]. The micro-grid protection philosophy is that it functions in grid-connected mode of operation under normal circumstances, but in case a fault takes place in the main grid side, it is disconnected from the rest of the network and is transferred to the islanded mode [8–10].

The most significant advantage of micro-grid is that it can provide high-reliability and high-quality power for the customers who need uninterruptible power supplies. In addition, a significant cost saving comes from the application of combined heat and power systems in micro-grids. Notwithstanding numerous advantages provided by micro-grids, they may pose some technical challenges which need to be fulfilled for researchers. Micro-grid protection and its entities is one of them [11–13]. Protection of micro-grids cannot be attained by the same philosophies which have traditionally been applied in distribution networks. The reason is that a protection scheme for micro-grids should take the followings into account: (a) bidirectional power flow in feeders; (b) existence of looped feeders; (c) decreased magnitude of the fault current in stand-alone operation mode [14–16]. As a result, the traditional overcurrent-based protection strategies are ineffective for micro-grids and some alternative strategies should be employed.

In a study by Oudalov and Fidigatti [17], an adaptive protection strategy was suggested, applying digital relaying and advanced communication technique. In the presented technique, the protection settings were updated periodically by means of micro-grid central controller in accordance with micro-grid operating modes. However, the proposed strategy necessitated updating or upgrading the protection devices which are presently applied in the distribution networks; moreover, fault calculations were relatively sophisticated for a micro-grid functioning in different modes. Dewadasa and his research group [18, 19] proposed an additional methodology for inverter-based micro-grids using an admittance relay with inverse time tripping characteristics. Despite the fact that the methodology had the ability to protect micro-grids either in grid-connected or in stand-alone mode, it was unable to protect micro-grids including rotating-based DERs. The further shortcoming of the strategy was that it was designed for only radial micro-grids. Tumility et al. [20] and Redfern and Al-Nasser [21] put forward a new protection approach based on voltage measurements to protect autonomous micro-grids against different kinds of faults. Nevertheless, the suggested approach did not take account of grid-connected operating mode as well as single-phase tripping. Jayawarna et al. [22, 23] proposed the installation of energy storage devices (such as batteries, flywheels etc.) within the micro-grid to equalise the magnitude of short-circuit current in both grid-connected and stand-alone modes of operation. By the application of such devices, micro-grid could still be protected using conventional overcurrent-based protection, but required adaptive protective devices. The major drawback of the proposed strategy was that the cost pertaining to such devices with high short-circuit capacity was extremely disadvantageous. In a study by Sortomme et al. [24], a differential based protection strategy was introduced which was able to protect micro-grids including radial or looped feeders in both modes of operations. However, the suggested strategy was only effective for the protection of lines and had not the ability to protect buses connected to DERs or loads. Nikkhajoei and Lasseter [25] established an alternative protection method based on
symmetrical components. The authors applied zero- and negative-sequence currents to protect micro-grids against asymmetrical faults. However, the suggested technique was ineffective in detecting three-phase faults; besides, the capability of single-phase tripping had not been taken into account in the method. Subsequently, in a research by Zamani et al. [26] another protection strategy was devised using zero- and negative-sequence components which had the ability to protect micro-grids against different kinds of faults; moreover, the proposed strategy did not require communication system. The main problem associated with the proposed method was that it was dependent on the micro-grid configuration, because the method had been designed for only radial micro-grids and was not capable of protecting micro-grids containing looped feeders; furthermore, because of the need for zero-sequence current in the proposed method, its implementation necessitated the application of a specific type of transformer (only grounded transformers) inside the micro-grid.

This paper presents a micro-grid protection scheme based on positive-sequence component using phasor measurement units (PMUs) and designed microprocessor-based relays (MBRs) along with a digital communication system. The proposed scheme has the ability to protect radial and looped micro-grids against different types of faults with the capability of single-phase tripping. Furthermore, since the MBRs are capable of updating their pickup values after the first change in the micro-grid configuration, they can protect micro-grid lines and buses against subsequent faults.

The remainder of this paper is organised as follows: in Section 2, technical challenges in the protection of micro-grids are discussed; Section 3 describes the proposed protection scheme; in Section 4, different parts of the designed MBR are introduced; Section 5 is dedicated to the simulation results; and finally, Section 6 concludes this paper.

2 Technical challenges in the protection of micro-grids

The majority of the distribution networks are designed to operate in radial mode, in which the power flows in one direction from higher-voltage levels to lower-voltage levels. Owing to this, the protection of such networks is accomplished using simple and relatively low-cost overcurrent-based protective devices such as overcurrent relays, reclosers and fuses. When a micro-grid is formed in a distribution network, the configuration is changed to a complicated multi-source power system. The protection of micro-grid should be in such a way that a safe and second protection is provided in both grid-connected and stand-alone operation modes [27, 28]. Nevertheless, the function of micro-grid in these two modes creates some new protection problems. During grid-connected operation mode, since micro-grid provides a large short-circuit current to the fault point, the protection can be performed by existing protective devices within the distribution networks, but in islanded mode, fault currents are drastically lower than those of grid-connected mode. The reason is that the Thevenin’s impedance viewed from the fault point in islanded operating mode is much higher than that of grid-connected mode; hence, the employment of traditional overcurrent-based protective devices in micro-grids is no longer valid and some alternative protection schemes should be developed.

Table 1 Existence of symmetrical components during different types of faults

<table>
<thead>
<tr>
<th>Fault type</th>
<th>Positive-sequence</th>
<th>Negative-sequence</th>
<th>Zero-sequence</th>
</tr>
</thead>
<tbody>
<tr>
<td>single line to ground</td>
<td>yes</td>
<td>yes</td>
<td>yes</td>
</tr>
<tr>
<td>line to line</td>
<td>yes</td>
<td>yes</td>
<td>no</td>
</tr>
<tr>
<td>line to line to ground</td>
<td>yes</td>
<td>yes</td>
<td>yes</td>
</tr>
<tr>
<td>three phase</td>
<td>yes</td>
<td>no</td>
<td>no</td>
</tr>
</tbody>
</table>

3 Proposed protection scheme

This paper presents a protection scheme for micro-grids using PMUs and designed MBRs, thereby detecting different kinds of faults in both grid-connected and islanded modes of operation. In the proposed protection scheme, PMUs which are responsible for extracting voltage and current phasors (magnitudes and their respective phasor angles) based on digital sampling of alternating current (AC) waveforms are installed at both ends of each line of micro-grid. Subsequently, the information extracted by PMUs of each line is transferred to the MBR of that line through a digital communication system. After a fault incident within the micro-grid, the information received by PMUs in all MBRs is analysed, and then the fault occurrence, location of fault and faulted phases are recognised by the relevant MBR or MBRs. Subsequently, depending on the fault type, proper tripping signals are issued to the relevant circuit breakers.

3.1 Detection of fault incident

To detect different types of faults, this paper presents a protection scheme based on symmetrical components approach. The approach, developed by Fortescue, is one of the most effective ones which is applied to transform a three-phase unbalanced system into three sets of symmetrically balanced phasors, namely positive-, negative- and zero-sequence components. In case a fault strikes within a network, these symmetrical components are formed depending on the fault type. Table 1 illustrates the existence of symmetrical components during different types of faults. As can be seen from this table, the positive-sequence is the only component which exists in all types of faults. For this reason, in this paper, the positive-sequence component is employed to detect different kinds of faults.

3.2 Detection of fault location

As mentioned earlier, the majority of the proposed methods to date are strongly dependent on the micro-grid configuration. To possess an appropriate method having the ability to protect different micro-grids with different configurations, micro-grid feeders should be sectionised in such a way that each section (micro-grid’s line or bus) is protected independent of other sections. To fulfil this, the upstream and downstream of each line are replaced with its upstream and downstream equivalent circuits, respectively. Both of these equivalent circuits include a voltage source in series with impedance. Fig. 1 indicates the upstream and downstream equivalent circuits of Line 12 of a typical micro-grid during a fault.

During a fault occurrence in Line 12 of Fig. 1, different symmetrical components are created depending on the fault type. The equivalent circuit diagram in the system of symmetrical components for different kinds of faults by considering upstream and downstream equivalent circuits are depicted in Fig. 2.

By replacing the equivalent impedance of negative- and zero-sequence networks between terminals AB of positive-sequence network for all types of faults, a general model for the analysis of different kinds of faults can be developed. The developed model is demonstrated in Fig. 3, in which impedance $Z_{eq2.0}$ is the representative of negative- and zero-sequence networks.

Depending on the fault type, the value of the impedance is different. Equation (1) expresses the value of impedance $Z_{eq2.0}$ for different types of faults

$$Z_{eq2.0} = \begin{cases} 
Z_{eq0} + Z_{eq2}, & \text{for single line to ground faults} \\
Z_{eq2}, & \text{for line to line faults} \\
Z_{eq0}|Z_{eq2}|, & \text{for line to line to ground faults} \\
0, & \text{for three-phase faults}
\end{cases}$$

IET Renew. Power Gener., 2015, Vol. 9, Iss. 6, pp. 600–609
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Fig. 1  Upstream and downstream equivalent circuits of Line12 of a typical micro-grid during a fault

Fig. 2  Equivalent circuit diagram in the system of symmetrical components by considering upstream and downstream equivalent circuits for
a. Single line to ground fault
b. Line to line to ground fault
c. Line to line fault
d. Three-phase fault
where

\[
Z_{eq0} = (Z_{U0} + Z_{LU0})||(Z_{D0} + Z_{LD0})
\]

\[
Z_{eq2} = (Z_{U2} + Z_{LU2})||(Z_{D2} + Z_{LD2})
\]

In the proposed protection scheme, after the detection of fault incident, the faulted section is recognised by the developed model of Fig. 3 in such a way as to compare the value of upstream and downstream equivalent positive-sequence impedances, before and after the fault. In fact, when a fault occurs inside a line, impedance \(Z_{eq2,0}\) is created between points C and D. Therefore the values of both upstream and downstream equivalent positive-sequence impedances after the fault \((Z_{U1}, Z_{D1})\) remain equal to the values of those impedances before the fault \((Z_{U1(pre)}, Z_{D1(pre)})\), but in case a fault occurs at the upstream or downstream of a line, respectively, only the value of \(Z_{D1}\) or only the value of \(Z_{U1}\) remains constant after the fault.

It should be noted that, in the proposed protection scheme, since the total positive-sequence impedance of each line is calculated using the positive-sequence voltage and current phasors, obtaining time-synchronised measurements from its both ends is necessary. However, in short distribution lines, the proposed scheme can function without the need for PMUs.

Fig. 4 demonstrates the single-phase diagram of the proposed protection scheme for Line 12 of the micro-grid shown in Fig. 1. According to this figure, after a fault occurrence inside of Line12, both values of \(Z_{D1}\) and \(Z_{U1}\) of MBR_Line12 remain constant; in fact, both PMU13 and PMU14 see the fault in their forward side, so PMU13 and PMU14 Forward Fault Trip signals from MBR_Line12 are issued to both CB13 and CB14, but in case of a fault at Bus11, the values of \(Z_{D1}\) of MBR_Line12 and \(Z_{U1}\) of MBR_Line11 remain constant, so PMU12 and PMU13 Reverse Fault Trip signals are issued, respectively, from MBR_Line11 and MBR_Line12, and disconnect CB12 and CB13. Similarly, in case of a fault incident at Bus12, PMU14 and PMU15 Reverse Fault Trip signals are issued, respectively, from MBR_Line12 and MBR_Line13 and disconnect CB14 and CB15.

As can be seen in this figure, the back-up protection is also provided in such a way that after any failure in the main protection of each line or bus, the disconnection signals are issued to its adjacent circuit breakers after a pre-determined time delay to isolate the smallest possible faulted area.

4 Designed MBR

Fig. 5 displays the schematic diagram of MBR_Line12. As can be seen in this figure, it consists of four main parts, namely, fault incident detector, fault locator, faulty phase detector and blocking signal issue-maker, each of which are described in detail in the following sections.

4.1 Fault incident detector

As explained earlier, the positive-sequence component is the only component which exists in all types of faults. Therefore, in the proposed protection scheme, the component is used to detect
Fig. 5  Schematic diagram of MBR_Line12
different kinds of faults. When a fault occurs in a micro-grid section (line or bus), the positive-sequence current magnitude of that section is increased; hence, the fault occurrence can be detected by comparing the magnitude before and after the fault.

In the designed MBR, for the detection of fault in each line and its adjacent buses, a fault incident detector is allocated. However, since a fault in one section may increase the positive-sequence current magnitude of other sections, MBRs related to non-faulted lines may issue fault trip signals mistakenly. Hence, the deployment of an additional detector (fault locator) is necessary.

4.2 Fault locator

As mentioned in Section 3.2, the faulted section is identified based on changes in the values of upstream and downstream equivalent positive-sequence impedances before and after the fault. In the designed MBR, this function is performed by fault locator. Prior to fault incident, the fault locator respective to MBR of each line, first, calculates the values of Thevenin’s equivalent positive-sequence impedances (TEPSIs) at both ends of that line, and then it deploys the values to determine the values of impedances $Z_{U1(\text{pre})}$ and $Z_{D1(\text{pre})}$.

Finally, the faulted section can be recognised by comparing the values of upstream and downstream equivalent positive-sequence impedances before ($Z_{U1(\text{pre})}$, $Z_{D1(\text{pre})}$) and after ($Z_{U1}$, $Z_{D1}$) the fault.

To determine the TEPSI of each point within the micro-grid, this paper introduces an online methodology using three consecutive voltage and current measurements of PMUs at different time instants. Since any changes in the frequency of the micro-grid system will lead to slip between micro-grid frequency system and the PMU sampling frequency, phase angles of voltage and current for these three measurements will be different.

On the basis of Thevenin’s model, the node positive-sequence voltage equation is defined as

$$V_1 = E_t - Z_t \cdot I_t \quad (2)$$

According to (2), the positive-sequence voltage equation for PMU13 terminals becomes

$$V_{1PMU13} = E_{tPMU13} - Z_{tPMU13} \cdot I_{tPMU13} \quad (3)$$

where $E_{tPMU13}$ = Thevenin’s equivalent positive-sequence voltage source at PMU13 terminals, $Z_{tPMU13}$ = TEPSI at PMU13 terminals.

![Positive-sequence phasor diagrams for two different measurements at PMU13 terminals](image)
Positive-sequence phasor diagrams of (3) for two different measurements at PMU13 terminals are indicated in Fig. 6.

Since $E_{1PMU13}$ is the Thevenin’s positive-sequence equivalent voltage source, its magnitude for both measurements are identical, but its angle in the IInd measurement is shifted by an angle equal to the phase drift. Referring to Fig. 6, $E_{1PMU13}$ equation for the 1st measurement can be written as

$$E_{1PMU13}^2 = V_{1PMU13}^2 + I_{1PMU13}^2 \cdot Z_{1PMU13}^2 + 2V_{1PMU13} \cdot I_{1PMU13} \cdot Z_{1PMU13} \cdot \cos(\theta + \varphi_1) \tag{4}$$

By expanding $\cos(\theta + \varphi_1)$, (4) can be expressed as follows

$$E_{1PMU13}^2 = V_{1PMU13}^2 + I_{1PMU13}^2 \cdot Z_{1PMU13}^2 + 2V_{1PMU13} \cdot I_{1PMU13} \cdot R_{1PMU13} - 2Q_{1PMU13} \cdot X_{1PMU13} \tag{5}$$

where $R_{1PMU13}$ and $X_{1PMU13}$ denote the resistance and reactance of the TEPSI, as well as $V_{1PMU13}$, $I_{1PMU13}$, and $Q_{1PMU13}$, which, respectively, represent active and reactive powers flowing through Line 12. Similarly, the $E_{1PMU13}$ equation for the IInd measurement can be written as

$$E_{1PMU13}^2 = V_{1PMU13}^2 + I_{1PMU13}^2 \cdot Z_{1PMU13}^2 + 2V_{1PMU13} \cdot I_{1PMU13} \cdot R_{1PMU13} - 2Q_{1PMU13} \cdot X_{1PMU13} \tag{6}$$

By subtracting (6) from (5)

$$V_{1PMU13}^2 - V_{1PMU13}^2 + (I_{1PMU13}^2 - I_{1PMU13}^2) \cdot Z_{1PMU13}^2 + 2(V_{1PMU13} - V_{1PMU13}) \cdot I_{1PMU13} - 2Q_{1PMU13} \cdot X_{1PMU13} = 0 \tag{7}$$

Equation (7) can be arranged as follows

$$\left(\frac{R_{1PMU13} + \frac{P_{1PMU13}}{I_{1PMU13}^2} - \frac{P_{1PMU13}}{I_{1PMU13}^2}}{R_{1PMU13} - \frac{P_{1PMU13}}{I_{1PMU13}^2} - \frac{P_{1PMU13}}{I_{1PMU13}^2}}\right)^2 + \left(\frac{X_{1PMU13} - \frac{Q_{1PMU13}}{I_{1PMU13}^2} - \frac{Q_{1PMU13}}{I_{1PMU13}^2}}{I_{1PMU13} - \frac{Q_{1PMU13}}{I_{1PMU13}^2} - \frac{Q_{1PMU13}}{I_{1PMU13}^2}}\right)^2 = \left(\frac{V_{1PMU13}^2}{I_{1PMU13}^2} - \frac{P_{1PMU13}^2 - P_{1PMU13}^2}{I_{1PMU13}^2 - \frac{P_{1PMU13}^2}{I_{1PMU13}^2} + \frac{P_{1PMU13}^2}{I_{1PMU13}^2} - \frac{P_{1PMU13}^2}{I_{1PMU13}^2}}\right)^2 + \left(\frac{Q_{1PMU13}^2 - \frac{Q_{1PMU13}^2}{I_{1PMU13}^2}}{I_{1PMU13}^2 - \frac{Q_{1PMU13}^2}{I_{1PMU13}^2} - \frac{Q_{1PMU13}^2}{I_{1PMU13}^2}}\right)^2 \tag{8}$$

This is the equation of a circle in the positive-sequence impedance plane which indicates a locus for the TEPSI seen from PMU13 terminals. As it does not specify a certain value for $Z_{1PMU13}$, a third measurement is required so that it is used with the first and second measurements to create another two circles for $Z_{1PMU13}$. Fig. 7 shows the positive-sequence impedance plane including the circles obtained from three different measurements. As shown in Fig. 7, the value of TEPSI seen from PMU13 terminals is specified by the intersection of the three circles.

According to Thevenin’s theorem, Thevenin’s equivalent impedance for any two-terminal of the network is the impedance seen from those terminals when the sources are set to zero. Hence, $Z_{1PMU13}$ for PMU13 terminals prior to fault incident is equivalent to $Z_{1PMU13}(Z_{1} + Z_{D})$. By setting this equal to the calculated $Z_{1PMU13}$ from the intersection point of the three circles

$$Z_{1PMU13} = Z_{U1}(pre)\left(Z_{L} + Z_{D}(pre)\right) \tag{9}$$

By following the same procedure for PMU14 terminals prior to fault incident

$$Z_{1PMU14} = Z_{D1}(pre)\left(Z_{L} + Z_{U1}(pre)\right) \tag{10}$$

![Fig. 7 Positive-sequence impedance plane including the circles obtained from three different measurements](image-url)
By solving (9) and (10), the values of $Z_{U1(pre)}$ and $Z_{D1(pre)}$ are obtained. Subsequently, the fault locator respective to each line compares the values of $Z_{U1(pre)}$ and $Z_{D1(pre)}$ with the values of $Z_{U1}$ and $Z_{D1}$ after the fault incident and identifies the faulted section.

4.3 Faulty phase detector

Single-phase tripping capability has long been regarded as an effective way of improving system security and reliability. It leads to removal of unnecessary interruptions of the unaffected phases in case the fault does not involve all three phases. In the designed MBR, having detected the faulted section by means of the fault locator, the affected phases of that section are identified through faulty phase detector. The faulty phase detector compares the current magnitude of each phase of the faulted section before and after the fault, and then issues the proper disconnection signals to the relevant circuit breakers of that section.

4.4 Blocking signal issue-maker

To update the values of $Z_{U1(pre)}$ and $Z_{D1(pre)}$ as well as precluding from mal-operation of MBRs for the subsequent faults, a blocking signal issue-maker has been considered. In fact, after the isolation of the first fault (inside or outside of micro-grid) a fault incident signal is issued from the disconnected circuit breakers to the central protection unit (CPU). Afterwards, CPU sends the signal to all MBRs in the micro-grid. The signal is responsible for resetting the memories as well as blocking the outputs of all MBRs until the new values of $Z_{U1(pre)}$ and $Z_{D1(pre)}$ are determined. To fulfil this, a positive edge-triggered monostable multivibrator is used. Once it received a fault incident signal resulted from the disconnection of circuit breakers, generates an output pulse with the duration of $T$. It is clear that the duration of the pulse should be more than the time which is needed so that the values of $Z_{U1(pre)}$ and $Z_{D1(pre)}$ are updated.

5 Simulation results

To evaluate the effectiveness of the proposed scheme and the designed MBR, several simulations have been carried out using DlgSILENT PowerFactory and MATLAB software packages. The configuration of the simulated micro-grid, which hereinafter is
referred to as ‘study micro-grid’ as well as the case studies are presented in the following sections.

5.1 Study micro-grid

The single-line diagram of the study micro-grid is illustrated in Fig. 8. As can be seen in this figure, the study micro-grid is connected to the main grid by means of a 69 kV/24.9 kV Dyn transformer. It also includes two photovoltaic parks (640 kW) and one wind farm (504 kW) which are interfaced with the network through respective Yyn transformers. The information associated with the applied transformers and loads of the study micro-grid is listed in Tables 2 and 3.

5.2 Case studies

To prove the efficacy of the proposed protection scheme in the grid-connected and islanded operating modes, the performance of several MBRs was simulated, but because of space restriction and format requirements of this publication, only the simulation results of MBR_Line203 is included in this paper. The simulation results showed that the suggested protection scheme can provide a robust protection against different kinds of faults.

Table 2 Information associated with the applied transformers in the study micro-grid

<table>
<thead>
<tr>
<th>Transformer type</th>
<th>HVb, kV</th>
<th>LVb, kV</th>
<th>Vector group</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tr-1</td>
<td>69</td>
<td>24.9</td>
<td>Dyn0</td>
</tr>
<tr>
<td>Tr-2</td>
<td>24.9</td>
<td>0.4</td>
<td>YNyn0</td>
</tr>
<tr>
<td>Tr-3</td>
<td>24.9</td>
<td>0.4</td>
<td>YNyn0</td>
</tr>
<tr>
<td>Tr-4</td>
<td>24.9</td>
<td>0.4</td>
<td>YNyn0</td>
</tr>
</tbody>
</table>

*aHigh voltage, bLow voltage

Table 3 Information associated with the loads in the study micro-grid

<table>
<thead>
<tr>
<th>Name</th>
<th>Phase A</th>
<th>Phase B</th>
<th>Phase C</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>kW</td>
<td>kVAR</td>
<td>kW</td>
</tr>
<tr>
<td>Load201</td>
<td>100</td>
<td>16</td>
<td>75</td>
</tr>
<tr>
<td>Load203</td>
<td>175</td>
<td>22</td>
<td>53</td>
</tr>
<tr>
<td>Load401</td>
<td>14</td>
<td>5</td>
<td>77</td>
</tr>
<tr>
<td>Load402</td>
<td>93</td>
<td>26</td>
<td>24</td>
</tr>
<tr>
<td>Load403</td>
<td>111</td>
<td>38</td>
<td>28</td>
</tr>
</tbody>
</table>

Table 4 Simulation results of MBR_Line203 during different kinds of faults at the midpoints of Lines 203 and 302 (F1 and F2 in Fig. 8) in the grid-connected operating mode

<table>
<thead>
<tr>
<th>Fault location</th>
<th>Phase A</th>
<th>Phase B</th>
<th>Phase C</th>
</tr>
</thead>
<tbody>
<tr>
<td>PMU203 (U)</td>
<td>AGc</td>
<td>BCc</td>
<td>BCGc</td>
</tr>
<tr>
<td>PMU203 (D)</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

According to the simulation results, the calculated values of upstream and downstream equivalent positive-sequence impedances (from the intersection of circles) for Line 203 before the fault incidents in both grid-connected and islanded operating modes are as follows

\[ Z_{U1 \, L203} \text{ (pre)cal} = \begin{cases} 8.7499 \Omega & \text{for grid-connected mode} \\ 47.1347 \Omega & \text{for islanded mode} \end{cases} \]

\[ Z_{D1 \, L203} \text{ (pre)cal} = \begin{cases} 8.5499 \Omega & \text{for grid-connected mode} \\ 77.059 \Omega & \text{for islanded mode} \end{cases} \]

where \( Z_{U1 \, L203} \text{ (pre)cal} = \) upstream equivalent positive-sequence impedance of PMU203 (U), \( Z_{D1 \, L203} \text{ (pre)cal} = \) downstream equivalent positive-sequence impedance of PMU203 (D).

Tables 4 and 5 indicate the simulation results of MBR_Line203 during different kinds of faults at the midpoints of Lines 203 and 302 (F1 and F2 in Fig. 8) in both grid-connected and islanded operating modes, respectively.

As can be seen from these tables, the positive-sequence current magnitudes during different types of faults in islanded mode are drastically lower than those of grid-connected mode. It is due to the fact that the Thevenin’s impedance viewed from the fault points (F1 and F2) in islanded operating mode is much higher than that of grid-connected mode; therefore, traditional over-current strategies with a single setting group will not be able to provide selective trips for all types of faults in both grid-connected and islanded modes of operation.

Once fault F1 or F2 occurred either in grid-connected or islanded mode, MBR_Line203 calculates the values of \( Z_{U1 \, L203} \) and \( Z_{D1 \, L203} \), and then compares them, respectively, with the values of \( Z_{U1 \, L203} \text{ (pre)cal} \) and \( Z_{D1 \, L203} \text{ (pre)cal} \). According to Tables 4 and 5, since Fault F1 has occurred inside of Line 203, the values of \( Z_{U1 \, L203} \) and \( Z_{D1 \, L203} \) are, respectively, equal to the values of \( Z_{U1 \, L203} \text{ (pre)cal} \) and \( Z_{D1 \, L203} \text{ (pre)cal} \), whereas fault F2 has occurred at the downstream of Line 203, and therefore only the value of \( Z_{U1 \, L203} \) is equal to the value of \( Z_{U1 \, L203} \text{ (pre)cal} \).

6 Conclusion

This paper proposed a protection strategy based on positive-sequence component for micro-grids. The proposed strategy which addresses the protection issues of a micro-grid in both modes of operation is implemented through PMUs and
Table 5 Simulation results of MBR_Line203 during different kinds of faults at the midpoints of Lines 203 and 302 (F1 and F2 in Fig. 8) in the islanded operating mode

<table>
<thead>
<tr>
<th>Fault location</th>
<th>AG</th>
<th>BC</th>
<th>BCG</th>
<th>ABC</th>
</tr>
</thead>
<tbody>
<tr>
<td>PMU203 (U)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$E_{PMU203(U)}$</td>
<td>10.988</td>
<td>11.3099</td>
<td>9.1148</td>
<td>9.743</td>
</tr>
<tr>
<td>$E_{D1} - E_{PMU203(U)}$</td>
<td>3.2179</td>
<td>2.9887</td>
<td>5.164</td>
<td>4.5415</td>
</tr>
<tr>
<td>$I_{D1}$</td>
<td>-</td>
<td>-</td>
<td>109.5593</td>
<td>96.3516</td>
</tr>
<tr>
<td>$I_{D1}$</td>
<td>-</td>
<td>-</td>
<td>175.7082</td>
<td>159.1533</td>
</tr>
<tr>
<td>$E_{D1} - E_{PMU203(D)}$</td>
<td>1.3469</td>
<td>1.3456</td>
<td>183.5472</td>
<td>166.1232</td>
</tr>
<tr>
<td>$I_{D1}$</td>
<td>-</td>
<td>-</td>
<td>3.5419</td>
<td>3.4532</td>
</tr>
<tr>
<td>$I_{D1}$</td>
<td>-</td>
<td>-</td>
<td>3.4145</td>
<td>3.4062</td>
</tr>
<tr>
<td>$E_{D1} - E_{PMU203(D)}$</td>
<td>3.2345</td>
<td>4.2114</td>
<td>5.2147</td>
<td>6.3656</td>
</tr>
<tr>
<td>$I_{D1}$</td>
<td>-</td>
<td>-</td>
<td>4.9743</td>
<td>6.1499</td>
</tr>
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<td>$I_{D1}$</td>
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<td>-</td>
<td>111.1268</td>
<td>152.4975</td>
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<tr>
<td>$E_{D1}$</td>
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<td>-</td>
<td>3.5672</td>
<td>3.5578</td>
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<td>-</td>
<td>3.4145</td>
<td>3.4062</td>
</tr>
<tr>
<td>$E_{D1} - E_{PMU203(D)}$</td>
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<td>4.2114</td>
<td>5.2147</td>
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<td>-</td>
<td>-</td>
<td>3.4145</td>
<td>3.4062</td>
</tr>
</tbody>
</table>

operated CBs in Line 203
phase A | yes | no | no | no | yes | no | yes | no |
phase B | no | no | no | yes | no | yes | no | yes |
phase C | no | no | yes | no | yes | no | yes | yes |

References

Designed MBRs along with a digital communication system. The suggested scheme can protect radial and looped micro-grids against different types of faults with the capability of single-phase tripping. In addition, since the MBRs are capable of updating their pickup values after the first change in the micro-grid configuration, they can protect micro-grid lines and buses against subsequent faults. Finally, in order to demonstrate the efficacy of the proposed protection scheme and the designed MBR, several simulations were accomplished using DlgSILENT PowerFactory and MATLAB software packages.