## LEAKY MODE EXPANSION FOR OPTICAL FIBRE SENSOR APPLICATION

# FOUZIYAH ABDULSALAM HAMID ALQAZOUIN

A project report submitted in partial fulfilment of the requirements for the award of the degree of Master of Engineering (Electronic and Telecommunication)

> School of Electrical Engineering Faculty of Engineering Universiti Teknologi Malaysia

> > JULY 2021

### DEDICATION

Specially dedicated to,

My father and mother, who are always praying for my success, as well as my beloved family, who has accompanied me throughout my struggle and success.

To my supervisor, who has helped, inspired, motivated, and advised me during this project,

Thank you to all of my friends who have helped me.

#### ACKNOWLEDGEMENT

I'd want to offer my in-depth gratitude to everyone who assisted me in completing my thesis in some form. First of all, I thank Allah the Almighty for providing me strength, guidance, and blessings.

My heartfelt thanks to my supervisor for his constant guidance and support. Finally, I'd like to express my indebtedness to everyone who has helped in making this project a success, whether directly or indirectly.

#### ABSTRACT

A multimode interference (MMI) based sensor for high refractive index sensing was proposed and demonstrated in this simulation work. The proposed sensor scheme works by a mode expansion according to leaky modes instead of traditionally used radiation modes. The simulation work tried to exhibit whether and how light delivered multimode interference before it worn out. The MMI structure that was used in the simulation consists of a Single-mode-Multimode-Single-mode (SMS) fibres configuration. In this structure, the multimode fibre (MMF) segment was assumed to have only the core while the cladding was discarded and has a specific length. This work exhibited high refractive index (RI) sensing based on the Guided-mode-Leakymode-Guided-mode (GLG) structure or the SMS fibre structure previously cited by comprehending the fundamental theories of leaky mode expansion. The work also attempted to analyse the effects of important parameters of leaky mode expansion on sensing performances such as length and diameter of MMF, and changing value of surrounding refractive index. The simulation work was performed utilising BeamProp software to ascertain the needed power intensity and RI sensitivity to excite light into the MMF for detection. The economical and simple sensor structure is ideal in numerous applications, including for detection, diagnosis, health determination, safety, environmental, liquid food, and water quality control.

#### ABSTRAK

Karya simulasi ini mencadangkan dan menunjukkan sensor berasaskan gangguan multimode (MMI) untuk pengindeksan indeks biasan tinggi. Skema sensor yang dicadangkan berfungsi melalui pengembangan mod berdasarkan mod kebocoran dan bukannya mod radiasi yang digunakan secara konvensional. Kerja simulasi cuba menunjukkan sama ada dan bagaimana cahaya memberikan gangguan multimode sebelum usang. Struktur MMI yang digunakan dalam simulasi terdiri daripada konfigurasi gentian mod tunggal-multimode-mod-tunggal (SMS). Dalam struktur ini, segmen serat multimode (MMF) dianggap hanya mempunyai inti sementara pelapisannya dibuang dan mempunyai panjang tertentu. Karya ini akan menunjukkan penginderaan indeks biasan tinggi (RI) berdasarkan struktur berpandu-mod-bocormod-berpandukan (GLG) atau struktur gentian SMS yang disebutkan sebelumnya dengan memahami teori-teori asas pengembangan mod kebocoran. Karya ini juga berusaha untuk menganalisis kesan parameter penting pengembangan mod kebocoran pada persembahan penginderaan seperti panjang dan diameter teras MMF, dan perubahan nilai indeks biasan sekitarnya. Kerja simulasi dilakukan menggunakan perisian BeamProp untuk menentukan intensiti daya yang diperlukan dan kepekaan RI untuk memancarkan cahaya ke MMF untuk penginderaan. Struktur sensor kos rendah dan sederhana diperlukan dalam banyak aplikasi termasuk untuk pengesanan, diagnosis, dan penentuan kesihatan, keselamatan, persekitaran, makanan cair, dan pengendalian kualiti air.

# TABLE OF CONTENTS

### TITLE

DECI	iii	
DEDI	iv	
ACK	NOWLEDGEMENT	v
ABST	TRACT	vi
ABST	`RAK	vii
TABI	LE OF CONTENTS	viii
LIST	OF TABLES	xi
LIST	OF FIGURES	xii xiv
LIST	OF ABBREVIATIONS	
LIST	OF SYMBOLS	XV
CHAPTER 1	INTRODUCTION	1
1.1	Project Background	1
1.2	Motivation of the Study	2
1.3	Problem Statement	2
1.4	Project Goal	2
1.5	Project Objectives	3
1.6 Scope of Project		3
1.7	Thesis Outline	4
CHAPTER 2	LITERATURE REVIEW	7
2.1	Introduction	7
2.2	Basic of Optical Fibre	7
	2.2.1 Brief History	8
	2.2.2 Optical Fibre Working Principle	9
	2.2.3 Types of Optical Fibres	10
	2.2.3.1 Single Mode Fibres	11
	2.2.3.2 Multimode Fibres	11

	2.2.4	Structure of Signal Mode-Multimoo Mode Optical Fibres	le-Signal 13
	2.2.5	Multimode Interference Effect (MMI)	14
	2.2.6	Optical Fibre Thread Modes	15
2.3	Optica	Fibre Advantages and Disadvantages	16
	2.3.1	Brief History of Fibre Optic Sensor	17
	2.3.2	Optical Fibre Sensing Principle	18
	2.3.3	Types Optical Fibre Sensors Classific Applications	ation and 20
		2.3.3.1 Extrinsic Fibre Optic Sensor	rs 20
		2.3.3.2 Intrinsic Fibre Optic Sensor	s 20
	2.3.4	Applications	21
	2.3.5	SMS Optical Fibre Sensors	22
2.4	Waveg	uide Mode	22
2.5	Leaky	Modes	24
2.6	Previo	is Studies	25
2.7	Resear	ch Direction	29
2.8	Chapte	r Summary	29
CHAPTER 3	RESE	ARCH METHODOLOGY	30
3.1	Introd	ction	30
3.2	Resear	ch Activities	30
3.3	Propos	al SMS Fibre Structure	31
3.4	Light l	ropagation Model in an SMS Fibre Str	ucture 32
3.5	Tools	nd Platforms	38
	3.5.1	The SMS Sensor's Design	39
		3.5.1.1 Design Simulation	39
		3.5.1.2 Refractive Index Setting	42
CHAPTER 4	RESU	LTS AND DISCUSSION	44
4.1	Overv	ew	44
4.2	Introd	ction	44

Appendices A	- C		68 - 73
REFERENCI	ES		64
5.2	Reco	mmendation	63
5.1	Conc	lusion	61
CHAPTER 5	CON	CLUSION	61
4.6	5 Sumr	nary	59
4.5	Resul	ts and Discussion	57
	4.4.1	The Result of SMS Sensor with Different Surrounding RI	45
4.4	The F	The Performance of an Improved SMS Sensor	

# LIST OF TABLES

# TABLE NO.TITLE

### PAGE

Table 2.1	Evolution of Optical Fibre	9
Table 2.2	Advantages and Disadvantages of Optical Fibres.	16
Table 2.3	Previous Studies Summary	25
Table 3.1	Parameters of SMS sensor	40
Table 4.1	Data from simulation result of SMS sensor with surrounding	
	RI=1.46	45
Table 4.2	Data from simulation result of SMS sensor with surrounding	
	RI=1.47	47
Table 4.3	Data from simulation result of SMS sensor with surrounding	
	RI=1.48	49
Table 4.4	Data from simulation result of SMS sensor with surrounding	
	RI=1.50	51
Table 4.5	Data from simulation result of SMS sensor with surrounding	
	RI=1.52	53
Table 4. 6	Data from simulation result of SMS sensor with surrounding	
	RI=1.55	55

# LIST OF FIGURES

### FIGURE NO.

### TITLE

### PAGE

Figure 2.1	Optical Fibre Components	8
Figure 2.2	Snell's Law inside single-mode optical fibres lead to total	
	internal reflection	10
Figure 2.3	Construction and light ray travels in a single mode fibre	11
Figure 2.4	Step-index MMF and Graded-index MMF	12
Figure 2.5	SMS Optical fibre sensor [9]	13
Figure 2.6	Multimode Interference on Optical Fibre SMS.	14
Figure 2.7	Self Imaging Phenomenon in Optical Fibre SMS[12].	15
Figure 2.8	Optical fibre Modes	16
Figure 2.9	FOS Configuration[14]	19
Figure 2.10	Basic block diagram for fiber optic sensor	19
Figure 2.11	Extrinsic Fibre Optic Sensor	20
Figure 2.12	Intrinsic Fibre Optic Sensor	21
Figure 2.13	Fibre Optic Sensor Applications	21
Figure 2.14	SMS Optical Fibre Sensor[16]	22
Figure 2.15	Ray-optical picture of modes propagating in an optical wave	guide 23
Figure 3.1	Project activities flowchart	31
Figure 3.2	SMS fibre instruction with high RI[5]	32
Figure 3.3	Startup window	39
Figure 3.4	The SMS sensor's cross-sectional area	40
Figure 3.5	Light pathway in SMS sensor	41
Figure 4.1	The intensity (dB) response at RI=1.46	46
Figure 4.2	The intensity (dB) response at RI=1.47	48
Figure 4.3	The intensity (dB) response at RI=1.48	50
Figure 4.4	The intensity (dB) response at RI=1.50	52
Figure 4.5	The intensity (dB) response at RI=1.52	54

Figure 4.6	The intensity (dB) response at RI=1.55	56
Figure 4.7	Light propagation and spectra response of the SMS fibre struct	ure to
	different surrounding RI	58
Figure 4.9	Variations of simulated output intensity with surrounding RI	59

# LIST OF ABBREVIATIONS

ANN	-	Artificial Neural Network
RI	-	Refractive Index
FBG	-	Fibre Bragg Grating
LPG	-	Long Period Grating
SMF	-	Single Mode Fibre
SMS	-	Single mode Multimode Single mode
MMF	-	Multi-Mode Fibre
GLG	-	Guided mode Leaky mode Guided mode
MMI	-	Multi-Mode Interference
FOS	-	Fibre Optic System
TIR	-	Total Internal Reflection
EMI	-	Electro Magnetic Interference
LMF	-	Leaky Mode Fibre
BPM	-	Beam Propagation Method

# LIST OF SYMBOLS

$n_1$	-	Refractive index for the core
$n_2$	-	Refractive index for the cladding
$W_m$	-	Wavelength of the multimode waveguide
$W_s$	-	Wavelength of the single mode waveguide
L	-	Length of the multimode waveguide
1	-	Orbital momentum of light
р	-	Number of radials mode oscillations
β	-	Propagation constant
n <sub>eff</sub>	-	Profile and effective index
c	-	Vacuum light speed
и	-	Normalize transverse phase
W	-	Attenuation constant
М	-	Number of guided modes
$w_0$	-	Spot size
$\beta_0$	-	Longitudinal propagation constant
а	-	Radius of SMF
E <sub>in</sub>	-	Input light in SMF
$E_m$	-	The field profile of the MMF's mth eigenmode
m	-	Number of guided modes in the MMF
C <sub>m</sub>	-	Excitation coefficient
v	-	Index suffix for the guided radial
μ	-	Index suffix for the azimuthal elements
$\beta_{v,\mu}$	-	Propagation constant for step index mmf of mth modes
$\beta_m$	-	The phase constant of mth excited leaky mode in the MMF
$\propto_m$	-	The attenuation constant of mth excited leaky mode in the MMF
T <sub>out</sub>	-	The normalize output intensity

# LIST OF APPENDICES

APPENDIX	TITLE	PAGE
Appendix A	SMF Optical Fibre Technical Sheet	68
Appendix B	MMF Optical Fibre Technical Sheet	69
Appendix C	BeamProp Simulation Procedure	70

#### **CHAPTER 1**

#### **INTRODUCTION**

#### 1.1 Project Background

Refractive index (RI) are required for some applications in the fields of biomedicine, biochemistry, processing manufacturing control, food industry quality control, and ecosystem safety, where exact estimations of the centralizations of various analytes are required [1]. A wide range of optical fibre-based sensing techniques have been proposed. Due to their susceptibility to electromagnetic interference, minimised size, conceivably minimal expense, and the capability of distributed measurement over long distances, optical fibre sensors can become tremendously powerful and flexible devices. RI sensing can be applied in various ways, for instance using a fibre Bragg grating (FBG)[2], a long-period grating (LPG), a macro-bend single-mode fibre (SMF), a surface plasmon resonance, a Fabry-Perot interferometer, a multi-D-shaped optical fibre, or a single mode-multimode-single mode (SMS) fibre structure. An optical sensor on an SMS fibre structure has the extra advantages of minimal expenses and simple assembling. External interruption may affect the multimode interference between modes in the multimode fibre (MMF). It is the basic operation of sensors in SMS fibre structures. So far, most RI sensor functions have focused on using the modal interference in the fully coordinated mode to estimate the surrounding IR below the multimode fibre core. If the surrounding RI is greater than the RI of the multimode fibre core instead of guided modes, the multimode fibre part will become a leaky waveguide that promotes progressive spectrum radiation modes. Instead of having multimode interference, the leaky structure conventionally defined that the light would leak out [3].

Although there is a leaky of light along the transverse direction, the light spreads with attenuate amplitude along the longitudinal direction. This system is called a guided-mode-leaky-mode-guided-mode (GLG) fibre structure with such a leaky mode expansion in the multimode fibre.

#### **1.2** The Motivation of the Study

Recently, a single mode-multimode-single mode (SMS) fibre optic sensor has been employed to measure changes in refractive index. With the expanding research attempts to find various additional detecting plans and strategies that could be gained from simple optical fibre structures, SMS fibre contributes to improving certain sensor applications with its simple design. This study demonstrated the improved performance sensitivity of the SMS fibre analytical design based on the multimode interference (MMI) through a theoretical study of leaky mode approximation for modal expansion in the optical fibre structure.

### **1.3** Problem Statement

Several methods have been used to achieve RI sensing, such as using sensing elements as a long-term grating (LPG) or Bragg grating with etched fibre, based on leaky mode expansion (FBG). These two approaches have their downsides that the fibre grating requires precise manufacturing procedures, high costs, and not so good sensitivity. On the other hand, the leakage modes, especially those used in long distances, do not fully leak through the optical fibres, and this increases the attenuation and thus, the lower sensitivity and the leakage loss in the fibre structure are greater.

Furthermore, in view of the MMI occurring within the SMS fibre structure, the traditional SMS working principle has been used to obtain sensing capabilities. However, due to the cladding of the multimode fibre (MMF), the structure of the SMS fibre limits the sensing sensitivity. The sensing principle of most fibre optic sensors (FOS) is achieved by interfering with changes in the refractive index within the

environment. However, the guided modes wrapped within the MMF render the fibre insensitivity to changes in the surrounding refractive index and result in negligible influence of the MMI.

For that reason, the refractive index sensor dependent on unique MMF without cladding is the alternative solution, which has various applications, including high refractive index sensing applications. In order to make the light waves propagating in the MMF completely internally reflected, the surrounding environment was used as a cladding layer. As a result, changes in the refractive index of the surrounding medium would have a direct impact on the MMI effect.

### 1.4 Project Goal

This project focused on developing a leaky mode expansion theoretical research model to enhance leaky mode structure analysis. Since the surrounding refractive indexes (RIs) are higher than the RIs of the silica fibre, the present researcher's concern was on the transmission criteria of the SMS structure. Moreover, as it studied optical waveguides, this project greatly verified the efficacy of analogous leaky mode expansion.

#### 1.5 **Project Objectives**

- a) To understand the underlying theories of leaky mode expansion.
- b) To apply leaky mode expansion for high surrounding refractive index sensing application.
- c) To analyse the effects of important parameters (length and diameter of MMF core, and changing value of surrounding refractive index) of leaky mode

expansion and fibre optic sensor structures on sensing performances using Beam Prop software.

### **1.6** Scope of Project

- (a) To drive theories of leaky mode expansion on guided-mode-leaky-modeguided-mode GLG fibre structure.
- (b) To use Beamprop software in simulating normalised output intensity of the SMS structure with several surrounding RIs around multimode fibre core.

### 1.7 Thesis Outline

This thesis is organised into five chapters, each of which covers and examines the literature study, the overall evolution of the project, and its implementation.

The first chapter of the project describes the project's introduction. This chapter offers an overview of the project history, issue description, goals, and scope of activity.

Chapter 2 discusses the project's literature review, which includes the various types of fibre optics and light propagation.

Chapter 3 looks at the flow of the method utilised throughout this project. The sensor design was created using RSoft Beamprop software.

The simulation results, as well as a discussion of the findings, are provided in Chapter 4. The sensitivity differences between the sensors are depicted using a graph.

Chapter 5 contains the conclusion and recommendations for further study.

#### REFERENCES

- J. Harris, P. Lu, H. Larocque, L. Chen, and X. Bao, "In-fiber Mach-Zehnder interferometric refractive index sensors with guided and leaky modes," *Sensors Actuators, B Chem.*, vol. 206, pp. 246–251, 2015, doi: 10.1016/j.snb.2014.09.062.
- Y. L. Yu, S. K. Liaw, H. H. Chou, H. Le-Minh, and Z. Ghassemlooy, "A Hybrid Optical Fiber and FSO System for Bidirectional Communications Used in Bridges," *IEEE Photonics J.*, vol. 7, no. 6, 2015, doi: 10.1109/JPHOT.2015.2488286.
- [3] S. F. S. M. Noor, S. W. Harun, H. Ahmad, and A. R. Muhammad, "Multimode interference based fiber-optic sensor for temperature measurement," *J. Phys. Conf. Ser.*, vol. 1151, no. 1, 2019, doi: 10.1088/1742-6596/1151/1/012023.
- [4] D. R. Anderson, L. Johnson, and F. G. Bell, "Fundamentals of fiber optics," *Troubl. Opt. Fiber Networks*, no. January, pp. 13–58, 2004, doi: 10.1016/b978-012058661-5/50022-7.
- [5] L. Yang, L. Xue, D. Che, and J. Qian, "Guided-mode-leaky-mode-guidedmode fiber structure and its application to high refractive index sensing," *Opt. Lett.*, vol. 37, no. 4, 2012, doi: 10.1364/ol.37.000587.
- [6] R. X. Gao, W. J. Liu, Y. Y. Wang, Q. Wang, F. Zhao, and S. L. Qu, "Design and fabrication of SMS fiber refractometer for liquid," *Sensors Actuators, A Phys.*, vol. 179, pp. 5–9, 2012, doi: 10.1016/j.sna.2012.02.020.
- [7] A. D. Gomes and O. Frazão, "Mach-Zehnder Based on Large Knot Fiber Resonator for Refractive Index Measurement," *IEEE Photonics Technol. Lett.*, vol. 28, no. 12, pp. 1279–1281, 2016, doi: 10.1109/LPT.2016.2538963.
- [8] P. Y. Aisyah, A. M. Hatta, and D. Y. Pratama, "Design of SMS (Single mode-Multi mode coreless-Single mode) optical fiber as corrosion sensor," *Second Int. Semin. Photonics, Opt. Its Appl. (ISPhOA 2016)*, vol. 10150, no. ISPhOA 2016, p. 101500Q, 2016, doi: 10.1117/12.2248493.
- [9] Q. Wang, G. Farrell, and W. Yan, "Investigation on single-mode-multimodesingle-mode fiber structure," *J. Light. Technol.*, vol. 26, no. 5, pp. 512–519, 2008, doi: 10.1109/JLT.2007.915205.

- K. Wang *et al.*, "Advances in Optical Fiber Sensors Based on Multimode Interference (MMI): A Review," *IEEE Sens. J.*, vol. 21, no. 1, pp. 132–142, 2021, doi: 10.1109/JSEN.2020.3015086.
- [11] R. W. Chuang, M. T. Hsu, Y. C. Chang, Y. J. Lee, and S. H. Chou, "Integrated multimode interference coupler-based Mach-Zehnder interferometric modulator fabricated on a silicon-on-insulator substrate," *IET Optoelectron.*, vol. 6, no. 3, pp. 147–152, 2012, doi: 10.1049/iet-opt.2010.0106.
- [12] W. Xu *et al.*, "Improved numerical calculation of the single-mode-no-coresingle-mode fiber structure using the fields far from cutoff approximation," *Sensors (Switzerland)*, vol. 17, no. 10, 2017, doi: 10.3390/s17102240.
- [13] L. Wang and N. Fang, "Applications of Fiber-Optic Interferometry Technology in Sensor Fields," *Opt. Interferom.*, 2017, doi: 10.5772/66276.
- [14] H. E. Joe, H. Yun, S. H. Jo, M. B. G. Jun, and B. K. Min, "A review on optical fiber sensors for environmental monitoring," *Int. J. Precis. Eng. Manuf. Green Technol.*, vol. 5, no. 1, pp. 173–191, 2018, doi: 10.1007/s40684-018-0017-6.
- P. Wang, G. Brambilla, M. Ding, Y. Semenova, Q. Wu, and G. Farrell,
  "Investigation of single-mode multimode single-mode fiber structures and their application for refractive index sensing," *America (NY)*., vol. 28, no. 5, pp. 1180–1186, 2011.
- [16] A. Kumar, R. K. Varshney, C. S. Antony, and P. Sharma, "Transmission characteristics of SMS fiber optic sensor structures," *Opt. Commun.*, vol. 219, no. 1–6, pp. 215–219, 2003, doi: 10.1016/S0030-4018(03)01289-6.
- [17] N. Marcuvitz, "On Field Representations in Terms of Leaky Modes or Eigenmodes," *IRE Trans. Antennas Propag.*, vol. 4, no. 3, pp. 192–194, 1956, doi: 10.1109/TAP.1956.1144410.
- [18] T. Tamir and A. A. Oliner, "Guided complex waves. Part 1: Fields at an interface," *Proc. Inst. Electr. Eng.*, vol. 110, no. 2, p. 310, 1963, doi: 10.1049/piee.1963.0044.
- [19] E. S. Cassedy and M. Cohn, "On the Existence of Leaky Waves Due to a Line Source Above a Grounded Dielectric Slab," *IRE Trans. Microw. Theory Tech.*, vol. 9, no. 3, pp. 243–247, 1961, doi: 10.1109/TMTT.1961.1125314.
- [20] D. B. Hall and C. Yeh, "Leaky waves in a heteroepitaxial film," J. Appl. Phys., vol. 44, no. 5, pp. 2271–2274, 1973, doi: 10.1063/1.1662549.

- [21] H. A. Haus and D. A. B. Miller, "Attenuation of Cutoff Modes and Leaky Modes of Dielectric Slab Structures," *IEEE J. Quantum Electron.*, vol. 22, no. 2, pp. 310–318, 1986, doi: 10.1109/JQE.1986.1072956.
- [22] Y. Suematsu and K. Furuya, "Quasi-Guided Modes and Related Radiation Losses in Optical Dielectric Waveguides with External Higher Index Surroundings," *IEEE Trans. Microw. Theory Tech.*, vol. 23, no. 1, pp. 170– 175, 1975, doi: 10.1109/TMTT.1975.1128518.
- [23] S. Kawakami and S. Nishida, "Perturbation Theory of a Doubly Clad Optical Fiber with a Low-Index Inner Cladding," *IEEE J. Quantum Electron.*, vol. 11, no. 4, pp. 130–138, 1975, doi: 10.1109/JQE.1975.1068578.
- [24] A. W. Snyder and D. J. Mitchell, "Ray Attenuation in Lossless Dielectric Structures.," *J Opt Soc Am*, vol. 64, no. 7, pp. 956–963, 1974, doi: 10.1364/JOSA.64.000956.
- [25] J. Petráček and K. Singh, "Determination of leaky modes in planar multilayer waveguides," *IEEE Photonics Technol. Lett.*, vol. 14, no. 6, pp. 810–812, 2002, doi: 10.1109/LPT.2002.1003101.
- [26] L. L. Xue, D. Che, and L. Yang, "High refractive index sensing based on single leaky mode attenuation," *Opt. Commun.*, vol. 294, pp. 198–201, 2013, doi: 10.1016/j.optcom.2012.12.082.
- [27] Y. Zhao, L. Cai, X. G. Li, F. C. Meng, and Z. Zhao, "Investigation of the high sensitivity RI sensor based on SMS fiber structure," *Sensors Actuators, A Phys.*, vol. 205, pp. 186–190, 2014, doi: 10.1016/j.sna.2013.10.023.
- [28] L.-L. Xue, H.-B. Liang, and L. Yang, "Single wavelength interrogated refractive index sensors based on leaky mode couplings," *Adv. Sens. Syst. Appl. IV*, vol. 7853, p. 78530F, 2010, doi: 10.1117/12.882340.
- [29] L. Xue, D. Che, and L. Yang, "Liquid level sensing based on leaky mode attenuation in a guided-mode-leaky-mode-guided-mode fiber structure," *Opt. Commun.*, vol. 325, pp. 160–164, 2014, doi: 10.1016/j.optcom.2014.04.001.