# AREA-OPTIMAL CACHE COHERENT PROTOCOL FOR MANY-CORE NETWORK-ON-CHIP

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## DEDICATION

This thesis is dedicated to my father, who taught me that the best kind of knowledge to have been that which is learned for its own sake. It is also dedicated to my mother, who taught me that even the largest task can be accomplished if it is done one step at a time.

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#### ABSTRACT

Cache coherence support is a major component in network-on-chip (NoC) systems which consist of multiple processing cores or elements as it is essential to ensure that the changes in shared memory are well communicated between all cores. Due to the nature and architecture of NoC, cache coherence protocols can have different characteristics in terms of various design consideration factors such as performance, area and power. Since the number of cores are expected to increase more in computing systems in the future, these factors need to be appropriately considered for scalability during design process so that the implementation will be feasible and be able to maintain an effectiveness of the system design. Cache coherence protocols proposed for NoC systems such as the directory protocol, Hammer and token protocol each has different impact on execution performance and design cost associated, due to the different mechanism used to maintain the cache coherency. In this project, these protocols are implemented and simulated using the GEM5 simulator and the area overhead is estimated using the Multicore Power, Area, and Timing (McPAT) framework. The simulation using blackscholes, fluidanimate and bodytrack application from the Princeton Application Repository for Shared-Memory Computers (PARSEC) benchmark shows that the Hammer protocol outperforms all evaluated protocols in execution performance, but the area overhead required for the protocol is also the largest. Token protocol, on the other hand, provide a significant lower performance, which is 2% lower compared to the Hammer protocol, but its 7% area overhead incurred is the lowest among all protocols. This shows that token protocol exhibits the best scalability for area overhead with increasing number of processing cores while providing moderate performance in terms of execution time.

#### ABSTRAK

Sokongan kesepaduan cache ialah komponen utama dalam sistem rangkaianpada-chip (NoC) yang terdiri daripada berbilang teras pemprosesan atau elemen kerana ia adalah penting untuk memastikan bahawa perubahan dalam memori dikongsi dikomunikasi dengan baik antara semua teras. Disebabkan oleh sifat dan seni bina NoC, protokol kesepaduan cache mempunyai ciri yang berbeza dari segi pelbagai faktor pertimbangan reka bentuk seperti prestasi, kawasan dan kuasa. Memandangkan nombor teras dijangka akan meningkat dalam sistem komputer pada masa hadapan, faktor-faktor ini perlu dipertimbangkan dengan sewajarnya untuk kebolehskalaan semasa proses reka bentuk supaya implementasi boleh dilaksanakan dan dapat mengekalkan keberkesanan reka bentuk sistem. Protokol kesepaduan cache yang dicadangkan untuk sistem NoC seperti protokol direktori, Hammer dan token mempunyai kesan yang berbeza terhadap prestasi pelaksanaan dan kos reka bentuk, disebabkan oleh perbezaan mekanisme yang digunakan untuk mengekalkan kesepaduan cache. Dalam projek ini, protokol-protokol tersebut telah dilaksanakan dan disimulasikan menggunakan simulator GEM5 dan overhed kawasan telah dianggarkan menggunakan Multicore Power, Area, and Timing (McPAT). Simulasi menggunakan aplikasi blackscholes, fluidanimate dan bodytrack daripada Princeton Application Repository for Shared-Memory Computers (PARSEC) menunjukkan bahawa protokol Hammer mengatasi semua protokol dari segi prestasi perlaksanaan, tetapi overhead kawasan tambahan yang diperlukan juga adalah yang paling besar. Protokol token, sebaliknya, memberikan prestasi yang lebih rendah, iaitu 2% lebih rendah berbanding dengan protokol Hammer, tetapi overhed kawasannya sebanyak 7% adalah yang paling rendah antara semua protokol. Ini menunjukkan bahawa protokol token mempamerkan kebolehskalaan yang terbaik untuk overhed kawasan dengan peningkatan bilangan teras pemprosesan sambil memberikan prestasi sederhana dari segi masa pelaksanaan.

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## LIST OF ABBREVIATIONS

AMD	-	Advanced Micro Devices
CMP	-	Chip Multi-processor
DWP-D	-	Dynamic Way Partitioning Directory
FFT	-	Fast Fourier Transform
GEMS	-	General Execution-driven Multiprocessor Simulator
IRDS	-	International Roadmap for Devices and Systems
KNL	-	Knights Landing
McPAT	-	Multicore Power, Area, and Timing
NoC	-	Network-on-Chip
PARSEC	-	Princeton Application Repository for Shared-Memory Computers
PDE	-	Partial Differential Equation
ROI	-	Region-of-Interest
SLICC	-	Specification Language for Implementing Cache Coherence
SPH	-	Smoothed Paticke Hydrodynamics
XML	-	Extensible Markup Language

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#### **CHAPTER 1**

### **INTRODUCTION**

#### 1.1 Problem Background

Most of the electronic devices today feature more than single processor core [1], as a methodology to better harness the thread-level parallelism in order to improve the computing performance. It is evident that the approach of adding more and more processing cores which can be individually turned on or off is apparently an appropriate architectural decision made in most modern architectures. It can maintain the balance between both the maximum peak performance when necessary and efficient power consumption during idle period.

The 2015 International Roadmap for Devices and Systems (IRDS) report predicts a 30-fold increase in the number of processing cores by 2030 due to the increasing demand for information processing [2]. With the number of processing cores increases and multicore computer architecture will be the norm in future, the architectural paradigm is trending towards communication intensive from computationally intensive.

Network-on-chip (NoC) possess a huge amount of application potential, as relatively, conventional bus-based systems can no longer effectively handle the communication between the large number of cores and leads to performance bottleneck [3]. At the time being, NoC architectures are widely researched [4] as an on-chip interconnect in improving inter-core communication to maximize performance of multi-core systems. Crossbar switches are not scalable when the number of processing elements increase to a certain extent. Since the shared interconnect becomes impractical as the cores increases [5], unordered point-to-point networks will be the mainstream interconnect technology [6].

With the introduction of NoC, associated challenges arise as the architecture per se when dealing with multi core system design considerations such as cache coherency [7]. Shared memory model provided to software programmers requires an efficient cache coherence support [6], to ensure all the changes made by processors in shared memory are communicated with all concerned processors in the system to maintain the overall order of instruction execution.

As in multi-core SoC designs, on-chip memory will be the mainstream paradigm used in NoC systems. Therefore, an efficient cache coherence protocol is a vital component in ensuring the optimum functioning and performance of a multi-core NoC system. Snooping based cache coherence protocol, which is common on conventional bus-based systems are not practical for NoC systems [6]. It is because its implementation does not scale well on systems with large number of cores, since it requires the usage of an impractically large interconnect bus while the snooping broadcast traffic incurred is also not feasible.

Therefore, cache coherence protocols such as directory [8], token [9] and Hammer [10] protocols, have been proposed as alternatives for unordered interconnect to address the shortcoming of the existing cache coherence methodologies. Since the number of processing elements are expected to exhibit an increasing trend, chip resources such as area utilization and power consumption is also expected to be increasing in the future computers.



Figure 1.1 Typical tiled chip multi-processor (CMP) structure [6].

### **1.2 Problem Statement**

With the current technology, it is possible that number of cores of multi core systems to be doubled every 18 months [11]. Scalability of various design parameters such as area and traffic will be a major challenge in chip design as the number of cores increases with the advancement in fabrication technology to boost both the computing performance and efficiency. When the number of cores in a system increases beyond some extend, not all protocols targeting implementation on unordered NoC will be well-adapted in terms of area and power overhead [4].

Chip area is among one of the most critical design constraints in today's chip design as cost of chip die is determined by chip area and chip power [12]. Furthermore, area-efficient designs will also result in a smaller size in the final end product, which is a desirable trait for designs which are targeting mobile platform market segment.

The directory protocol requires large chip area overhead as it utilises on-chip directory to store cache coherence information and the directory area grows with the number of processors. Hammer protocol on the other hand uses broadcast mechanism instead and requires less are overhead, giving slightly lower execution performance. Token protocol is based on token counting for cache coherence, hence also requires low area overhead, but can achieve comparatively better performance.

Therefore, it will be beneficial for multi core NoC systems to be optimally designed with the appropriate selection of the cache coherence protocol and architecture which exhibit good scalability for area overhead requirements.

## **1.3** Research Objectives

The primary goal of this proposal is to build a cache coherent multi core NoC system optimized for area scalability. Specifically, the objectives of this project are:

- I. To characterize the impact of various cache coherence protocols in terms of the execution performance.
- II. To validate and characterize using benchmark the cache coherence protocol with good scalability for area overhead.

#### 1.4 Scope of research

When the number of processors to be simulated increases, the simulation time will also increase significantly. Therefore, the simulated architecture will be targeting a NoC system with 4 processing cores. The interconnect network topology is 2-dimensional (2-D) mesh network. Due to lack of hardware for evaluation, the performance evaluation is done through simulation approach, utilizing the GEM5 NoC simulator.

The evaluation of the cache coherence protocols is carried out using the Princeton Application Repository for Shared-Memory Computers (PARSEC) [13], limited to a subset of the benchmark suite, focusing on workload applications with moderate or high intensity of memory access. The chip area for proposed models is obtained based on the simulator is subsequently used for analysis and comparison.

## **1.5** Report Organization

This report is organized into five chapters. In Chapter 2, the following chapter, presents a literature review of related works on cache coherent NoC design and the analysis on different cache coherence protocol proposals. Next, Chapter 3 illustrates the proposed research methodology in this work, which includes the overall experiment flow and validation procedures. The corresponding project results and discussion will be contained in Chapter 4 of this thesis. Last but not least, the execution performance and area overhead for various cache coherence protocols will be concluded in Chapter 5.

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