A NEW BINARY PARTICLE SWARM OPTIMIZER TO SELECT A SMALLER SUBSET OF GENES FOR LEUKAEMIA CANCER CLASSIFICATION

Mohd Saberi Mohamad^{1,2}, Sigeru Omatu¹, Safaai Deris² and Michifuci Yoshioka¹, Anazida Zainal²

> ¹Department of Computer Science and Intelligent Systems, Graduate School of Engineering, Osaka Prefecture University, Sakai, Osaka 599-8531, Japan

> ²Department of Software Engineering, Faculty of Computer Science and Information System, Universiti Teknologi Malaysia, 81310 Skudai, Johor, Malaysia

Email: mohd.saberi@sig.cs.osakafu-u.ac.jp, {sigeru,yoshioka}@.cs.osakafu-u.ac.jp, safaai@utm.my

Abstract: The application of microarray data for cancer classification has recently gained in popularity. The main problem that needs to be addressed is the selection of a smaller subset of genes from the thousands of genes in the data that contributes to a disease. This selection process is difficult because of the availability of the small number of samples compared to the huge number of genes, many irrelevant genes, and noisy genes. Therefore, this paper proposes an improved binary particle swarm optimization to select a near-optimal (smaller) subset of informative genes that is relevant for cancer classification. Experimental results show that the performance of the proposed method is superior to the experimental method and other related previous works in terms of classification accuracy and the number of selected genes.

Keywords: Gene Selection, Hybrid Approach, Microarray Data, Particle Swarm Optimization.

1. INTRODUCTION

Microarray is a device that can be employed in measuring of expression levels of thousands of genes simultaneously. It finally produces microarray data that contain useful information of genomic, diagnostic, and prognostic for researchers [5]. Thus, there is a need to select informative genes that contribute to a cancerous state [7]. However, the gene selection process poses a major challenge because of the following characteristics of microarray data: the huge number of genes compared to the small number of samples (higher-dimensional data), irrelevant genes, and noisy data. To overcome this challenge, a gene selection method is used to select a subset of genes that increases the classifier's ability to classify samples more accurately [6].

Recently, several methods based on particle swarm optimization (PSO) are proposed to select informative genes from microarray data [1],[2],[8]. PSO is a new evolutionary technique proposed by Kennedy and Eberhart [3]. It is motivated from the simulation of social behaviour of organisms such as bird flocking and fish schooling. Shen et al. have proposed a hybrid of PSO and tabu search approaches for gene selection [8]. However, the results obtained by using the hybrid method are less significant because the application of tabu approaches in PSO is unable to search a near-optimal solution in search spaces. Next, an improved binary PSO have been proposed by Chuang et al. [1]. This approach produced 100% classification accuracy in many data sets, but it used a higher number of selected genes to achieve the higher accuracy. It uses the higher number because of all global best particles are reset to the same position when their fitness values do not change after three consecutive iterations. Li et al. have introduced a hybrid of PSO and GA for the same purpose [2]. Unfortunately, the accuracy result is still not high and many genes are selected for cancer classification since there is no direct probability relation between genetic algorithms (GA) and PSO. Generally, the proposed methods that based on PSO [1],[2],[8] are intractable to efficiently produce a near-optimal (smaller) subset of informative genes for higher classification accuracy. This is mainly because the total number of genes in microarray data is too large (higher-dimensional data).

2. METHODS

2.1 The Standard Version of Binary PSO (BPSO)

Binary PSO (BPSO) is initialised with a population of particles. At each iteration, all particles move in a problem space to find the optimal solution. A particle represents a potential solution (gene subset) in an *n*-dimensional space [4]. Each particle has position and velocity vectors for directing its movement. The position vector and velocity vector of the *i*th particle in the *n*-dimension can be represented as $X_i = (x_i^1, x_i^2, ..., x_i^n)$ and $V_i = (v_i^1, v_i^2, ..., v_i^n)$, respectively, where x_i^d is a binary bit, *i*=1,2,..*m* (*m* is the total number of particles); d=1,2,..*n* (*n* is the dimension of data).

In gene selection, the vector of particle positions is represented by a binary bit string of length n, where n is the total number of genes. Each vector denotes a gene subset. If the value of the bit is 1, it means that the corresponding gene is selected. Otherwise, the value of 0 means that the corresponding gene is not selected. Each particle in a generation updates its own position and velocity according to the following equations:

$$v_i^d = w^* v_i^d + c_1 r_1^* (pbest_i^d - x_i^d) + c_2 r_2^* (gbest^d - x_i^d)$$
(1)

$$Sig(v_i^{d}) = \frac{1}{1 + e^{-v_i^{d}}}$$
(2)

if
$$Sig(v_i^d) > r_3$$
, then $x_i^d = 1$; else $x_i^d = 0$. (3)

where w is the inertia weight. c_1 and c_2 are the acceleration constants in the interval [0,2]. r_1, r_2 , and r_3 are random values in the range [0,1]. $Pbest_i = (pbest_i^1, pbest_i^2, ..., pbest_i^n)$ and $Gbest = (gbest^1, gbest^2, ..., gbest^n)$ represent the best previous position of the *i*th particle and the global best position of the swarm (all particles), respectively. $Sig(v_i^d)$ is a sigmoid function where $Sig(v_i^d) \in [0,1]$.

2.2 An Improved Binary PSO (IPSO)

In this paper, we propose IPSO for gene selection. It is introduced to solve the problems derived from the microarray data, overcome the limitation of the related previous works [1],[2],[8], and inline with the diagnostic goal. IPSO in our work differs from the methods in the previous works in one major part. The major difference is that we modify the existing rule (Eq. 3) for the position update, whereas the previous works used a standard rule (Eq. 3). Firstly, we analyse the sigmoid function (Eq. 2). This function represents a probability for x_i^d to be 0 or 1 ($P(x_i^d = 0)$ or $P(x_i^d = 1)$). It has the properties as follows:

$$\lim_{v_i^d \to \infty} Sig(v_i^d) = 1$$
(4)

$$\lim_{v_i^d \to -\infty} Sig(v_i^d) = 0$$
(5)

if
$$v_i^d = 0$$
 then $P(x_i^d = 1) = 0.5$ or $Sig(0) = 0.5$ (6)

- if $v_i^d < 0$ then $P(x_i^d = 1) < 0.5$ or $Sig(v_i^d < 0) < 0.5$ (7)
- if $v_i^d > 0$ then $P(x_i^d = 1) > 0.5$ or $Sig(v_i^d > 0) > 0.5$ (8)

$$P(x_i^d = 0) = 1 - P(x_i^d = 1)$$
(9)

Also note that the value of x_i^d can change even if the value of v_i^d does not change, due to the random number r_3 in the Eq. 3. To propose IPSO, the following approaches are suggested:

2.2.1 Modify the existing rule of position update (Eq. 3)

In order to support the diagnostic goal that needs the least number of genes for accurate cancer classification, the rule of position update is simple modified as follows:

if
$$S(V_i) > r_3$$
, then $x_i^d = 0$; else $x_i^d = 1$ (10)

The value of particle velocity, V_i in the modified formula (Eq. 10) represents the whole of elements of a particle velocity vector, whereas the standard formula represents a single element. Moreover, V_i is also a positive real number. Based on this positive velocity value, Eq. 2, and Eq. 10, the possibility of $x_i^d = 1$ is too small. This situation causes a smaller number of genes is selected in order to produce a near-optimal gene subset from higher-dimensional data (microarray data).

2.2.2 A Simple Modification of the Formula of Velocity Update (Eq. 1)

In this formula, the calculation of the value of velocity is completely based on the whole of bits of a particle position vector, whereas the original formula (Eq. 1) is based on a single bit.

$$V_{i} = w * V_{i} + c_{1}r_{1} * (Pbest_{i} - X_{i}) + c_{2}r_{2} * (Gbest - X_{i})$$
(11)

2.2.3 Calculation for the distance of two positions

The number of different bits between two particles relates to the difference between their positions. For example, Gbest = [0011101000] and $X_i = [1100110100]$. The difference between Gbest and X_i is [-1-1110-11-100]. A value of 1 indicates that compared with the best position, this bit (gene) should be selected, but it is not selected, which may decrease classification quality and lead to a lower fitness value. In contrast, a value of -1 indicates that, compared with the best position, this bit should not be selected, but it is selected. The selection of irrelevant genes makes the length of the subset longer and leads to a lower fitness value. Assume that the number of 1 is a, whereas the number of -1 is b. We use the absolute value of (a-b), |a-b| to express the distance between two positions. In this example, |a-b|=|3-4|=1, so the distance between Gbest and X_i is $Gbest - X_i = 1$.

2.2.4 Fitness function

A fitness value of a particle (a gene subset) is calculated as follows:

$$fitness(X_i) = w_1 \times A(X_i) + (w_2(M - R(X_i)) / M)$$
(12)

in which $A(X_i) \in [0,1]$ is leave-one-out-cross-validation (LOOCV) accuracy on the training set using the only genes in X_i . This accuracy is provided by support vector machine classifiers (SVM). $R(X_i)$ is the number of selected genes in X_i . M is the total number of genes for each sample in the training set. w_1 and w_2 are two weights.

3. EXPERIMENTS

3.1 Data Sets and Experimental Setup

A real microarray data sets is used to evaluate IPSO, namely the leukaemia cancer data set. The leukaemia data set contains 72 samples of the expression levels of 7,129 genes. It can be obtained at http://www.broad.mit.edu/cgi-bin/cancer/datasets.cgi.

Firstly, we applied the gain ratio technique to pre-select 500-top-ranked genes. These genes are then used by IPSO in the next process. In this paper, LOOCV is used to measure classification accuracy of a gene subset that produced by IPSO. The implementation of LOOCV is in exactly the same way as did by Chuang *et al.* [1] Two criteria following their importance are considered to evaluate the performance of IPSO: LOOCV accuracy and the number of selected genes. A near-optimal subset that produces the highest classification accuracy with the smallest number of genes is selected as the best subset. Several experiments are independently conducted 10 times on each data set using IPSO and the standard version of binary PSO (BPSO). Next, an average result of the 10 independent runs is obtained.

3.2 Experimental Results

Based on the standard deviations of classification accuracy and the number of selected genes in Table 1, results that produced by IPSO were nearly consistent on the leukaemia data set. Interestingly, all runs have achieved 100% LOOCV accuracy with less than five selected genes. This means that IPSO has efficiently selected and produced a near-optimal gene subset from higher-dimensional data (microarray data).

Figure 1 shows that the average of fitness values of IPSO increases dramatically after a few generations. The higher average produces a smaller subset of selected genes with higher classification rate. The condition of velocity that should always be positive real numbers provided in the initialisation method, and the new rule of position update provoke the early convergence of IPSO. In contrast, the average of fitness values of BPSO was no improvement until the last generation.

| | Leukaemia Data Set | | | | |
|---------------|-----------------------------|-----------------|--|--|--|
| Kun# | Classification Accuracy (%) | #Selected Genes | | | |
| 1 | 100 | 4 | | | |
| 2 | 100 | 2 | | | |
| 3 | 100 | 4 | | | |
| 4 | 100 | 4 | | | |
| 5 | 100 | 3 | | | |
| 6 | 100 | 4 | | | |
| 7 | 100 | 4 | | | |
| 8 | 100 | 3 | | | |
| 9 | 100 | 4 | | | |
| 10 | _100 | 3 | | | |
| Average ± S.D | 100 ± 0 | 3.50 ± 0.71 | | | |

Table 1. Experimental results for each run using IPSO.

Note: Results of the best subsets shown in shaded cells. S.D. denotes the standard deviation, whereas #Selected Genes and Run# represent a number of selected genes and a run number, respectively.



Figure 1. A relation between the average of fitness values (10 runs on average) and the number of generations for IPSO and BPSO.

According to the Table 2, overall, it is worthwhile to mention that the classification accuracy and the number of selected genes of IPSO are superior to BPSO in terms of the best, average, and standard deviation results.

For an objective comparison, we compare our work with related previous works that used PSO in their methods [1],[2],[8]. It is shown in Table 3. The averages of LOOCV accuracy and the number of selected genes of our work were 100% and 3.5 selected genes, respectively. The latest previous work also came up with the similar LOOCV result to ours, but they used more than 1,000 genes to obtain the same result [1]. Overall, this work has outperformed the related previous works in terms of LOOCV accuracy and the number of selected genes.

| Data | Method | IPSO | | | The standard version of binary PSO (BPSO) | | |
|-----------|-------------------------------|----------|---------|------|---|---------|------|
| | Evaluation | The Best | Average | S.D | The Best | Average | S.D |
| Leukaemia | Classfication Accuracy (%) | 100 | 100 | 0 | 98.61 | 98.61 | 0 |
| | #Selected Genes | 2 | 3.50 | 0.71 | 216 | 224.70 | 5.23 |

Table 2. A comparison in terms of statistical results of the proposed IPSO and BPSO.

Note: The best result of each data set shown in shaded cells. S.D. denotes the standard deviation, whereas #Selected Genes represents a number of selected genes.

Table 3. A comparison between our method (IPSO) and other previous methods based

| Data | Method Evaluation | IPSO [Our work] | PSOTS (Shen et al. [8]) | IBPSO (Chuang et al.[1]) | PSOGA (Li et al. [2]) |
|-----------|--------------------------------|--------------------|----------------------------|-----------------------------|--------------------------|
| Leukaemia | Classification Accuracy (%) | (100) | (98.61) | 100 | (95.1) |
| | #Selected Genes | (3.5) | (7) | 1034 | (21) |

on PSO.

Note: The results of the best subsets shown in shaded cells. '-' means that a result is not reported in the related previous work. A result in '()' denotes an average result. #Selected Genes represents a number of selected genes. PSOTS = A hybrid of PSO and tabu search. IBPSO = An improved binary PSO. PSOGA = A hybrid of PSO and GA.

According to Fig. 1 and Tables 1-3, IPSO is reliable for gene selection since it has produced the near-optimal solution from microarray data. This is due to the modification of position update that causes the selection of a smaller number of genes. Therefore, IPSO yields the optimal gene subset (a smaller subset of informative genes with higher classification accuracy) for leukaemia cancer classification.

4. CONCLUSIONS

In this paper, IPSO has been proposed and tested for gene selection on the leukaemia microarray data set. Based on the experimental results, the performance of IPSO was superior to the standard version of binary PSO and related previous works. This is due to the fact that the modified rule of position update in IPSO causes a smaller number of genes is selected in each iterative, and finally produce a near-optimal subset of genes for better cancer classification. For future works, a combination between a constraint approach and PSO is proposed to increase the classification accuracy.

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