

MODELING WATER QUALITY PARAMETER BOD IN JOHOR RIVER AND
MUAR RIVER

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To my beloved father: Puah Eng Chiew

To my beloved mother: Ng Bee Kee

To my dearest grandfather: Puah Kok Kuah

To my dearest grandmother: Tan Siew Tin

To my precious brothers: Puah Chee Hock & Puah Zi Jian

To my precious sisters: Puah Lee Sia & Puah Lee Lee

To my precious brother in law: Chua Tor Hee

To my precious sisters in law: Yong Siew Lee & Lee Seow Ching

And

My adorable nieces and nephews

Thank you for all your love and support

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ABSTRACT

Rivers are one of the important sources of water. Rivers also support a diverse flora and fauna. As Malaysia is a fast becoming an industrial country, many of the rivers have become polluted. Water pollution is very harmful to human, animals and water life. Therefore, water quality models are very important to describe and to predict the observed effects of a change in the river system. Biochemical oxygen demand (BOD) concentration data of Sungai Johor and Sungai Muar in Johor were fitted to two models, namely Streeter-Phelps and nonlinear regression (NLR) models, by using weighted least squares method and Gauss-Newton method respectively. BOD is one of the indicators for river. The data used in the study is BOD concentration data of Sungai Johor and Sungai Muar in Johor state from year 1981 to year 1990 and the data were obtained from Drainage and Irrigation Department Malaysia. The performance of the results was tested by mean squared error (MSE). The NLR model gives the smaller MSE values for Sungai Johor and Sungai Muar with values of 0.662319 and 2.367337 respectively. Conclusively, the results showed that NLR model is a better model than Streeter-Phelps model in estimating the parameters of BOD concentration data of Sungai Johor and Sungai Muar in Johor.

ABSTRAK

Sungai adalah salah satu sumber air yang penting. Sungai juga menjadi tempat tinggal pelbagai binatang dan tumbuhan. Oleh sebab Malaysia berkembang pesat menjadi sebuah negara perindustrian, terdapat banyak sungai yang telah tercemar. Pencemaran air sangat bahaya kepada manusia, binatang dan hidupan akuatik. Oleh itu, model kualiti air sangat penting untuk menerangkan dan menjangkakan perubahan daripada kesan yang diperhatikan dalam sistem sungai. Data kepekatan keperluan biokimia oksigen (BOD) daripada Sungai Johor dan Sungai Muar di Johor telah digunakan dalam dua model, iaitu model Streeter-Phelps dan model regresi tak linear, masing-masing yang menggunakan kaedah wajaran kuasa dua terkecil dan kaedah Gauss-Newton. BOD ialah salah satu penunjuk ukur untuk sungai. Data yang digunakan dalam kajian ini ialah data kepekatan keperluan biokimia oksigen daripada Sungai Johor dan Sungai Muar di negeri Johor dari tahun 1981 hingga tahun 1990. Data ini diperolehi daripada Jabatan Saliran dan Perparitan Malaysia. Model regresi tak linear telah memberikan keputusan nilai ralat purata kuasa dua (MSE) yang lebih kecil untuk Sungai Johor dan Sungai Muar, iaitu 0.662319 dan 2.367337. Kesimpulannya, keputusan tersebut telah menunjukkan bahawa model regresi tak linear ialah model yang lebih baik daripada model Streeter-Phelps dalam menjangkakan ukuran bagi data kepekatan keperluan biokimia oksigen bagi Sungai Johor dan Sungai Muar di Johor.

TABLE OF CONTENTS

CHAPTER	TITLE	PAGE
	DECLARATION	ii
	DEDICATION	iii
	ACKNOWLEDGEMENT	iv
	ABSTRACT	v
	ABSTRAK	vi
	TABLE OF CONTENTS	vii
	LIST OF TABLES	xi
	LIST OF FIGURES	xii
	LIST OF ABBREVIATIONS	xiv
	LIST OF SYMBOLS	xv
1	INTRODUCTION	
	1.1 Introduction	1
	1.2 Background of the Study	4
	1.3 Problem Statement	5
	1.4 Objectives of the Study	6
	1.5 Scope of Study	6
	1.6 Significance of Study	7
	1.7 Thesis Organization	8

2	LITERATURE REVIEW	
2.1	Introduction	9
2.2	Water Resources and River Basins Management in Malaysia	9
2.3	Johor	12
2.3.1	Sungai Johor in Kota Tinggi	13
2.3.2	Sungai Muar in Segamat	14
2.4	Biochemical Oxygen Demand	15
2.5	Modeling Water Quality	17
2.5.1	Streeter-Phelps Model	18
2.5.2	Nonlinear Regression	19
2.6	The Case Studies in Malaysia Using the River Water Quality Models	20
2.7	The Application of Streeter-Phelps Model in the River Water Quality Models	21
2.8	The Application of Nonlinear Regression Model in the River Water Quality Models	22
2.9	Conclusion	23
3	RESEARCH METHODOLOGY	
3.1	Introduction	25
3.2	Research Procedures	26
3.3	Research Framework	27
3.4	Data Sources	27
3.5	Descriptive Statistics	28
3.5.1	Mean	29
3.5.2	Standard Deviation	29
3.6	The Derivation of Streeter-Phelps Model of Water Quality	30

3.6.1	Parameter Estimation for the Streeter-Phelps Model	31
3.7	The Derivation of Nonlinear Regression Model of Water Quality	32
3.7.1	Parameter Estimation for the Nonlinear Regression Model	33
3.7.1.1	The Gauss-Newton Method	33
3.7.1.1.1	Step Factor	35
3.8	Assumptions about Residuals in Regression Analysis	35
3.9	Mean Squared Error	36
3.10	Conclusion	37
4	ANALYSIS OF DATA	
4.1	Introduction	38
4.2	Real Data	38
4.2.1	BOD Data for Sungai Johor	39
4.2.2	BOD Data for Sungai Muar	40
4.2.3	Descriptive Statistics	40
4.2.4	Classification of the Water Quality	41
4.3	Parameter Estimation of Streeter-Phelps Model	43
4.3.1	Streeter-Phelps Model for Sungai Johor	43
4.3.2	Streeter-Phelps Model for Sungai Muar	45
4.4	Parameter Estimation of Nonlinear Regression Model	46

4.4.1	Nonlinear Regression Model for Sungai Johor	47
4.4.2	Nonlinear Regression Model for Sungai Muar	48
4.4.3	Checking Assumptions about Residuals for Sungai Johor	49
4.4.4	Checking Assumptions about Residuals for Sungai Muar	51
4.5	Mean Squared Error	54
4.6	Result and Discussion	57
4.7	Conclusion	59
5	CONCLUSION AND RECOMMENDATIONS	
5.1	Introduction	61
5.2	Conclusion	62
5.3	Recommendations	63
	REFERENCES	64

LIST OF TABLES

TABLE	TITLE	PAGE
3.1	BOD concentration of Sungai Johor	28
3.2	BOD concentration of Sungai Muar	28
4.1	Descriptive statistics of BOD concentration data for Sungai Johor and Sungai Muar	41
4.2	DOE water quality index classification	42
4.3	Calculation of MSE for the Streeter-Phelps model of Sungai Johor	55
4.4	Calculation of MSE for the Streeter-Phelps model of Sungai Muar	55
4.5	Calculation of MSE for the NLR model of Sungai Johor	56
4.6	Calculation of MSE for the NLR model of Sungai Muar	56
4.7	MSE for Streeter-Phelps model and NLR model of Sungai Johor and Sungai Muar	57

LIST OF FIGURES

FIGURE	TITLE	PAGE
1.1	Water quality status for river basins of Peninsular Malaysia	2
2.1	Source of water used in Malaysia	10
2.2	Districts of Johor	12
2.3	Map of Sungai Johor	13
2.4	Map of Sungai Muar	15
3.1	The research framework of this study	27
4.1	Time series plot of BOD concentration for the period of 76 months for Sungai Johor	39
4.2	Time series plot of BOD concentration for the period of 70 months for Sungai Muar	40
4.3	Time series plot of estimated BOD concentration for 76 months for Sungai Johor (Streeter-Phelps model)	44

4.4	Time series plot of estimated BOD concentration for 70 months for Sungai Muar (Streeter-Phelps model)	46
4.5	Time series plot of estimated BOD concentration for 76 months for Sungai Johor (NLR model)	47
4.6	Time series plot of estimated BOD concentration for 70 months for Sungai Muar (NLR model)	48
4.7	Residual plot of Sungai Johor (Streeter-Phelps model)	49
4.8	P-P plot to test for normality of Sungai Johor (Streeter-Phelps model)	50
4.9	Residual plot of Sungai Johor (NLR model)	50
4.10	P-P plot to test for normality of Sungai Johor (NLR model)	51
4.11	Residual plot of Sungai Muar (Streeter-Phelps model)	52
4.12	P-P plot to test for normality of Sungai Muar (Streeter-Phelps model)	52
4.13	Residual plot of Sungai Muar (NLR model)	53
4.14	P-P plot to test for normality of Sungai Muar (NLR model)	54
4.15	BOD concentration (mg/L) versus time for Sungai Johor	57
4.16	BOD concentration (mg/L) versus time for Sungai Muar	58
4.17	P-P plot to test for normality	58

LIST OF ABBREVIATIONS

ABBREVIATIONS	MEANING
DOE	Department of Environment
BOD	Biochemical Oxygen Demand
INWQS	Interim National Water Quality Standards
WQI	Water Quality Index
NLR	Nonlinear Regression
PS	point sources
NPS	non-point sources
LSE	Least Squares Estimates
MSE	Mean Squared Error
WHO	World Health Organization
UNICEF	United Nations Children's Fund
NWRC	National Water Resources Council
APHA	American Public Health Association
AN	Ammoniacal Nitrogen
COD	Chemical Oxygen Demand
DO	Dissolved Oxygen
TSS	Total Suspended Solid
USEPA	U. S. Environmental Protection Agency

LIST OF SYMBOLS

SYMBOLS	MEANING
$\%$	Percent
y	Response or dependent variable
x	Predictor or explanatory variable
km^3	Cubic kilometer
km^2	Square kilometer
km	Kilometer
$^\circ$	Degree
m^3	Cubic meter
mg/L	Milligram per liter
L	Amount of first order BOD remaining in wastewater at time t , mg/L
k_1	BOD reaction rate constant, time^{-1}
t	Time
$f(t, \theta)$	Predicted BOD, mg/L
μ	Mean
n	Number of observations
σ	Standard deviation
B_t	BOD concentration level at time t , mg/L
B_0	Ultimate BOD, mg/L
E	Disturbance or error term

CHAPTER 1

INTRODUCTION

1.1 Introduction

A river is a large natural stream of water flowing into an ocean, lake, wetland, sea or other body of water and usually fed along its course by converging tributaries. Small rivers may sometimes be called by several other names, such as stream, creek, brook, rivulet and rill.

Rivers are one of the important sources of water for households, industry and agriculture, and are used for navigation and recreational activities, including boating, angling and walking. Rivers also support a diverse flora and fauna. Although rivers contain only about 0.0001% of the total amount of water in the world at any given time, they are vital carries of water and nutrients to areas all around the earth. Rivers also play a very important role in the water cycle, acting as drainage channels for surface water. The world's rivers drain nearly 75% of the land's surface.

Many rivers have been polluted because of the rapid growth in industrialization to support the country's growing population and economy. Domestic and industrial sewage, agricultural wastes have polluted the rivers. According to Chapra (1997) each of these uses will affect the water quality.

Industries discharge their liquid waste products into rivers. Agriculture with chemical fertilizers and pesticides usage contribute to river pollution as rainwater drains these chemicals into the rivers. The size of towns and cities will grow as the population grows. Hence, the amount of domestic wastes that are thrown into rivers

will increase and add the level of pollution. It will pose a serious health problem if people continue to depend on this polluted water from the river. Pollution of river will also affect the reproductive ability of animal and fish species in rivers thus causes extinction in future.

Recent studies show that most of the rivers from all over the world, including Malaysia, are polluted. Based on the Malaysia Environment Quality Report 2007, the Department of Environment (DOE) has described that one of the major pollutants is Biochemical Oxygen Demand (BOD). Data from DOE in 2004, based on BOD, 18 river basins were classified polluted, 37 river basins were slightly polluted and 65 river basins were in clean condition. According to the Malaysian River Classification and River Water Quality Monitoring Project Reports, the general trend of the overall river water quality in Malaysia is deteriorating. There are several factors, such as domestic and industrial sewage, agricultural wastes and discharge from livestock and heavy metal, will influence the river water quality which will lead to deterioration of river water quality (Abu Bakar and Dalilah, 2007). Figure 1.1 shows the water quality status for river basins of Peninsular Malaysia.



Figure 1.1 Water quality status for river basins of Peninsular Malaysia

According to the Interim National Water Quality Standards (INWQS), water quality of the main river basins in Malaysia was assessed based on the Water Quality Index (WQI) score using Roman numerals I, II, III, IV and V, where had been recommended as very clean, clean, moderate, slightly polluted and severely polluted respectively.

Nowadays several water quality models exist and have been applied in many regions from all over the world for various purposes. It has become a priority to model the water quality for simulating the level of river water pollution. Many researchers had created a large number of water quality models. The water quality models are not only for assessing water quality and detecting trends of water quality parameters, but for identifying the impact on water quality of the various potential alternative actions. Water quality models can be classified based on the type of approach, pollutant items, area of applications, nature etc. (Tsakiris and Alexakis, 2012). Many different types of models are used for different problems and purposes, appropriate model and data are chosen based on the purpose of the specific study.

In this research, two models are chosen to fit the data of the two rivers in Johor state. The two models are Streeter-Phelps model and nonlinear regression (NLR) model. Streeter-Phelps model and NLR model have been applied in many fields such as management science, physics, biology, electronics, engineering, economics and psychology, and in operations research. They have spread widely over queuing, finance and insurance.

A thorough grounding in linear regression (LR) is fundamental to understanding NLR. LR is the most widely used of all statistically techniques. LR is an approach for modeling the relationship between a dependent variable, y , and one or more explanatory variables denoted by x . The case of one explanatory variable is called simple linear regression. For more than one explanatory variable, the process is called multiple linear regressions (Freedman, 2009).

The basic idea of the NLR is almost the same as in the LR, namely to relate a response or dependent variable, y , to a vector of predictor variables or explanatory variables x . NLR is characterized by the fact that the prediction equation depends nonlinearly on one or more unknown parameters. On the other hand, LR is often used for building a purely empirical model. NLR usually arises when there are physical reasons for believing that the relationship between the response and the predictors follows a particular functional form (Smyth, 2002).

1.2 Background of the Study

River pollution is one the most common hazard in many countries in the world, which includes Malaysia. There are two main sources in contributing to the river water pollution, which are point sources (PS) and non-point sources (NPS). The point sources consist of detectable sources pollution component such as domestic waste water discharge and industrial waste water discharge. Non-point sources are undetectable pollution sources such as surface runoffs, agriculture activities and so on.

In recent times, the rapid growth in industrialization to support the country's growing population and economy had caused river pollutions due to domestic and industrial sewage, agricultural wastes. Activities such as deforestation due to illegal logging, mining, clearance of land for various usage like agriculture, housing and industrial purposes had ruined the ecosystem and increased the sediments in river. The sediments contain other materials such as organics matter, nutrients and toxics. It will increase the BOD level of river. BOD is one of the indicators for river pollution besides Ammoniacal Nitrogen (AN), Chemical Oxygen Demand (COD), Dissolved Oxygen (DO), Total Suspended Solid (TSS) and pH. The water quality model of the rivers is very important in order to solve the problem of deterioration of

river water. There are many types of water quality models due to wide variety of river system. Each type of river water body needs the appropriate type of model.

In this research, the study gives an understanding to the potential change in the data of BOD from year 1981 to year 1990. The study aims to benefit environment engineer, scientist, specialist and agency in designing and managing the river systems based on the expected BOD data over a certain period of time.

To estimate the parameters for the Streeter-Phelps model and NLR model, this study focuses on the weighted least squares and Least Squares Estimates (LSE) methods respectively. The advantage of using LSE is that the method is fairly simple and produces consistent estimators.

1.3 Problem Statement

A study has been done by DOE on 116 rivers nationwide. Some 10 percent of these rivers are heavily polluted or dead, 63 percent are polluted and only 27 percent are healthy. The study also showed that 70 percent of the pollution is caused by human activities such as deforestation, dumping and logging. Furthermore, arising of new development land use for agriculture and sand extractions may cause a lot of pollution to river water quality.

As Malaysia is a fast becoming an industrial country, many of the rivers have become polluted due to a lot of wastes that have been discharged into the rivers. Water pollution is very harmful to human, animals and water life.

In order to model the water quality of the river, two models were used in this study, namely Streeter-Phelps model and NLR. LR is a powerful method for analyzing data described by models which are linear in the parameters. It has a mathematical expression which relates the response to the predictor variables, and these models are usually nonlinear in the parameters. In such cases, linear regression techniques must be extended, which introduces considerable complexity.

In this study, information related to BOD concentration data is valuable towards designing water treatment structures.

1.4 Objectives of the Study

The main objectives of the study are:

1. to estimate the parameters of Streeter-Phelps model and NLR model using weighted least squares and LSE.
2. to compare which model is the best fit to the data of the two rivers in Johor state using Mean Square Error (MSE).

1.5 Scope of Study

In this study, Streeter-Phelps model and NLR model were used. The BOD concentration data for the two rivers in Johor state from year 1981 to year 1990 is analyzed. The values of the parameter estimations of the Streeter-Phelps and NLR

models had been estimated by using the weighted least squares and LSE methods. The Gauss-Newton method is used to estimate the parameters in the NLR.

Finally, to find the best model in this study, MSE will be utilized.

1.6 Significance of Study

Analysis of river water pollution is significant to many as it is beneficial for managing the consumption of water, improving the river basins and predicting the level of water pollution in Malaysia. Better estimation will assist environment engineer, scientist or specialist to design and manage the river water resources more efficiently. The analysis and information about river water quality can be used to evaluate and measure the level of water pollution so that the appropriate actions will be taken once the degree of the related river is polluted or severely polluted is found.

Moreover, environmental agencies will be able to predict the practical material that should be used for water treatment to improve the water quality. From the information received, the relevant authorities can make better decision to control water pollution and provide an alternative to better water quality management. Besides, it is hoped that the study may contribute towards preventing unnecessary costs and economic damages as well as avoiding danger and hazard as a result of river water pollution in the country.

1.7 Thesis Organization

This thesis is organized into five chapters. Chapter 1 is the introduction of this thesis. It highlights the background of the study and the problem statement. Objectives and scopes of this study are also mentioned in this chapter together with significance of study.

Chapter 2 outlines literature review of this study. It starts with a discussion on the water resources and river basins management in Malaysia, followed by an introduction of Sungai Johor in Kota Tinggi and Sungai Muar in Segamat which are the scope of this study. This chapter discusses the basic knowledge of BOD, the application of Streeter-Phelps model and NLR model in the water quality modeling done by earlier researchers. In this chapter, previous work and studies that are related to the research is highlighted.

Chapter 3 includes the methodology used to estimate the unknown parameters in Streeter-Phelps and NLR models. For the parameter estimation in the NLR model, the Gauss-Newton method is introduced and calculated. All the steps that are considered and discussed in Chapter 3 are summarized in the research framework in Section 3.3. A detailed explanation about the data sources of the study is also presented.

Chapter 4 presents the descriptive statistics of the BOD concentration data and the analysis of the results are reported. Next, the values of the parameter estimations of the Streeter-Phelps and NLR models are estimated using the weighted least squares and LSE methods. Finally, the performances of the two models are compared by using mean squared error (MSE).

Lastly, Chapter 5 discusses the conclusion of this dissertation. A few recommendations for the future studies are also presented at the end of the chapter.

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