# NON-LINEAR FINITE ELEMENT ANALYSIS OF STEEL FIBRE SELF COMPACTING REINFORCED CONCRETE BEAMS

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A project report submitted in fulfilment of the requirements for the award of the degree of Master of Engineering (Structure)

School of Civil Engineering Universiti Teknologi Malaysia To my beloved mother, Noribah binti Sadar, my supportive family and friends for their love and encouragement.

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#### **ABSTRACT**

Steel fibre reinforced concrete (SFRC) may be defined as a composite material made with portland cement, aggregate, and incorporating discrete discontinuous fibres. The role of randomly distributed discontinuous fibres is to bridge across the cracks which provide post-cracking ductility. Through this study, the models of reinforced concrete (RC) beam were developed by using finite element method to observe and simulate the behaviour of RC beam in terms of cracking pattern and the relationship between shear and deflection. The data on mechanical properties such as tensile strength, compressive strength and flexural strength were adopted from the previous study. By using LUSAS Software, a nonlinear analysis is carried out where three beams were modelled considering the different type of concrete mix namely Normal Concrete (NC), Self Compacting Concrete (SCC) and Steel Fibre Self Compacting Concrete (SFSCC). SFSCC was used where the stirrups were reduced to 50% in order to study the possibility of steel fibre to partly replaced normal stirrups. The analysis observed that the addition of 1% steel fibre by volume in plain concrete with the same number of stirrups produced 37.1% increment in ultimate shear load resistance compared to control sample (NC125). Meanwhile, an appreciable increase in strength was also recorded for the beam with increased stirrups spacing, which is 31.8%. The addition of steel fibre in the concrete mix also improved the ultimate deflection of the beam in the range of 15.6% and 35%. The comparative study between Finite Element Analysis (FEA) and the experimental result showed a small difference range, between 8% and 18%, thus, proving the numerical prediction using LUSAS software.

#### **ABSTRAK**

Konkrit tetulang dengan gentian keluli (SFRC) boleh didefinisikan sebagai bahan komposit yang dibuat dengan simen portland, agregat, dan menggabungkan gentian yang berasingan. Peranan gentian keluli yang ditabur secara rawak adalah untuk merentasi keretakan seterusnya memberikan kemuluran semasa pasca-retak. Melalui kajian ini, rasuk konkrit bertetulang (RC) dimodelkan dengan menggunakan kaedah unsur terhingga (FEM) untuk memerhati dan mensimulasikan keadaan rasuk RC dari segi corak retakan dan hubungan antara kekuatan ricih dan lenturan rasuk.Ciri-ciri mekanikal seperti kekuatan tegangan, kekuatan mampatan dan kekuatan lenturan diadaptasi dari kajian terdahulu. Dengan menggunakan perisian LUSAS, satu analisis tidak linear dijalankan di mana tiga rasuk dimodelkan dengan jenis campuran konkrit yang berbeza iaitu konkrit biasa (NC), konkrit mampatan sendiri (SCC) dan konkrit mampatan sendiri dengan gentian keluli (SFSCC). Untuk mengkaji potensi gentian keluli dalam mengantikan rakap biasa, SFSCC digunakan di mana rakap dikurangkan kepada 50%. Analisis menunjukkan bahawa penambahan gentian keluli sebanyak 1% dalam konkrit biasa dengan bilangan rakap yang sama menghasilkan kenaikan kekuatan ricih sebanyak 37.1% berbanding dengan sampel kawalan (NC125). Sementara itu, peningkatan kekuatan yang ketara juga direkodkan pada rasuk dengan tambahan jarak rakap, iaitu sebanyak 31.8%. Penambahan gentian keluli dalam campuran konkrit juga telah meningkatkan nilai lenturan rasuk iaitu dalam julat 15.6% dan 35%. Kajian perbandingan antara analisis unsur terhingga (FEA) dan hasil eksperimen menunjukkan perbezaan yang kecil, antara 8% dan 18%. Hal ini membuktikan kesahihan ramalan berangka menggunakan perisian LUSAS.

# TABLE OF CONTENTS

CHAPTER	TITLE	PAGE
	DECLARATION	ii
	DEDICATION	iii
	ACKNOWLEDGEMENT	iv
	ABSTRACT	v
	ABSTRAK	vi
	TABLE OF CONTENTS	vii
	LIST OF TABLES	X
	LIST OF FIGURES	xi
	LIST OF ABBREVIATIONS	xiii
	LIST OF SYMBOLS	xiv
1	INTRODUCTION	1
	1.1 Introduction	1
	1.2 Problem statement	3
	1.3 Objectives	3
	1.4 Scope of work	4
2	LITERATURE REVIEW	5
	2.1 Introduction	5
	2.2 Self-compacting concrete	6
	2.2.1 Background and practical applications of SCC	6
	2.2.2 Characteristics of SCC	9
	2.2.3 Factors affecting self-compactibility of	10
	SCC	
	2.2.4 Mechanical properties of hardened SCC	14
	2.2.4 Physical properties	15

	2.2.6	Advantages of SCC	16
	2.3 Sto	eel fibre reinforced concrete	18
	2.3.1	Advantages of SFRC	18
	2.3.2	Type of SFRC	19
	2.3.3	Mechanical properties of SFRC	20
	2.3.4	Structural performance of SFRC	24
	2.3.4	Application of SFRC	25
	2.4 Sto	eel fibre self-compacting concrete	25
	(S	FSCC)	
	2.4.1	Previous research on SFSCC	25
	2.5 Fi	nite element method (FEM)	28
	2.5.1	Introduction to FEM	29
	2.5.2	Type of FE analysis	29
	2.5.3	Advantages of FEM	30
	2.5.4	Previous research on FEM	30
	2.6 Cri	tical summary	35
3	<b>METH</b>	ODOLOGY	36
	3.1 Int	troduction	36
	3.2 Int	troduction to LUSAS software	38
	3.3 As	ssumptions in modelling	38
	3.4 La	boratory test configuration	39
	3.5 Fi	nite element modelling	41
	3.5.1	Pre-processing: Construction of	41
		geometric model	
	3.5.2	Conversion of geometric model to finite	43
		element model	
	3.5.3	Material property data representation	44
	3.5.4	Defining the boundary condition	46
	3.5.5	Loading configuration	47
	3.6 No	onlinear analysis	48
	3.7 Su	ımmary	50

4	RES	SULTS AND DISCUSSION	51
	4.1	Introduction	52
	4.2	Load-deflection relationship	52
	4.3	Ultimate shear capacity	53
	4.4	Mode of failure and cracking pattern	55
	4.5	Summary	58
5	CO	NCLUSION AND RECOMMENDATION	59
	5.1	Conclusion	59
	5.2	Recommendation	60
REFERENCES			61
Appendix A			65

# LIST OF TABLES

TABLE	TITLE	PAGE
2.1	Acceptance criteria for self-compacting concrete	9
2.2	The composition of the specimens	26
2.3	The specification of steel fibres	26
2.4	Summary of the beam experiments	27
3.1	Concrete material properties	44
3.2	Reinforcement material properties	45
3.3	Summary of FEA attribute	50
4.1	Comparison of ultimate shear capacity	55

# LIST OF FIGURES

FIGURE	TITLE	PAGE
2.1	Utilisation of SCC in Japan	7
2.2	Location of mega column in World Financial Centre, Shanghai	8
2.3	Method to achieve self-compactibility	10
2.4	Relationship of coarse aggregate content and self-compactibility	11
2.5	Relationship between mortar's flow-ability and self- compactibility of	
	concrete	12
2.6	Normal stress generated in mortar due to approaching coarse aggregate	
	particles	12
2.7	A simple evaluation method for stress transferability of fresh mortar	13
2.8	Relationship between fine aggregate content in mortar and Rcs/Rm	13
2.9	Cube compressive strength vs. equivalent water/cement ratio	14
2.10	Modulus of elasticity vs. compressive strength	15
2.11	Flowability of SCC	17
2.12	Types and notations of steel fibres	19
2.13	Stress-strain curve for plain concrete & SFRC	20
2.14	Influence of fibre content on tensile strength	21
2.15	The effect of weight percent of fibre on the flexural strength of mortar and	
	concrete	22
2.16	The effect of Wl/d on the Flexural toughness	22
2.17	Modified JSCE-SF6 test set up	27
2.18	Typical crack pattern for beam experiment	28
2.19	Typical elements and nodes in FEM.	29
2.20	Finite element model	31
2 21	The model of test beam	32

2.22	The cracks on tst beam	32
2.23	SF-2 load-deflection curve	34
2.24	SF-3 load-deflection curve	34
3.1	Workframe overview	37
3.2	Schematic diagram for the shear test	39
3.3	Shear test setup	40
3.4	Reinforcement detailing for shear test specimens	40
3.5	Geometric model for B-SFSCC250	41
3.6	Geometric model for B-NC125, B-SCC125 and B-SFSCC125	41
3.7	LUSAS interface for geometric line definition.	42
3.8	LUSAS interface for geometric surface definition.	42
3.9	LUSAS interface for assigning the mesh to the line attribute	43
3.10	LUSAS interface for assigning the mesh to the surface attribute	44
3.11	LUSAS interface for assigning the properties of isotropic concrete	45
3.12	LUSAS interface for assigning the properties of isotropic reinforcement	46
3.13	LUSAS interface for assigning the support condition	47
3.14	LUSAS interface for assigning the load.	48
3.15	LUSAS interface for assigning nonlinear and transient analysis	49
3.16	LUSAS interface to define nonlinear and transient analysis	49
4.1	Load-Deflection Curve	53
4.2	Cracking behaviour of the beams in Lusas	56
4.3	Actual cracking pattern in the experiment	57

# LIST OF ABBREVIATIONS

RC - Reinforced Concrete

NC - Normal Concrete

SCC - Self Compacting Concrete

SFSCC - Steel Fibre Self Compacting Concrete

FEA - Finite Element Analysis

FEM - Finite Element Method

LUSAS - London University Structural Analysis System

# LIST OF SYMBOLS

As - Area of main steel reinforcement

 $A_{sv}$  - Area of links

E - Modulus of elasticity

V<sub>ult</sub> - Ultimate shear capacity

V<sub>f</sub> Fibre volume fraction

V<sub>fd</sub> - Shear contribution from steel fibres

V<sub>wd</sub> - Shear resistance provided by shear reinforcement

V<sub>Rd,c</sub> - Shear resistance of concrete

 $f_y \qquad \text{-} \qquad Yield \ strength$ 

#### **CHAPTER 1**

#### INTRODUCTION

## 1.1 Introduction

Concrete has high compressive strength but weak in tension. Thus, it is commonly reinforced with material that is strong in tension such as steel. Over the years, reinforcement solutions to plain concrete in the form of steel bar have been studied in many types of research and applications. Reinforced concrete structures consist of a series of individual members that are interconnected to support the load imposed on them. A complete building can comprise the structural elements such as beams, slabs, columns, walls, foundations and stairs. This study focused on the behaviour of the reinforced concrete beam when subjected to the load. Reinforced concrete beam is a structural member that commonly used in the reinforced concrete structure and particularly in precast structures. Generally, a beam is horizontal members carrying lateral loads. Due to lower tensile strength of concrete, the shear strength of beams can be improved with an addition of steel fibres (SF) in the concrete mix to produce Steel Fibre Reinforced Concrete (SFRC). According to its application, fiber volume percentage and fiber effectiveness, the behaviour of SFRC can be classified into three group; i) very low volume fraction of SF (less than 1% per volume of concrete), ii) moderate volume fraction of SF (1% to 2%), and iii) high volume fraction of SF (more than 2%). Furthermore, steel fibre is one of the

materials that are strong in tension which can cooperate with the concrete to improve their strength.

However, with the addition of steel fibre, the workability of concrete will decrease. Further to this, the SCC mixes need a proper proportioning method since steel fibres are reported to affect the shear yield stress and viscosity of fresh SCC. Steel Fibre Self-Compacting Concrete (SFSCC) is recent hybrid materials that collectively combine these two concrete types. The combination of SCC and SFRC contribute to superior behaviour in the fresh and hardened state respectively. With an improvement in flowability of concrete, SFSCC allows the concrete to be poured easily and partially replace the traditional reinforcement bars. In fact, if the amount of fibres that being introduced to the concrete is sufficiently high, the shear capacity of SFSCC structure can be improved. Due to its ability to redistribute the stresses and to bridge cracks with an improvement of the post-cracking behaviour and other mechanical performance, SFSCC becomes a common alternative in both conventional reinforced concrete and precast concrete industry.

The work presented in this study aims to examine the shear behaviour of SFSCC reinforced concrete beam using non-linear finite element method. To describe the non-linear behaviour of the beam, the effect of steel fibres is directly modelled into the existing parameter of concrete that has been reported by previous research. Finite element method is a powerful mathematical tool to analyse the structure. It is proved to be effective in structural engineering where the critical analysis with accuracy is an important parameter. In order to construct a mathematical model for this analysis, the parameter of the beam needs to be identified as they may influence the behaviour of the structure. The parameters could be material and geometric properties of the structure, support conditions and applied loads. In this study, models are generated using LUSAS Software as a tool. This study focused on an application of finite element method of analysis for reinforced concrete beams considering the different type of concrete; Normal Concrete (NC), Self Compacting Concrete (SCC) and Steel Fibre Self Compacting Concrete (SFSCC). The structural behaviour is observed and compared with experimental and theoretical calculation.

## 1.2 Problem statement

A significant number of studies have been conducted on the shear strengthening of RC beams with an addition of steel fibre in the concrete mix. However, most of these studies have been experimentally based and only few researches are available on the numerical modelling of such beams using the finite element method. The lack of in-depth finite element studies is mostly due to the challenging nature of modelling shear cracking in SFSCC beams and the interfaces between different materials. As consequences of lacking in numerical analysis of SFSCC beams, the purpose of the numerical simulation is to verify the experimental result as well as to avoid tedious experimental work of subjecting the structure to numerous fractures in future research. Besides, due to the high cost required to run the experiment, the finite element can be an option to study the shear behaviour of the beams. Thus, in future research, the time and money can be saved.

## 1.3 Objectives

There are four objectives that need to be assessed in this study. These are:

- To distinguish the different properties between NC beam, SCC beam and SFSCC beam in term of mechanical properties based on the experimental test that has been conducted from the previous research.
- ii. To develop the 2D model of NC beam, SCC beam and SFSCC beam using nonlinear finite element analysis.
- iii. To analysis the structural behaviours of the beam in terms of shear resistances, deformations and cracking patterns.
- iv. To compare the result from finite element analysis with experimental and theoretical calculation.

## 1.4 Scope of work

The models of the reinforced concrete beams were developed by using finite element method to observe and simulate the behaviour of the reinforced concrete beam in term of failure mode, the relationship between shear and deflection and the strain in concrete and steel. The properties for design purpose such as tensile strength, compressive strength and flexural strength are adopted from the previous study. The reinforced concrete beam models were analysed by using LUSAS software. For design purpose, the models were assumed to be limited to 2-dimension analysis modelling and the materials for precast concrete corbel were limited to normal concrete (NC), self-compacting concrete (SCC) and steel fibre self-compacting concrete (SFSCC).

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