

STATE AND PARAMETER ESTIMATOR DESIGN
FOR CONTROL OF VEHICLE SUSPENSION SYSTEM

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STATE AND PARAMETER ESTIMATOR DESIGN
FOR CONTROL OF VEHICLE SUSPENSION SYSTEM

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To my family, especially my wife for the nice cuppas of latte and espressos every now and then. Forget bout putting you steady. You may marry someone else. Just a waste of space.

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ABSTRACT

Modern vehicle stability and navigational systems are mostly designed using inaccurate bicycle models to approximate the full-car models. This results in incomplete models with various unknown parameters and states being neglected in the controller and navigation system design processes. Earlier estimation algorithms using the bicycle models are simpler but have many undefined parameters and states that are crucial for proper stability control. For existing vehicle navigation systems, direct line of sight for satellite access is required but is limited in modern cities with many high-rise buildings and therefore, an inertial navigation system utilizing accurate estimation of these parameters is needed. The aim of this research is to estimate the parameters and states of the vehicle more accurately using a multivariable and complex full-car model. This will enhance the stability of the vehicle and can provide a more consistent navigation. The proposed method uses the kinematics estimation model formulated using special orthogonal SO_3 group to design estimators for vehicles velocity, attitude and suspension states. These estimators are used to modify the existing antilock braking system (ABS) scheme by incorporating the dynamic velocity estimation to reduce the stopping distance. Meanwhile the semi-active suspension system includes suspension velocity and displacement states to reduce the suspension displacements and velocities. They are also used in the direct yaw control (DYC) scheme to include mass and attitude changes to reduce the lateral velocity and slips. Meanwhile in the navigation system, the 3-dimensional attitude effects can improve the position accuracy. With these approaches, the stopping distance in the ABS has been reduced by one meter and the vehicle states required for inertial navigation are more accurately estimated. The results for high speed lane change test indicate that the vehicle is 34% more stable and 16% better ride comfort on rough terrains due to the proposed DYC and the active suspension system control. The methods proposed can be utilized in future autonomous car design. This research is therefore an important contribution in shaping the future of vehicle driving, comfort and stability.

ABSTRAK

Sistem keseimbangan dan navigasi pengemudian kenderaan moden kebanyakannya direka dengan menggunakan model dua tayar yang tidak tepat untuk menganggarkan model-model kereta-penuh. Ini akan menghasilkan model yang tidak lengkap dengan pelbagai parameter dan keadaan yang tidak diketahui diabaikan di dalam proses merekabentuk pengawal dan sistem navigasi. Algoritma awal penganggaran menggunakan model dua tayar adalah lebih ringkas tetapi mempunyai banyak parameter dan keadaan yang penting yang tidak ditakrifkan untuk kawalan kestabilan yang sepatutnya. Untuk sistem navigasi kenderaan yang sedia ada, garis penglihatan langsung untuk capaian satelit diperlukan tetapi ia terhad di dalam bandar yang mempunyai banyak bangunan tinggi. Oleh itu, sistem pengemudian inersia yang memberikan anggaran lebih tepat bagi parameter-parameter tersebut adalah diperlukan. Matlamat penyelidikan ini adalah untuk menganggarkan parameter-parameter dan keadaan kenderaan tersebut secara lebih tepat dengan menggunakan model berbilang pemboleh ubah dan kereta-penuh. Ini akan menambahkan kestabilan kenderaan dan memberikan pengemudian yang lebih konsisten. Kaedah yang dicadangkan menggunakan model penganggaran kinematik yang dirumuskan menggunakan kumpulan SO_3 ortogonal khas untuk penganggaran halaju, sikap dan keadaan ampaian kenderaan. Penganggar ini digunakan untuk mengubah skema sistem brek antikunci (ABS) dengan menggabungkan penganggar dinamik halaju untuk mengurangkan jarak berhenti. Sementara itu, sistem ampaian separa aktif dengan menyertakan halaju dan sesaran digunakan bagi mengurangkan sesaran dan halaju ampaian. Ia juga digunakan dalam skema pengawalan rewang terus (DYC) dengan menyertakan perubahan jisim dan sikap untuk mengurangkan halaju dan gelincir sisi. Dalam sistem navigasi pula, kesan sikap ini boleh meningkatkan kejituan posisi. Dengan pendekatan ini, jarak berhenti dalam ABS telah dikurangkan sebanyak 1 meter dan keadaan kenderaan diperlukan untuk navigasi inersia dianggarkan dengan lebih tepat. Keputusan bagi perubahan lorong ketika halaju tinggi ialah 34% lebih seimbang dan 16% lebih selesa di atas permukaan kasar hasil dari DYC dan pengawalan sistem ampaian aktif yang dicadangkan. Kaedah yang dicadangkan boleh digunakan dalam merekabentuk kenderaan autonomi pada masa hadapan. Penyelidikan ini adalah sumbangan penting dalam membentuk masa depan pemanduan, penyelesaian, dan keutuhan kestabilan.

TABLE OF CONTENTS

CHAPTER	TITLE	PAGE
	DECLARATION	ii
	DEDICATION	iii
	ACKNOWLEDGEMENT	iv
	ABSTRACT	v
	ABSTRAK	vi
	TABLE OF CONTENTS	vii
	LIST OF TABLES	viii
	LIST OF FIGURES	ix
	LIST OF ABBREVIATIONS	x
	LIST OF SYMBOLS	xii
	LIST OF APPENDICES	xxi
1	INTRODUCTION	1
	1.1 Background	1
	1.2 Problem Statement	3
	1.3 Objectives	3
	1.4 Scope of Work	4
	1.5 Dissertation Organization	4
2	THEORATICAL BACKGROUND OF VEHICLE SYSTEM	6
	2.1 Introduction	6
	2.2 Modeling of the Plant	7
	2.2.1 Overall Chassis Modeling	7
	2.2.1.1 The Bicycle Model	7
	2.2.1.2 Full Car Model	10
	2.2.2 Vehicle Suspension Modeling	14
	2.2.2.1 Macpherson Suspension	15
	2.2.2.2 Twisted Beam Suspension	16

	2.2.2.3	Quarter Car Suspension Model	17
	2.2.2.4	Full Car Suspension	18
	2.2.3	Tire Models	20
	2.2.3.1	Fiala Tire Model	21
	2.2.3.2	Dugoff Model	23
	2.2.3.3	Magic Formula Tire Model	25
	2.2.4	System Delay and Non-Linearity	28
	2.2.4.1	Hydraulic system delays and non-linearity	29
	2.2.4.2	Active and passive Steering System delays and non-linearity	30
	2.2.4.3	Transmission Non-linearity and Gear Shifting Problem	32
	2.2.4.4	Active and semiactive suspension	34
	2.2.4.5	Electronic System Delays and Noise	35
2.3		State and Parameter Estimation	38
	2.3.1	Kinematics-Based Estimation	38
	2.3.2	Model-Based Estimation	39
2.4		Controller Design	41
	2.4.1	Classical Controller (PI Controller)	42
	2.4.2	Optimal Controller	47
	2.4.3	Composite Controller	48
	2.4.4	Sliding Mode Controller	51
2.5		Car Navigation	53
	2.5.1	Inertial Navigational System (INS)	53
	2.5.2	GPS System	57
	2.5.3	GPS-INS Integration	61
	2.5.3.1	Loosely Coupled Mode of Integration	68
	2.5.3.2	Tightly Coupled Mode of Integration	69
	2.5.3.3	Ultra-tightly coupled mode of integration	70
	2.5.4	MARG Sensors	72
3		LITERATURE REVIEW	74
	3.1	Introduction	74

3.2	Modeling of the Plant	75
3.2.1	Chassis System	76
3.2.2	State Space Representation in State Dependent Continuous form (SDC)	76
3.2.3	Gap Analysis of the Car Model	82
3.3	State and Parameter Estimation	83
3.3.1	Kinematics-Based Estimation	84
3.3.2	Model-Based Estimation	85
3.3.3	Gap Analysis of State and Parameter Estimation	88
3.4	Controllers	89
3.4.1	Gap Analysis of Controllers for Vehicle Stability	90
3.5	Navigation	91
3.5.1	GPS-INS Integration	92
3.5.2	MARG Integartion	93
3.5.3	Gap Analysis for Navigation	93
3.6	Summary	93
4	METHODOLOGY	95
4.1	Introduction	95
4.2	Modeling Improvements	96
4.2.1	Linearized SDC Model Modifications to Include the Mass and Attitude changes	96
4.2.2	Model of Semi-Active Magnetorheologi- cal Damper (MR) for Suspension Systems	99
4.3	Design of Proposed Systems	101
4.3.1	Design of State and Parameter Estimators	101
4.3.1.1	Proposed SO_3 Attitude State Estimator	102
4.3.1.2	Proposed Velocity Estimator	105
4.3.1.3	Estimation of unknown suspen- sion states	107
4.3.2	Design of Controller for Longitudinal, Lateral and Vertical Stability	109
4.3.2.1	SDRE based controller in opti- mal direct yaw control (DYC)	110
4.3.2.2	ABS control using proposed Attitude and Velocity estimator	113

	4.3.2.3	Modified Skyhook + LQR Algorithm for Vertical Stability	116
	4.3.3	Design of Non-GPS Navigation System	119
4.4		Simulation setup	120
	4.4.1	Split- μ Test Setup	121
	4.4.2	High Speed Lane Change Test Setup	122
	4.4.3	Speed Bump Test Setup	123
	4.4.4	Cyclic Test Setup for State Estimation	124
	4.4.5	Noncyclic Test Setup	125
	4.4.6	Double Lane change (DLC) Test Setup	126
4.5		Hardware Implementation and System Design	127
	4.5.1	Experimental Vehicle Specification	127
	4.5.2	Sensor Arrangement and Installation	128
	4.5.3	Sensor Noise and Drift Mitigation	134
	4.5.4	Sensor Integration	134
4.6		Summary	136
5		RESULTS AND DISCUSSIONS	137
	5.1	Introduction	137
	5.2	Simulation Results	138
	5.2.1	Attitude Estimation During DLC Test	138
	5.2.2	Split- μ test for modified Antilock Braking System	141
	5.2.3	Modified Direct Yaw Control (DYC) System	145
	5.2.4	Semi-Active suspension system	150
	5.2.5	Estimation of Suspension States	152
	5.3	Experimental results	160
	5.3.1	Non-GPS Navigation results	160
	5.4	Summary	162
6		CONCLUSIONS FOR FUTURE WORKS	163
	6.1	Conclusions	163
	6.2	Future Recommendations	164
	6.3	List of Publications	165
		REFERENCES	167
		Appendix A	180

LIST OF TABLES

TABLE NO.	TITLE	PAGE
3.1	List of parameters and states estimated using Kinematic Kalman estimator by various researchers	85
3.2	List of parameters and states estimated using model based estimator by various researchers	86
4.1	List of various states of a Full Car Suspension	107
4.2	List of various dimensions of test car	127
4.3	List of various intrinsic parameters of ADXL103 accelerometer (Analog-Device, 2014) and L3G4200 gyroscope (ST-Microelectronics, 2010) used in the simulation	130
4.4	SKM53(L1 Band C/A Code 22 Tracking/66 Acquisition Channels) GPS specifications	132
4.5	Inertial sensor types and their specifications	135
5.1	Comparison of the estimated car attitude with reference systems.	139
5.2	Performance of various ABS systems during split- μ test	143
5.3	Performance of various ABS systems on high friction road ($\mu = 1$)	144
5.4	RMS Values during Split- μ test	149
5.5	RMS Values during Double Lane Change	150
5.6	Steady state time and maximum displacement of the chassis using various controllers	151
5.7	RMS error in position, velocity and heading in GPS, Proposed and INS with kalman system	161

LIST OF FIGURES

FIGURE NO.	TITLE	PAGE
2.1	Bicycle Model (Bevly and Cobb, 2010)	8
2.2	Force diagram of the model used in longitudinal dynamics (Bevly and Cobb, 2010; Oh and Choi, 2013)	9
2.3	Lateral view of the model (Bevly and Cobb, 2010)	12
2.4	Vehicle roll model (ISO8855 Coordinates) (Cho <i>et al.</i> , 2010a)	13
2.5	Simplified force diagram of the suspension system (Racing, 2015)	14
2.6	Detailed model of the front Macpherson suspension (Car-Engineer, 2013)	16
2.7	Detailed model of the twisted beam suspension (Invetr, 2008)	17
2.8	Quarter Car Model with states (Car-contacts, 2013)	18
2.9	Suspension system of Full Car Model	19
2.10	Lateral forces acting on the tire and tire slip angle (Bevly and Cobb, 2010)	21
2.11	Tire coefficient changes along the slip angle and horizontal direction	22
2.12	Longitudinal and lateral forces of tire under varying slip (Pacejka and Bakker, 1992)	24
2.13	Variation of longitudinal and lateral forces of tire under varying slip and weight (Pacejka and Bakker, 1992)	25
2.14	Variation of tire slip angle (κ) with horizontal force F_x , while vertical force F_z changes with the weight (Pacejka and Besselink, 1997)	26
2.15	Effects of various parameters on the output (Pacejka and Bakker, 1992)	27
2.16	Variation of tire slip angle α_i with lateral force F_y while vertical force F_z changes with the weight and coefficient of friction of tire road surface (Pacejka and Besselink, 1997)	28
2.17	A basic car brake system (Shadow, 2013)	29
2.18	A basic brake-by-wire car brake system (Sportrider, 2012)	30

2.19	A typical steer-by-wire car steering system (Corporation, 2016).	32
2.20	A typical automatic transmission system (Bevly <i>et al.</i> , 2000)	33
2.21	Block diagram of a typical MR damper	35
2.22	A typical CAN bus interface	36
2.23	A typical I2C Interface	37
2.24	Closed loop yaw rate block diagram (Bevly and Cobb, 2010)	42
2.25	Active front wheel steering with feed forward control (Manning and Crolla, 2007)	45
2.26	Active front wheel steering with feed forward and feedback (Manning and Crolla, 2007)	45
2.27	Active front wheel steering with yaw rate control and braking based stability control system (Manning and Crolla, 2007)	46
2.28	Active front wheel steering control with feed-forward and feed back yaw rate control (Manning and Crolla, 2007)	46
2.29	Block diagram of a typical Optimal controller	48
2.30	Block diagram of general Composite controller	48
2.31	Model of a basic mechanical gyro (Farrell, 2008)	55
2.32	Structure of a basic accelerometer (Wiak <i>et al.</i> , 2005)	56
2.33	Conventional block diagram of base-band Processing (Kim <i>et al.</i> , 2003)	60
2.34	Location of point $p(x,y,h)$ in earth reference frame	61
2.35	Different configurations of IMU sensors (Aggarwal <i>et al.</i> , 2014)	63
2.36	Drift in the output parameters in various configurations (Aggarwal <i>et al.</i> , 2014)	65
2.37	Block diagram of GPS-INS sensor fusion (Jwo <i>et al.</i> , 2012)	67
2.38	Block diagram of a loosely coupled GPS-INS system (Farrell, 2012)	69
2.39	Block diagram of tightly coupled GPS-INS system (Jwo <i>et al.</i> , 2012)	70
2.40	Ultra-tightly coupled GPS/INS integration with doppler velocity aiding. (Kim <i>et al.</i> , 2003)	71
2.41	Uncompensated and compensated plot of the magnetic flux for hard iron and soft iron effects (Ozyagcilar, 2012)	73
3.1	Block Diagram of a Complete Car Model	75
3.2	List of various estimators used for the estimation of various car states and parameters	83

3.3	List of Kinematic estimators by various researchers (Crassidis and Junkins, 2011)	84
3.4	List of parameters and states estimated using model based estimator by various researchers	86
3.5	List of various controllers used in literature	90
3.6	List of various navigational system currently in use	92
4.1	Various parameters used by the estimator (Racing, 2015)	103
4.2	Block diagram of the proposed car velocity estimator	106
4.3	Comparison between measured and actual velocity of vehicle in Km/h	113
4.4	Block diagram of the proposed ABS systems	115
4.5	Quarter car semiactive suspension model (Yi and Suk Song, 1999)	117
4.6	Block diagram of the procedure used in the estimation of vehicle heading (ψ)	120
4.7	Friction coefficient applied to the left side wheels of the vehicle	122
4.8	Steering input to the system during high speed lane change test	123
4.9	Disturbance input to the suspension	124
4.10	Disturbance input to suspension to mimic a cyclic test	125
4.11	Disturbance input to suspension to mimic a noisy road speed bump	126
4.12	Dimension of the proposed car (Benev <i>et al.</i> , 2013)	127
4.13	Model of L3G4200 triaxial gyroscope (ST-Microelectronics, 2010)	128
4.14	Model of ADXL345 triaxial accelerometer (Analog-Device, 2014)	129
4.15	Model of an-isotropic magnetoresistive sensor (Abdeen <i>et al.</i> , 2016)	131
4.16	Internal diagram of HMC5883L and interfacing with uC (Abdeen <i>et al.</i> , 2016; Benev <i>et al.</i> , 2013)	131
4.17	Proposed GPS sensor module from Skylab used in the experimental work (Nasr <i>et al.</i> , 2016)	132
4.18	Wheel speed sensor attached to the front right wheel of test car	133
4.19	Wheel speed sensor interfacing circuit	133
5.1	Simulation results for attitude estimates using the SO_3 estimator	138

5.2	Comparison of estimated roll (θ), pitch (ϕ) and yaw (ψ) of the vehicle.	140
5.3	Actual Velocity, wheel speed based velocity and estimated velocity of the vehicle (Km/h)	141
5.4	Change in pitch angle (ϕ) during heavy braking during split- μ test	142
5.5	Output pressures for each wheel operation during split- μ test	142
5.6	Braking times of various ABS system using conventional reference wheel velocity, proposed estimator based vehicle velocity and actual velocity	143
5.7	Braking times of various ABS system using conventional reference wheel velocity, proposed estimator based vehicle velocity and actual velocity	144
5.8	Change in the longitudinal velocity V_x and lateral velocity V_y during lane change test	145
5.9	Change in the yaw rate ($\dot{\omega}_z$) with steering input (δ) during lane change test	146
5.10	F_z changes during lane change test	147
5.11	Chassis roll (θ) change during lane change test	148
5.12	Slip across the front left wheel during lane change test.	149
5.13	Response of chassis to external disturbances	152
5.14	Actual and estimated displacement in front left damper	153
5.15	Measured and estimated pitch of the chassis	154
5.16	Measured and estimated roll of the chassis during motion	155
5.17	Actual and estimated displacement of the chassis	156
5.18	Actual and estimated displacement in front left damper	157
5.19	Measured and estimated pitch of the chassis	158
5.20	Measured and estimated roll of the chassis during motion	159
5.21	Actual and estimated displacement of the chassis during motion	159
5.22	Vehicle position plot using the proposed SO_3 estimator, Kalman estimator and GPS.	160

LIST OF ABBREVIATIONS

<i>BM</i>	–	Bicycle Model
<i>CG</i>	–	Center of gravity
<i>diag</i>	–	Diagonal matrix, a matrix with all non parameters defined in the diagonal column only
<i>DMHE</i>	–	Direct Moving Horizon Estimator
<i>EKF</i>	–	Extended Kalman Filter
<i>EKBF</i>	–	Extended Kalman Bucy Filter
<i>EPF</i>	–	Extended Particle Filter
<i>FCM</i>	–	Full Car Model
<i>FL</i>	–	Fuzzy Logic
<i>GPS</i>	–	Global Positioning System
<i>GINS</i>	–	Global Inertial Navigational System
<i>GLONASS</i>	–	Global Navigation and Observatory System
<i>INS</i>	–	Inertial Navigation System
<i>IMU</i>	–	Inertial Measurement Unit
<i>KF</i>	–	Kalman Filter
<i>KM</i>	–	Kinematics Model
<i>KBF</i>	–	Kalman Bucy Filter
<i>LMS</i>	–	Least Mean Square
<i>MR</i>	–	Magnetorheological
<i>MH</i>	–	Moving Horizon Estimator
<i>MMS</i>	–	Multiple model and switching method
<i>NLO</i>	–	Nonlinear Observer
<i>PF</i>	–	Particle Filter

<i>RLS</i>	–	Recursive Least Square
<i>RLSF</i>	–	Recursive Least Square with Forgetting Factor
<i>RTLSF</i>	–	Recursive Time varying Least Square with Forgetting Factor
<i>SDC</i>	–	State Dependent Coefficient Form
<i>SDRE</i>	–	State Dependent Ricatti Equation
<i>LQR</i>	–	Linear Quadratic Recursion

LIST OF SYMBOLS

Vehicle Physical Parameters

A_p	–	Wind Drag Coefficient
e	–	Lateral Width of the vehicle [m]
f	–	Frequency of the source
h	–	Distance of C.G from roll axis [m]
h_{cg}	–	Height of center of gravity from level ground [m]
I	–	Moment of Inertia along x,y,z axis[Kgm ²][I_x, I_y, I_z].
l_a	–	Distance of C.G from front axle [m]
l_b	–	Distance of C.G from rear axle [m]
l	–	Wheel Base(a + b) [m]
M	–	Vehicle Mass [Kg]
M_1	–	Roll Compensated Vehicle Mass [Kg]
m	–	Lower suspension mass [Kg]
\mathbb{M}	–	Vector of masses [M, m_1, m_2, m_3, m_4]
r_{11}	–	Longitudinal distance from front left damper to wheel joint [m]
r_{12}	–	Lateral distance from front left damper to wheel joint [m]
r_{21}	–	Longitudinal distance from front right damper to wheel joint [m]
r_{22}	–	Lateral distance from front right damper to wheel joint [m]
r_{31}	–	Longitudinal distance from rear left damper to wheel joint [m]
r_{32}	–	Lateral distance from rear left damper to wheel joint [m]
r_{41}	–	Longitudinal distance from rear right damper to wheel joint [m]
r_{42}	–	Lateral distance from rear right damper to wheel joint [m]

R_e	–	Radius of the Earth [m]
R_c	–	Radius of Curvature during turning [m]
t_f	–	Distance between front tires [m]
t_r	–	Distance between rear tires [m]
θ_{bank}	–	Banking angle of road surface
μ	–	Nominal friction coefficient of the road surface

Sensor Parameters

A_{NL}	–	Accelerometer Nonlinearity
aab	–	Accelerometer beam coefficients[aa_1, ab_1]
a_{bcx}	–	x-axis accelerometer constant potential for running
a_{brx}	–	x-axis accelerometer random potential for running
ae_1	–	Accelerometer demodulator filter effects
ah_1	–	Output filter Coefficient $1/(6.28 \times 50)$
aFS	–	Accelerometer Range Selectable (2g/4g/8g/16g)
A_m	–	Accelerations measurement Vector[A_x, A_y, A_z]
A_{maxGPS}	–	operational Limits (Acceleration) [g]
A_R	–	Satellite Received Signal Amplitude
b_{ai}	–	Accelerometer bias[b_{ax}, b_{ay}, b_{az}]
b_{ari}	–	Random bias of accelerometer[$b_{arx}, b_{ary}, b_{arz}$]
b_{aci}	–	Constant Accelerometer bias[$b_{acx}, b_{acy}, b_{acz}$]
b_{gci}	–	Constant Gyro bias[$b_{gcx}, b_{gcy}, b_{gcz}$]
b_{gci}	–	Constant Gyro bias[$b_{gcx}, b_{gcy}, b_{gcz}$]
b_{grr_i}	–	Random x-axis run-to-run gyro bias[$b_{grrx}, b_{grry}, b_{grrz}$]
a_{gebx}	–	x-axis gyro constant potential for running
a_{grbx}	–	x-axis gyro random potential for running
δt^i	–	Residual satellite clock error after performing the corrections
δ_g	–	Anomalous gravity
$\epsilon(\omega)$	–	gyro error noise
$\epsilon(a)$	–	Accelerometer error noise

$e_g(t)$	–	Error in Gyroscope
f_1	–	L1 Band frequency
f_2	–	L2 Band frequency
F_{slant}	–	VCO clock slant correction factor
g_{bin}	–	Biassing when the gyroscope is running
gT_{comp}	–	Gyro Temperature Compensation
G_s	–	gyro scale factor
gDV_{off}	–	Gyro Digital Zero Rate Level [dps]
g_{NL}	–	gyro Non-Linearity [% FS]
g_{ODR}	–	Gyro rate level change vs Temp [dps/C]
gR_n	–	Gyro rate Noise Density [dps / \sqrt{Hz}]
g_{FS}	–	Gyro Range [dps]
GPS_{AC}	–	GPS Accuracy
h_{maxGPS}	–	operational Limits (Altitude) [m]
I_r^i	–	Error due to dispersion atmospheric effects
I_r	–	Mobile signal recieved signal struength
k_{a1}	–	Accelerometer amplifier Gain [V/V]
m_{FS}	–	Magnetometer Range [Gauss]
m_{DFS}	–	magnetometer dynamic range [Gauss]
$M_{\rho_i}^i$	–	Pseudo-range multiple path errors on the L_i pseudo-range measurements [$M_{\rho_1}^i, M_{\rho_2}^i$]
M_g	–	Magnetometer Sensitivity [LSB/Gauss]
M_N	–	Magnetomter Noise Floor [milli-Gauss]
M_{res}	–	Magnetometer Resolution in [milli-Gauss/bit]
N_p	–	Pressure Sensor RMS Noise [m]
N	–	Non-Orthogonalities
\aleph	–	Sensor and Process random white gaussian noise [\aleph, ϕ]
ω_{gbias}	–	Process noise driving the gyroscope bias [rad/s] [$\omega_{xbias}, \omega_{ybias}, \omega_{zbias}$]
ω_{abias}	–	Process noise driving the accelerometer bias [m/s ²]

Ω	–	Gyro measurements Vector [$\Omega_x, \Omega_y, \Omega_z$][radians/s]
ψ_{GPS}	–	GPS Heading [radians]
θ_{GPS}	–	GPS Roll [radians]
ψ_m	–	Magnetometer yaw [radians]
ψ_{INS}	–	INS yaw [radians]
ψ_{MARG}	–	MARG yaw [radians]
KF	–	Magnetometer confidence factor
p_{GPS}	–	Position measured using GPS
V_{GPS}	–	Velocity measured using GPS [$V_{GPS}^{east}, V_{GPS}^{north}, V_{GPS}^{up}$]
P_{AC}	–	Pressure Sensor Absolute Accuracy Pressure [hPa]
p_{FS}	–	Pressure Sensor Resolution [hPa]
PT_{res}	–	Pressure Sensor Temp Resolution [$^{\circ}C$]
Q_{bias}	–	Sensor bias covariance
ρ	–	Pseudorange at position p(x)
σ_{gps}	–	Standard deviation of GPS noise [radians/Hz]
σ_{accel}	–	Standard deviation of accelerometer noise [radians/Hz]
σ_{gyro}	–	Standard deviation of gyro noise [radians/Hz]
σ_N	–	Random white Gaussian sensor noise density [W/\sqrt{Hz}]
σ_{Na}	–	Random white Gaussian Accelerometer noise density [W/\sqrt{Hz}]
σ_{Ng}	–	Random white Gaussian Gyroscope noise density [W/\sqrt{Hz}]
σ_R	–	Random white Gaussian Process noise density [W/\sqrt{Hz}]
S_{gps}	–	GPS sensitivity [dBm]
S_a	–	Accelerometer Sensitivity [LSB/g]
S_g	–	Gyro sensitivity [mdps/digit]
S_2	–	Accelerometer frequency sensitivity factor
S_{gODR}	–	Sensitivity deration per degrees [mg/deg]
T_r^i	–	Error due to non-dispersion atmospheric effects
τ_{bias}	–	Markov Time Constant
T_{gps}	–	Sampling Rate of GPS [s]

T_s	–	Sampling Rate of Inertial sensors [s]
T_R	–	Received signal period [s]
v_{gyro}	–	Gyro sensor noise
v_{accel}	–	Accelerometer sensor noise
v_{gps}	–	GPS sensor noise
$v_{\rho_i}^i$	–	random measurement noise on the L_i pseudo-range measurements [$v_{\rho 1}^i, v_{\rho 2}^i$]
V_{maxGPS}	–	operational Limits (Velocity) [m/s]
$V_{\psi_{gps}}$	–	standard deviation of GPS heading noise [radians]
$V_{\theta_{gps}}$	–	standard deviation of GPS grade noise [radians]

Tire Parameters

α_i	–	Lateral tire slip angle [radians] [α_f, α_r]
κ	–	Tire slip ratio
C_α	–	Tire Coefficient along tire slip angle
C_σ	–	Tire Coefficient along tire density
C_i	–	Tire Coefficient along longitudinal and lateral axis [C_x, C_y]
C_α	–	Front and Rear Tire Cornering Stiffness [Nm] [$C_{\alpha f}, C_{\alpha r}$]
E	–	Tire Curvature Factor
γ	–	slip switching function
ϱ	–	Lateral Tire Slip Function
K_t	–	Tire Spring Constant [N/m]
λ	–	Slip in tire
M_z	–	Tire Braking Force [N]
S_i	–	Tire Horizontal and Vertical Shift [S_H, S_v]
T_b	–	Braking torque [N/m]
T_d	–	Traction Torque [N/m]
ς	–	Tire Peak Value
Υ	–	Tire Stiffness Factor
ϖ	–	Tire Shape Factor

Wheel Parameters

I_w	–	Wheel moment of inertia [Kgm/s ²]
J	–	Tire Horizontal Slip Function
ω_w	–	Wheel Angular velocity of wheel [rad/s]
R_w	–	Radius of Wheel [m]
V_w	–	Wheel Linear Velocity [m/s]

Vehicle Dynamic Parameters

α	–	Kinematic model based observer design parameter
A_c	–	Actual linear accelerations vector [a_x, a_y, a_z] [m/s ²]
\mathbb{A}	–	Attitude Vector [θ, ϕ, ψ][Radians]
β	–	Sideslip angle [radians]
δ	–	Steering angle [rad]
δ_c	–	Steering input from controller for assistance [rad]
δ_{max}	–	Maximum steering angle [rad]
F_x	–	Longitudinal Force Component [N]
F_y	–	Lateral Force Component [N]
F_z	–	Vertical Force Component [N]
F_ϕ	–	Force causing vehicle roll [N]
\tilde{h}	–	Odd submatrix of Rotation Matrix
\mathbb{J}	–	Cost Function
K_p	–	Proportional Gain
ω_c	–	Actual Angular velocity vector [$\omega_x, \omega_y, \omega_z$][Radians/s]
p	–	position of the vehicle[x,y,z][m]
θ	–	Roll angle [radians]
ϕ	–	Pitch Angle [radians]
ψ	–	Yaw angle [radians]
τ	–	Coefficient of rotation matrix
\mathbb{R}	–	Rotation Matrix using direction cosines
S	–	Sliding Surface

τ_δ	–	Steer system time constant [s]
τ_c	–	Actuator time constant [s]
τ_{CAN}	–	Steer system time constant [s]
τ_{I2C}	–	Steer system time constant [s]
V	–	Velocity of the vehicle [m/s][V_x, V_y, V_z]
\mathbb{W}	–	Lyapunov Energy Function

Suspension Physical Parameters

b_ϕ	–	Damping Coefficient of damper along roll axis [Ns/m][$b_{\phi f}, b_{\phi r}$]
B	–	Vector of Damping Coefficient of the MR Dampers [$b_{0FL}, b_{0FR}, b_{0RL}, b_{0RR}$][Ns/rad]
k_ϕ	–	Spring Constant along roll axis [N/m][$k_{\phi f}, k_{\phi r}$]
K	–	Vector of spring constants [k_1, k_2, k_3, k_4]
\mathfrak{R}_i	–	Damper Coefficients matrix[$\mathfrak{R}_1, \mathfrak{R}_2, \mathfrak{R}_3$]

MR Damper

$m\alpha_i$	–	Fixed and variable MR fluid factor
A_m	–	MR damper piston surface area [m^2]
β_m	–	MR fluid factor
bm_0	–	Fixed and variable Bingham damping coefficients [Ns/m][b_0a, b_0b]
bm_1	–	Fixed and variable Hysteresis damping coefficients [Ns/m][b_1a, b_1b]
η_m	–	Response time of the MR fluid
γ_m	–	MR fluid factor

System Matrices

A	–	State Matrix
A_N	–	Nominal State Matrix
B	–	Input State Matrix[B_1, B_2]

B_N	–	Nominal Input State Matrix
$B(x, t)$	–	Nonlinear input state dependent function
C	–	Output State Matrix
C_N	–	Nominal Output State Matrix
CCR	–	Submatrix of the state matrix
χ	–	Linear and nonlinear composite controller control effort [χ_N, χ_L]
D	–	Feedforward State Matrix
D_N	–	Nominal Feedforward State Matrix
<i>EngineType</i>	–	DOHC DVVT [K3VE]
$f(x, t)$	–	Nonlinear system state dependent function
F	–	Linear substate state matrix in composite control scheme
G	–	Linear substate input matrix in composite control scheme
Γ	–	Bias Augmented state matrix
I	–	Identity Matrix
K_∞	–	Measurement error gain Covariance Matrix
\mathfrak{K}	–	Estimator Gain matrix
KK	–	Submatrix of the state matrix
Ω_\times	–	Special orthogonal rate matrix
O	–	Zero Matrix
Ψ	–	Observability Matrix
Π	–	Bias Augmented input matrix
Φ	–	Bias Augmented feedforward matrix
P	–	Covariance Matrix
P_∞	–	Steady state kalman error Covariance Matrix
Q	–	Process Noise Covariance Matrix [Q_i, Q_j]
R	–	Sensor Noise Covariance Matrix
Θ	–	Bias Augmented output matrix
Ξ	–	Controllability Matrix
$u(t)$	–	Input vector [u_1, u_2]

\mathbb{U}	–	Second moment of distance submatrix
\mathbb{V}	–	First moment of distance submatrix
ξ	–	Subfunction in sliding mode controller
$x(t)$	–	State vector
$y(t)$	–	Output vector
y_m	–	System output measurements vector

LIST OF APPENDICES

APPENDIX	TITLE	PAGE
A	Quaternion Representation and Operators	180

CHAPTER 1

INTRODUCTION

1.1 Background

Since the early 19th century, the cars has passed through a number of improvements (Bevly and Cobb, 2010; Leung *et al.*, 2011; Oh and Choi, 2013; Farrell, 2008). During the early days, clutch system and variable speed gear system was introduced to improve the vehicle handling (Lee *et al.*, 2014; davidL, 2000). Similarly flexible suspension system using spring mass damper system and air filled tires were introduced to improve the ride comfort and long term reliability (Lin and Kanellakopoulos, 1997). These innovations were introduced using bulky mechanical system and conceived on paper using expert knowledge; as there were no means of doing simulations (Stensson *et al.*, 1994; Fallah *et al.*, 2009). Earlier introduction of electromechanical systems in the form of motors for engine starting, encouraged the car engineers to replace the bulky mechanical assemblies with electromechanical systems to reduce weight and improve system performance (Bevly and Cobb, 2010; Farrell, 2008). Most of the earlier electromechanical systems used simple drive-by-wire technology for control. The improvements in digital control theory and microprocessors lead to the use of computer for driver assistance in collision avoiding system, like antilock braking system (ABS), and driver assisting systems, like assisted direct yaw control (DYC) (Jagtman and Wiersma, 2003; Abdulrahim, 2006; Aripin *et al.*, 2014; Suzuki and Takeda, 2016). When designing driver assisted control systems, the focus was mainly on improving the specific component of the car. For example, the automatic transmission system design process was focused on how to change the drive train by including electromechanical valves coupled with a large array of speed sensors and a digital controller for gear shift (Ackermann and Buente, 1997; Lee *et al.*, 2014). It did not include the engine block in the design process to optimize speed and torque. Similarly, the antilock braking system (Khachane and Shrivastav, 2016; Rizzi *et al.*, 2016; Boopathi and Abudhahir, 2016) included the speed obtained from the wheels speed sensors (Madau *et al.*, 1993; Mauer, 1995; Suraci *et al.*, 2006)

and did not include the linear accelerations (Bowman and Law, 1993) and angular velocities acting on the vehicle when developing the controller (Peric *et al.*, 2016; Antic *et al.*, 2016; Tang *et al.*, 2016).

The use of electromechanical systems for steering control and navigational system for autonomous driving, is another application which is being developed and refined (Inoue *et al.*, 2016; Zhao *et al.*, 2017). The use of electromechanical systems for direct steering, by using drive-by-wire technology has resulted in the reduction of weight, by reducing heavy mechanical linkages used in the ackermann shaft. It has also resulted in the improvement of the system response time, since direct control with lightning response and very low torque requirements are needed. High torque requirements for turning are common in bigger car, trucks and buses. Excessively high torque requirements had forced the car engineers to design power steering systems. With drive-by-wire technology, power steering systems become irrelevant. The drive-by-wire technology, reduces engine load required by power steering, reduces the weight and converts torque requirements into systems response inputs. The drive-by-wire technology also helps in placing digital controllers to assist the driver by changing the steering input habits of the driver for better control and reduce accident chances (Zhao *et al.*, 2017).

Recently, the drive-by-wire steering system, the automatic cruise control system and the braking system has been integrated with a reliable navigational system to provide the driver with a fully autonomous or partially autonomous system. The aim of this system has been in replacing or comforting the driver by employing various sensors and controllers. These systems have shown promising results under various test conditions. Since these systems have not gone through strenuous testing, they are considered less reliable and their accuracy is also limited. The reliability of these systems has created a sense of uncertainty in the car industry. The industry is also looking for systems which are simpler, since simpler systems are more reliable, have better accuracy and good component and system reliability. A good component reliability can result in higher component service life, which results in lesser maintenance (Dhahri *et al.*, 2012).

When considering the reliability of such systems, the reliability of each component is important. Hence each component is being tested and refined to improve its reliability. The amount of energy consumed is one important factors for judging the reliability of a component, subsystem or system. Some safety and comfort related systems have thus been graded as unreliable or uneconomical. One such system is the

active suspension system, which consumes a lot of power and its components have a very limited operational life. They are thus replaced by sub-optimal semi-active suspension systems, which are much more reliable and consume less energy (Chen *et al.*, 2015). Similarly, in semi-autonomous systems, the global positioning system, because of its direct line of sight requirements and limited 3D accuracy, is considered less reliable. There is a need to have navigational systems which can provide reliable accuracy (Wu *et al.*, 2016; Lin *et al.*, 2016; Sarbishei, 2016).

1.2 Problem Statement

The research work aims to address the following problems:

- i. Most of the current vehicle stability control systems incorporate essential and measurable parameters and states. Essential but non-measurable parameters are either estimated using complex estimation schemes, or are neglected (Sandu *et al.*, 2010; Crivellaro and Alves, 2006; Qazi *et al.*, 2014). The resultant control scheme is therefore, not robust enough or has high computational cost. Earlier control systems did not use expensive sensors or fast processing computers due to their higher cost (Cherouat *et al.*, 2005; Hac and Simpson, 2000). Current technologies has made the cost of sensors to reduce considerably and high end processors are also becoming cheaper. Therefore parameters and states which were neglected must be included to have more robustness and reliability (Chen *et al.*, 2015; Qazi *et al.*, 2014).
- ii. Current navigational systems use direct line of sight satellite communications, which are easily obstructed by underground bridges, sky scrapers and overhead bridges (Cohen *et al.*, 1994; Jwo *et al.*, 2012; Farina *et al.*, 2002). The system has to do a lot of computations to provide accurate 3D positional and velocity accuracy, which makes the system unsuitable for real time navigation (Wu *et al.*, 2016). The inertial navigation system can provide data in real time but does not have high accuracy. It does not require direct line of sight. A fusion of GPS with INS, as used in existing systems, cannot overcome the direct line of sight problem with GPS, without sacrificing the system accuracy. By fusing the inertial navigation system with other sensors to achieve redundancy and by using better algorithms, the INS accuracy can be improved without any direct line of sight problems (Sarbishei, 2016).

- iii. Newer and better control schemes must be provided to improve the stability and control of the vehicle to overcome general problems with existing control schemes.

1.3 Objectives

The objectives of this research are listed as follows:

- i. To estimate the important states and parameters of vehicles for better control of the vehicle.
- ii. To design a simple and robust controller that can improve the longitudinal, lateral and vertical stability of the vehicle.
- iii. To develop a navigational system that has no dependency on GPS.

1.4 Scope of Work

The scope of work in this research are

- i. The systems were tested using hatchback car model, since it has the ability to loose traction during turning. The real time systems were tested on test car since its structure is hatch back with good weight to torque settings for a utility car.
- ii. The important data for states and parameters were obtained using CarsimTM (a nonlinear vehicle simulator) and used for comparison in real time estimation, since those states and parameters were not possible to physically measure them.
- iii. The proposed controllers were only simulated with tests in CarsimTM.
- iv. The proposed navigational algorithm was tested on practical environment and the attitude states were compared with simulated results obtained from CarsimTM since they were not possible to measure in practical environment.

1.5 Dissertation Organization

The research is divided into several chapters. Following is the list of chapters with a brief detail of each chapters.

- i. Chapter 1: This chapter gives a brief introduction of the work. It consists of the problem statement, the objectives of this research, the scope of the work and important contributions of this work.
- ii. Chapter 2: This chapter describes the theory of existing systems. This chapter clearly defines the important parameters, models and states used to build the foundation of this research.
- iii. Chapter 3: This chapter briefly describes the literature review of existing systems. It revisits certain models to introduce important missing parameters. It also revisits the existing observers and controllers to suggest improvements and new control and estimation algorithms.
- iv. Chapter 4: The proposed changes are discussed with elaborate mathematical justification in this chapter. The method used for testing the proposed changes and its implementation are also discussed. The chapter thus includes the methodology of the proposed works. The proposed changes and the method used to test the changes and evaluate them in comparison to the existing methods is also done in this chapter.
- v. Chapter 5: The chapter presents all the test results and provides a comprehensive analysis of each test result, that are compared with existing results. The chapter thus provides the results and analysis of the research.
- vi. Chapter 6: This chapter concludes the work done in this research. It gives all the conclusions drawn from the research. Based on the conclusions, it also suggests recommendations for further research.

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