

CONTROL OF BRUSHLESS DC MOTOR USING SINGLE-INPUT FUZZY
PROPORTIONAL-INTEGRAL CONTROLLER

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To my family for their ever loving support over the years
To my friends for their never ending encouragement and support

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ABSTRACT

Over the years, development in control industry has brought a hybrid controller, Fuzzy Proportional-Integral (PI) Controller (FPIC) as Brushless DC (BLDC) motor speed regulator with as good performance as PI controller. The FPIC suffers from lengthy design time due to the large number of rules and parameter tuning. Thus, this thesis proposes a newly developed Single-Input Fuzzy PI Controller (SIFPIC) to be used as the BLDC motor speed controller. SIFPIC is a simplified version of FPIC with one input variable derived using signed distance method. SIFPIC gives a speed performance comparable to the FPIC but with much faster computing time and simpler tuning process. The motor performance with SIFPIC is evaluated through simulation and experimental approach in terms of speed, current and torque response under several test conditions. The performance is then compared with the motor performance with discrete PI and FPIC speed controller. FPIC is excluded from the comparison in the experiment due to the limitation of DS1104 Digital Signal Processor. From the simulation conducted, SIFPIC produced a comparable performance as FPIC in speed response where both controllers eliminated undershoot and oscillation problems. Under constant speed and changing speed conditions, SIFPIC also showed its superiority from discrete PI controller with average of 36.3% and 11.7% lower ripples than discrete PI controller, respectively. The simulation findings have been verified by the experimental results.

ABSTRAK

Selama bertahun-tahun, pembangunan dalam industri kawalan telah membawa pengawal hibrid iaitu pengawal kabur kadar kamir (FPIC) sebagai pengawal kelajuan motor arus terus tanpa berus (BLDC) dengan prestasi sebaik pengawal kamiran-berkadar (PI). Namun, pengawal FPIC yang dihasilkan mempunyai masalah iaitu memerlukan masa yang panjang untuk mereka-bentuk pengawal kerana mempunyai jumlah parameter talaan dan peraturan kawalan yang banyak. Oleh itu, tesis ini mencadangkan Pengawal Kadar Kabur Kamir Masukan Tunggal (SIFPIC) untuk digunakan sebagai pengawal kelajuan untuk sistem motor BLDC. Pengawal SIFPIC adalah versi yang dipermudahkan daripada FPIC yang mempunyai masukan tunggal yang diterbitkan menggunakan kaedah jarak bertanda. Pengawal SIFPIC memberikan prestasi kelajuan setanding dengan pengawal FPIC tetapi dengan masa pengiraan yang lebih cepat dan proses penalaan yang lebih mudah. Prestasi motor BLDC dengan SIFPIC dinilai melalui pendekatan simulasi dan ujikaji tindak balas kelajuan, motor, arus dan daya kilas di bawah beberapa keadaan ujian. Seterusnya, prestasi motor akan dibandingkan dengan prestasi motor yang dikawal oleh pengawal PI diskrit dan pengawal FPIC. FPIC dikecualikan daripada kajian perbandingan disebabkan oleh kekangan memproses isyarat digital DS1104. Daripada hasil simulasi, pengawal SIFPIC menghasilkan prestasi setanding FPIC dalam tindak balas kelajuan motor dimana kedua-dua pengawal menghapuskan masalah lajukan turun dan ayunan. Dibawah keadaan kelajuan tetap dan berubah, SIFPIC menunjukkan keunggulan berbanding pengawal PI diskrit dengan purata 36.3% dan 11.7% riak yang lebih kecil untuk arus dan daya kilas. Penemuan simulasi telah disahkan oleh hasil eksperimen.

TABLE OF CONTENTS

CHAPTER	TITLE	PAGE
	DECLARATION	ii
	DEDICATION	iii
	ACKNOWLEDGMENT	iv
	ABSTRACT	v
	ABSTRAK	vi
	TABLE OF CONTENTS	vii
	LIST OF TABLES	xi
	LIST OF FIGURES	xii
	LIST OF SYMBOLS	xv
	LIST OF ABBREVIATIONS	xvii
	LIST OF APPENDICES	xix
1	INTRODUCTION	1
	1.1 Overview	1
	1.2 Objective of the Research	4
	1.3 Scope of the Research	4
	1.4 Importance of Research	5
	1.5 Organization of Thesis	5
2	BRUSHLESS DC MOTOR DRIVE CONTROL TECHNIQUES	7
	2.1 Introduction	7
	2.2 Brushless DC Motor Drive (BLDC)	8
	2.2.1 Motor Construction	8

2.2.2	Comparison between Brushless and Brushed DC Motor	10
2.3	BLDC Mode of Operation	11
2.3.1	Single-phase BLDC Motor Drive	12
2.3.2	Three-phase BLDC Motor Drive	12
2.4	Speed Control Technique	16
2.4.1	Model Based Controller	18
2.4.1.1	PI/PD/PID Controller	18
2.4.1.2	Deadbeat Controller	22
2.4.1.3	Sliding Mode Controller (SMC)	23
2.4.2	Non-model Based Controller	25
2.4.2.1	Fuzzy Logic Controller (FLC)	25
2.4.2.1.1	Operation of Fuzzy Control	26
2.4.2.1.2	FLC Issues	30
2.4.2.2	Neural Network	31
2.4.3	Hybrid Controller	32
2.4.3.1	Fuzzy Sliding Mode Controller (FSMC)	33
2.4.3.2	Fuzzy PI Controller (FPIC)	35
2.5	Summary	36
3	SINGLE-INPUT FUZZY PI CONTROLLER (SIFPIC)	37
3.1	Introduction	37
3.2	Number of Input and Rules Reduction	38
3.3	Control Surface	42
3.4	Relationship Between Single-Input FLC (SIFLC) and Discrete PI Controller	51
3.4.1	Small Signal Disturbance	54
3.4.2	Large Signal Disturbance	56
3.5	Summary	57
4	METHODOLOGY	58
4.1	Introduction	58

4.2	BLDC Motor Drive System Model Design	59
4.2.1	Back EMF Generation	60
4.2.2	SIFPIC Controller Design	61
4.3	Simulation Work	64
4.3.1	Control Surface Test	66
4.3.2	Discrete PI and Fuzzy PI Controller	69
4.4	Hardware Implementation	71
4.4.1	Controller Design using Rapid Prototyping in Real-Time Interface (RTI)	73
4.5	Summary	76
5	RESULTS AND ANALYSIS	77
5.1	Introduction	77
5.2	Simulation Based on Motor Rating	78
5.2.1	Speed Response	78
5.2.1	Current Response	81
5.2.1	Torque Response	84
5.3	Simulation Based on Hardware Capability	87
5.2.2	Speed Response	88
5.2.2	Current Response	91
5.2.2	Torque Response	93
5.4	Experiment	95
5.4.1	Speed Response	95
5.4.2	Current Response	99
5.4.3	Torque Response	101
5.5	Results Validation	103
5.6	Summary	104
6	CONCLUSION	105
6.1	Conclusion	105
6.2	Contribution	107
6.3	Future Work	108

REFERENCES	109
Appendices A-G	115

LIST OF TABLES

TABLE NO.	TITLE	PAGE
2.1	Rule table with Toeplitz structure	29
3.1	Rule table with Toeplitz structure of a typical FLC	39
3.2	Reduced rule table	41
4.1	System parameter	59
4.2	Inner and outer control loop parameter	63
4.3	Summary from control surface test	68
4.4	List of equipment with description	73
5.1	Summary of results comparison	103

LIST OF FIGURES

FIGURE NO.	TITLE	PAGE
2.1	BLDC motor construction and label	9
2.2	BLDC motor physical construction (a) in-runner configuration (b) out-runner configuration	9
2.3	Permanent magnet arrangement in rotor	10
2.4	Structure of Brushed and Brushless DC motor	11
2.5	H-bridge circuit of single-phase BLDC motor drive	12
2.6	Three-phase bridge connection for 3-phase BLDC motor drive	13
2.7	Equivalent circuit of BLDC motor	13
2.8	Switching state and conduction sequence according to the operating modes	15
2.9	Back EMF (e_a, e_b, e_c) and phase current waveform (I_a, I_b, I_c) of BLDC motor drive	16
2.10	General block diagram of a closed-loop control system	17
2.11	Tree diagram shows the classification of control techniques	18
2.12	Block diagram of PID control feedback loop	19
2.13	Pole mapping on s-plane to z-plane using Dead-beat control technique	22
2.14	Illustration of general process of Fuzzy Logic	27
2.15	Example of membership function of Fuzzy Logic in triangular shape	27
2.16	Second order dynamic response	29
2.17	The interconnection between the neurons in layers	31
2.18	Fuzzy Sliding Mode Control by [35] in 1992	33
2.19	The control surface of FSMC	34

2.20	Fuzzy PI Controller standard control scheme	35
3.1	The illustration of derivation of signed distance, d	39
3.2	The control structure for SIFLC	41
3.3	Linear control surface	42
3.4	Non-linear control surface with low degree of non-linearity	42
3.5	Non-linear control surface with high degree of non-linearity	43
3.6	Analysis of approximate linear surface produced by different set of membership function of input and output	44
3.7	The piecewise linear region with adjustable slope representing non-linear behavior	45
3.8	(a) Approximate linear control surface with evenly arranged membership function of input sets (b) The equivalent control surface of FLC	47
3.9	(a) Approximated control surface of adjusted peak location of input sets (b) Equivalent control surface of FLC	48
3.10	(a) Approximate control surface with adjusted location of output singleton (b) Equivalent control surface of FLC	49
3.11	(a) Approximate control surface with additional membership function in input and output sets (b) Equivalent control surface of FLC	50
3.12	The control structure of SIFLC	52
3.13	The control structure of discrete linear PI controller	53
4.1	Block diagram of the complete drive system of BLDC motor	59
4.2	Mathematical model of BLDC motor	61
4.3	Mathematical control structure of outer control loop	62
4.4	BLDC motor drive system model in MATLAB/Simulink	64
4.5	SIFPIC speed controller Simulink model	65
4.6	Discrete PI current controller Simulink model	65
4.7	Control surface A; altered peak location of triangular input set	66
4.8	Control surface B; altered location of singleton output set	67
4.9	Control surface C; added membership function into both input and output	67

4.10	Discrete PI speed controller modeled in Simulink	69
4.11	The Simulink model of FPIC	70
4.12	Control surface for FPIC	72
4.13	Schematic diagram of the overall BLDC system configuration	72
4.14	Snapshot of experiment set-up	72
4.15	Simulink model of controllers and generators with RTI I/O blocks	75
4.16	Simulink model of open loop BLDC motor with RTI I/O blocks	76
5.1	Speed response under several test conditions	79-81
5.2	Current responses under several test conditions	82-84
5.3	Torque response under several test conditions	85-87
5.4	Speed response under several test conditions	88-90
5.5	Current response under several test conditions	91-92
5.6	Torque response under several test conditions	93-94
5.7	Speed response from experiment under several conditions	96-98
5.8	Current response from experiment under several conditions	99-100
5.9	Torque response from experiment under several conditions	101-102

LIST OF SYMBOLS

B	–	Damping factor
ce	–	Change of error
$d, d(k)$	–	Signed distance input
d_{bp}	–	Breakpoint distance
d_o	–	Distance from random point to origin line
d_{sn}	–	Distance from sliding surface to random point
e_a, e_b, e_c	–	Back EMF of phase a, b and c
$e, e(k)$	–	Error signal
$e_p, e_p(k)$	–	Scaled error signal
$\dot{e}, \dot{e}(k)$	–	Change of error signal
$\dot{e}_p, \dot{e}_p(k)$	–	Scaled of change of error signal
f_c	–	Cross-over frequency
f_s	–	Switching frequency
$f_a(\theta), f_b(\theta), f_c(\theta)$	–	Rotor angle function for phase a, b and c
i_a, i_b, i_c	–	Motor phase current
i_{ref}	–	Current reference
J	–	Moment of inertia
k_b/k_e	–	Back EMF constant
k_e	–	Input scaling factor for error signal
$k_{\dot{e}}$	–	Input scaling factor for change of error signal
k_d	–	Derivative gain
k_i	–	Integral gain
k_p	–	Proportional gain
k_t	–	Torque constant
k_u	–	Ultimate gain for Ziegler-Nichols tuning
L_s	–	Stator inductance

m, n	–	Gain parameter for SIFPIC
R_k	–	k^{th} rule of FLC
R_s	–	Stator resistance
T	–	Period
T_e	–	Electromagnetic torque
T_d	–	Derivation period for Ziegler-Nichols
T_i	–	Integral period for Ziegler-Nichols
T_L	–	Load torque
T_s	–	Sampling time
T_{s1}, T_{s2}	–	Sampling time for inner and outer loop
T_u	–	Period of oscillation for Ziegler-Nichols
$u, u(k)$	–	Actual control output
$\dot{u}, \dot{u}(k)$	–	Change of actual control output
$\dot{u}_o, \dot{u}_o(k)$	–	Control output from lookup table
v_a, v_b, v_c	–	Motor voltage for phase a, b and c
w_o, w_m	–	Output/motor speed
w_{ref}	–	Speed reference
x_1, x_2	–	Crisp data
x	–	Input state variable
\dot{x}	–	Change of input state variable
z^{-1}	–	Unit delay
α_{ss}, α_{ls}	–	Slope for small and large signal disturbance
r	–	Scaling factor
p	–	Fuzzification level
q	–	Number of input
μ	–	Degree of membership function
ω_n	–	Natural frequency
ψ	–	Control surface
ζ	–	Damping ratio

LIST OF ABBREVIATIONS

AC	–	Alternating Current
ADC	–	Analogue to Digital Converter
BLDC	–	Brushless DC
BoA	–	Bisector of Area
CoG	–	Centre of Gravity
CoGS	–	Centre of Gravity Singleton
DAC	–	Digital to Analogue Converter
DC	–	Direct Current
DSP	–	Digital Signal Processor
EMF	–	Electromagnetic Force
EMI	–	Electromagnetic Interference
FLC	–	Fuzzy Logic Control
FPIC	–	Fuzzy PI Controller
FSMC	–	Fuzzy Sliding Mode Control
IGBT	–	Insulate Gate-Bipolar Transistor
MoM	–	Mean of Maxima
NB	–	Negative Big
NS	–	Negative Small
PB	–	Positive Big
PD	–	Proportional Derivative
PI	–	Proportional Integral
PID	–	Proportional Derivative Integral
PS	–	Positive Small
PWM	–	Pulse Width Modulation
RTI	–	Real-Time Interface
SIFLC	–	Single-Input Fuzzy Logic Controller
SIFPIC	–	Single-Input Fuzzy PI Controller

SMC	—	Sliding Mode Control
SW	—	Switch
UoD	—	Universe of Discourse
Z	—	Zero

LIST OF APPENDICES

APPENDIX	TITLE	PAGE
A	Ziegler-Nichols Tuning Table	115
B	Fuzzy Logic Controller (FLC) Implementation	116
C	Simulink Model	118
D	Control Surface Test	119
E	Hardware Implementation	129
F	Speed Response Under Step-up Speed Command	133
G	List of Publications	134

CHAPTER 1

INTRODUCTION

1.1 Overview

Energy exists in variety of forms: kinetic, electrical, mechanical, chemical and potential energy. In power electronic and electric drive field, energy is mainly in either electrical or mechanical energy depends on the application requirements. There are also applications that use both form of energy known as electro mechanics such as traffic light and washing machine. Electromechanical devices involve energy conversion either an electrical signal creating mechanical movement or mechanical movement creating the electrical signal with the aid of converters [1]. Those devices are more known as electric machines. The machine is said to act as a motor when conversing electrical energy into mechanical energy and as a generator when conversion is vice-versa.

Electric motor is the prime movers of the electrical drive which is applied for a system with motion control requirement. Most electric motors are used in constant speed operation that do not need to be controlled unless for starting, stopping and protection [1, 2]. However, at some point there is need for the motor to be controlled where speed and torque must support the mechanical load demand. The electric motor is categorized into two classes: Direct Current (DC) and Alternating Current (AC) motor. DC motor can be controller over a wide range of speed by using either a variable voltage supply or by changing strength of field winding current. The AC motor operates with two rotating or moving magnetic fields on the rotor and stator respectively [2]. Two main types of AC motor are induction and synchronous motor. The induction motor always relies on slip speed to induce the rotor AC current while

synchronous motor uses either permanent magnet, salient poles or independent excited rotor winding.

In this work, a permanent magnet Brushless DC (BLDC) motor is used for the drive system. BLDC motor is a three-phase synchronous motor which received AC current converted from DC power supply by power inverter. The BLDC motor is made up of permanent magnet rotor and stator winding with rectangular stator current that produces trapezoidal back electromotive force (EMF) and a constant torque [3]. Thus in order to obtain variable speed operation, the motor requires a drive system operates in electromechanical system that includes an electronic motor controller and a rotor position feedback sensor. BLDC motor has the ability to develop high torque with good speed response which is appealing in motion control industry [3, 4]. Besides that, BLDC motor has excellent efficiency, higher power density and a simple control scheme.

Since the 1990's, the Proportional-Integral (PI) controller is widely known and used in electric drive field due to its fast and efficient response [5]. PI controller is a linear controller that implements a well-established design procedure such as bode-plot technique, Nyquist and etc. In addition, the performance of this type of controller is easy to analyze using several mathematical and computer tools that have been established. PI controller has a few disadvantages and the most known is its limitation of operating well in one point. Thus, as it is desirable to have variable-speed operation in a non-linear system, PI controller may not be the best option. Other than that, PI controller also has slow computation, oscillation and overshoot problems and complicated mathematical model [5, 6]. Non-model based method such as Neural Network and Fuzzy Logic can help get rid of the problem in deriving the mathematical model of a system.

Fuzzy Logic Controller (FLC) is commonly more familiar in drive control industry than Neural Network and other Artificial-Intelligence method. FLC basically uses an algorithm to systematically convert the linguistic rules into an automatic control scheme [7]. This type of controller has a few advantages over PI controller such as auto-tuning technology where it can be set manually by the

researcher; it can be used for a broad range of operating condition and produces a precise control performance. However, despite all the benefits offered, FLC still suffers from lengthy period of design procedure due to many parameters and number of rules to tune. In addition, it does not have any standard design procedure which means the design still based on heuristic method [8].

Experimental approach in purpose to analyze the comparison between FLC and PI speed response in high-performance AC drives has been done and recorded in [9]. The study concluded that FLC does not necessarily superior over PI controller except in case of load transient rejection; FLC is indeed always superior. Some researchers have implemented a new kind of controller where both FLC and PI controller is combined, namely a hybrid controller as way to overcome the issues of both controllers. The hybrid Fuzzy PI Controller (FPIC) gives control performance with shorter settling time, better robustness and stability [10]. The fuzzy part of this controller can be structured as its PI counterpart in small signal disturbance in where the control surface exhibits a linear surface. One main drawback of FPIC is that it is not a mathematical-based controller which means it cannot avoid heuristic design approach and make it still suffers from lengthy designing time.

In this research, Single-Input Fuzzy PI Controller (SIFPIC) is proposed as the speed controller instead of the conventional FPIC for the BLDC motor drive system. SIFPIC introduced a new variable called distance, d as the sole-input to the controller which has been previously derived by [11] through signed-distance method. SIFPIC has simple generation and tuning process but still able to provide a control response comparable to the conventional controller response but with much shorter computing time.

1.2 Objective of Research

The objectives of this research are:

- (i) To design the SIFPIC as speed controller for BLDC motor drive system.
- (ii) To construct and develop a prototype of BLDC motor drive system with SIFPIC as the speed controller.
- (iii) To evaluate the speed, current and torque performance of SIFPIC through simulation and experimental approach.

1.3 Scope of Research

This research will cover a comprehensive and inclusive review of control method for motor drive especially for BLDC motor drive. Previous related work on motor drive are reviewed and analyzed critically. The purpose of the review is to propose a simple control method for the drive system. This work proposed SIFPIC as the speed controller for the BLDC motor drive system which has been developed in previous study for a converter regulation. The modeling design of SIFPIC and simulation works are done using software MATLAB/Simulink. The evaluation of the SIFPIC is evaluated through comparison with discrete PI controller and FPIC in form of speed, current and torque response. This work will also implement a hardware prototype to validate the simulation findings through experimental approach.

1.4 Importance of Research

It is believed that the conventional Fuzzy PI controller has solved the small signal disturbance issues, yet for large signal disturbance, the complication of heuristic tuning and the lengthy design time cycle is still become great obstacle. In addition to that, consistent response is somewhat difficult to achieve as the system has to consider large number of rules and parameters to tune. These problems can be solved by implementing SIFPIC as proposed. SIFPIC used single variable as its input which called signed-distance, d derived from signed-distance method. SIFPIC reducing the number of rules that needed to tune make it a simpler control scheme. The computation time of the system is expected to become very fast and SIFPIC can easily behaves as discrete PI controller in small signal disturbance with approximately equivalent response.

1.5 Organization of Thesis

This thesis is organized into five chapters. Their contents is outlined as follows:

- (i) Chapter 2 provides a comprehensive literature review of control method on regulating the speed of BLDC motor. The review includes for both linear and non-linear system. The advantages and disadvantages of all methods are all listed.
- (ii) Chapter 3 proposes the SIFPIC as the simpler version of the conventional Fuzzy PI controller. The controller introduced a concept of Signed-distance method in order to shorten the computation time. A relationship with discrete PI controller is established with discussion on the control surface of fuzzy controller is presented.

- (iii) Chapter 4 presents the design procedures of closed loop BLDC motor drive system in MATLAB/Simulink. System simulation and performance evaluation is done under several conditions and were compared with the performance of discrete PI controller and FPIC. This chapter also presents the complete procedure of hardware implementation of the controller on drive system..
- (iv) Chapter 5 presents the results from both simulation and experimental approach. A discrete PI controller and FPIC have been developed for comparison purpose. However, FPIC does not included in experimental approach due to difficulty in processing the rule inference in the actual system. This chapter also provides the detail analysis on the response.
- (v) Chapter 6 concludes the research on the proposed method for the motor drive system. The conclusion is made through the analysis of the control response from both simulation and experimental approach.

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