

DAMAGE MECHANICS BASED APPROACH IN FAILURE PREDICTION OF  
DRAW FORMING PROCESSES

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## **DEDICATION**

To my beloved parents and family

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## ABSTRACT

In a cup draw forming operation, the desired shape results from the material hardening process under controlled plastic deformation and the springback phenomena. In this study, a mechanics-of-deformation approach is developed based on damage variables and large plastic deformation. The approach is then employed to estimate the onset of the material damage event and the location of fracture based on the mechanics response of the metal blank. Draw forming behavior of low carbon steel is examined as a case study. The loading rate is conducted at a slow loading response of the steels in the large deformation of the draw forming processes. Axisymmetric and 3D solid models are developed for finite element (FE) simulations to gain insight into the evolution of internal states and damage in the steel blanks during the draw forming process. In the FE simulation, Johnson-Cook constitutive model with isotropic hardening rule is employed. The Rice-Tracey ductile damage criterion is employed to indicate damage initiation event along with a linear energy-displacement relation for damage evolution rule. Results show that while the applied loading (tool displacement) is quasi-static corresponding to the strain rate of  $0.001 \text{ sec}^{-1}$ , the maximum plastic strain rate at fracture could reach 100 times greater at the critical material flow region. Failure of the deforming steel blank is localized with excessive plastic deformation. While the onset of damage can be efficiently predicted using the axisymmetric FE model with damage-based model, the subsequent damage evolution of the localized ductile failure requires a 3D continuum FE model. The predicted tool load-displacement response is employed in validating the FE model. Effects of drawing parameters including drawing speed, blank holder force and die clearance on the resulting deformation of the drawn cup-shape part are established. Based on the response of the mechanics-of-deformation, the established failure prediction approach is proven more accurate and reliable.

## ABSTRAK

Di dalam operasi pembentukan cawan, bentuk yang diinginkan terhasil daripada proses pengerasan bahan di bawah fenomena tindakan ubah bentuk plastik dan anjalan. Di dalam kajian ini, kaedah mekanik ubah bentuk dibangunkan berdasarkan pemboleh ubah kerosakan dan ubah bentuk besar plastik. Kaedah ini kemudiannya diguna pakai bagi menganggarkan permulaan kejadian kerosakan bahan serta lokasi retakan berdasarkan tindak balas mekanik kepingan logam kosong. Sifat pembentukan keluli berkarbon rendah adalah dikaji sebagai satu kajian kes. Muatan ke besi dikenakan pada kadar tindak balas perlahan mengakibatkan perubahan besar dalam proses penghasilan pembentukan. Model asimetrik dan model pepejal 3D dibangunkan untuk simulasi unsur terhingga bagi mendapatkan pemahaman evolusi keadaan dalaman dan kerosakan logam kosong semasa proses pembentukan tarikan. Di dalam simulasi unsur terhingga, model menjuzuk Johnson-Cook bersama dengan peraturan pengerasan isotrop adalah diguna pakai. Kriteria kerosakan mulur Rice-Tracey digunakan bagi menunjukkan kejadian permulaan kerosakan berserta hubungan linear tenaga dan sesaran untuk peraturan evolusi kerosakan. Hasil menunjukkan walaupun laju alat yang dikenakan adalah pada kuasi-statik menurut kadar terikan  $0.001\text{saat}^{-1}$ , kadar terikan retakan plastik tertinggi boleh mencecah 100 kali ganda di kawasan genting pengaliran bahan. Kerosakan oleh perubahan logam kosong ditempatkan dengan lebihan ubah bentuk plastik. Sementara itu permulaan kerosakan boleh di jangka dengan berkesan menggunakan model simulasi unsur terhingga asimetrik menggunakan model berasaskan model kerosakan, evolusi kerosakan seterusnya adalah kerosakan mulur setempat memerlukan model unsur terhingga 3D. Jangkaan respon beban kepada sesaran digunakan bagi mengesahkan model simulasi unsur terhingga. Kesan parameter penarikan termasuk kelajuan penarikan, daya pemegang logam kosong dan kelegaannya acuan tekan pada hasil ubah bentuk oleh tertarik berbentuk cawan adalah tertubuh. Berdasarkan respon mekanik ubah bentuk, pendekatan jangkaan kerosakan tertubuh dibuktikan lebih tepat dan yakin.

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## LIST OF ABBREVIATIONS

|      |   |                                   |
|------|---|-----------------------------------|
| AHSS | - | Advance High Strength Steel       |
| BHF  | - | Blank Holder Force                |
| CAE  | - | Computer Aided Engineering        |
| CDM  | - | Continuum Damage Mechanics        |
| Cof  | - | Coefficient of friction           |
| C-S  | - | Cowper- Symonds                   |
| DC   | - | Die Clearance                     |
| DIC  | - | Digital Image Correlation         |
| FE   | - | Finite Element                    |
| FFL  | - | Fracture Forming Limit            |
| FLC  | - | Forming Limit Curve               |
| FLD  | - | Forming Limit Diagram             |
| FLDF | - | Forming Limit Diagram at Fracture |
| FLDN | - | Forming Limit Diagram at Necking  |
| GTN  | - | Gurson–Tvergaard–Needleman        |
| HER  | - | Hole Expansion Ratio              |
| J-C  | - | Johnson-Cook                      |
| LCS  | - | Low Carbon Steel                  |
| LDH  | - | Limiting Dome Height              |
| LDR  | - | Limiting Drawing Ratio            |
| R-K  | - | Rusineck-Klapeczko                |
| RVE  | - | Representative Volume Element     |
| SEM  | - | Scanning Electron Microscope      |
| TM   | - | Tanimura-Mimura                   |
| Z-A  | - | Zerilli-Armstrong                 |

## LIST OF SYMBOLS

|                |   |  |
|----------------|---|--|
| $A$            | - | Area   |
| $A'$           | - | Johnson-Cook material constant                                 |
| $a$            | - | Material damage initiation parameters                          |
| $B'$           | - | Johnson-Cook strain hardening coefficient                      |
| $C'$           | - | Johnson-Cook strain rate sensitivity                           |
| $c$            | - | Material damage initiation parameters                          |
| $D$            | - | Damage variable  |
| $\dot{D}$      | - | Material constant  |
| $d$            | - | Drawing depth  |
| $d_i$          | - | Damage initiated   |
| $d_L$          | - | Drawing limit  |
| $d_{max}$      | - | Maximum drawing depth  |
| $dA$           | - | Change of area   |
| $dF$           | - | Change of loading force  |
| $d\sigma$      | - | Change of stress   |
| $d\varepsilon$ | - | Change of strain   |
| $E$            | - | Young's modulus  |
| $E_o$          | - | Young's modulus of the material in the initial undamaged state |
| $E_D$          | - | Damaged state after loading                                    |
| $F$            | - | Force  |
| $F_{max}$      | - | Maximum force  |
| $F_L$          | - | Limit punch force  |
| $G_f$          | - | Fracture energy  |
| $L$            | - | Characteristic length of the element                           |
| $m$            | - | Johnson-Cook temperature sensitivity                           |



|                            |   |   |
|----------------------------|---|---|
| $n$                        | - | Johnson-Cook strain hardening                                 |
| $T^*$                      | - | Johnson-Cook homologous temperature                           |
| $T_{melt}$                 | - | Melting temperature   |
| $T_{room}$                 | - | Room temperature  |
| $t$                        | - | Thickness   |
| $t_{blank}$                | - | Thickness of the blank  |
| $\bar{u}^{pl}$             | - | Equivalent plastic displacement                               |
| $\bar{u}_f^{pl}$           | - | Equivalent plastic displacement at failure (damage evolution) |
| $\nu$                      | - | Poisson's ratio   |
| $\omega_D$                 | - | Internal state variable                                       |
| $\Delta A$                 | - | Apparent area (undamaged surface)                             |
| $\Delta \tilde{A}$         | - | Changes the effective area                                    |
| $\Delta A_{void}$          | - | Area with micro-voids   |
| $\Delta F$                 | - | External loading force  |
| $\bar{\sigma}$             | - | Equivalent stress   |
| $\tilde{\sigma}$           | - | Effective stress  |
| $\sigma_m$                 | - | Mean stress   |
| $\sigma_y$                 | - | Yield stress  |
| $\sigma_{yo}$              | - | Value of yield stress when damage criterion is met            |
| $\varepsilon$              | - | Strain  |
| $\dot{\varepsilon}$        | - | Strain rate   |
| $\dot{\varepsilon}^*$      | - | Johnson-Cook dimensionless strain rate                        |
| $\dot{\varepsilon}_0$      | - | Johnson-Cook nominal strain rate                              |
| $\varepsilon_D^{pl}$       | - | Effective plastic strain at the damage initiation             |
| $\bar{\varepsilon}^{pl}$   | - | Equivalent plastic strain                                     |
| $\bar{\varepsilon}_0^{pl}$ | - | Effective plastic strain at the damage initiation             |
| $\bar{\varepsilon}_f^{pl}$ | - | Effective plastic strain at fracture                          |
| $\bar{\varepsilon}_D^p$    | - | Plastic strain rate at the onset of damage                    |

|                             |   |   |
|-----------------------------|---|---|
| $\dot{\bar{\epsilon}}^{pl}$ | - | Equivalent plastic strain during the damage evolution stage |
| $\eta$                      | - | Stress triaxiality  |
| $\rho$                      | - | Material density  |

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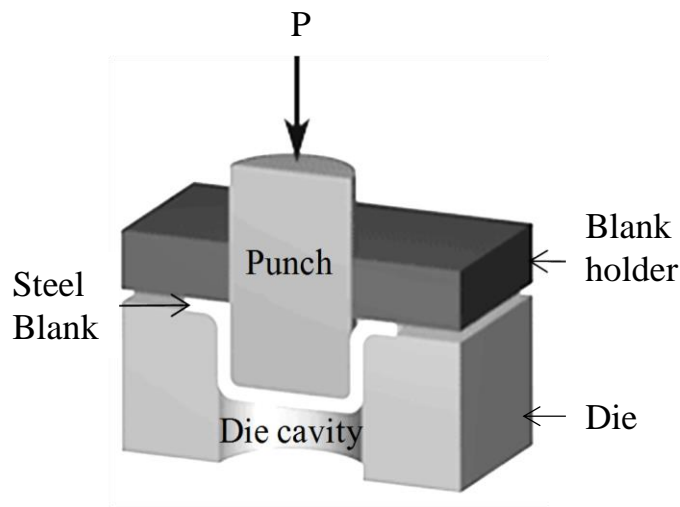
## **CHAPTER 1**

### **INTRODUCTION**

#### **1.1 Background of Study**

Automotive body parts such as front quarter panel, suspension housing and floor panel are produced through numerous metal forming processes. It is a process of governing the formability of material into the desired shape throughout the forming operation without fail [1]. In the classical shop floor approach, the well-known forming limit diagram (FLD) is employed as a tool to predict the material failure in the metal forming operation. It is practiced as an approach to prevent the occurrence of fracture in sheet metal forming production.

In general, metal forming operation is divided into two main distinct processes, which are cutting and shaping. The process of cutting such as blanking is a process of separating the blank. While shaping for instance draw forming is to form the blank into desired parts. As the main shaping metal forming process in the automotive industries, the study of material failure concentrates on the draw forming operation. The typical tool and die movement are described thru the mechanism of the draw forming process. The tool consists of a punch, blank holder and die cavity while steel blank is employed as deformable parts as depicted in Figure 1.1. This monotonic loading process of punch draws the steel blank into the die cavity at a specified drawing depth and loading speed to draw forming shaped parts. The interactions between deformable blank and forming tools induced large plastic deformation until it is properly form into desired shape.



**Figure 0.1:** Cross sectional view of typical cup draw forming process

During the draw forming operation, steel blank undergoes material hardening process under controlled plastic deformation and springback phenomena. As a result, variation of thickness strain induced by the large plastic deformation is detected in the draw-forming cup. The blank holder force (BHF) induces the compressive stress at the flange region, while the punch tool induces the longitudinal and radial stresses throughout the loading process into the die cavity. These excessive stresses can cause the material failure known as wrinkling and localized necking. Wrinkling at flange is local buckling phenomena that attribute to the excessive compressive stresses [2]. Whereas, localized necking is due to the excessive tensile stresses [3]. The localized necking is usually detected in the sidewall region that can lead to ductile fracture.

As commonly practiced by the shop floor, the popular conventional FLD is defines as a linear strain path dependent criteria [4]. Thus, it is inaccurate for the analysis of complex draw forming processes [5]. The proposed approach is to use the internal states change of steel blank during draw forming processes. It is a mechanics of deformation approach. A process of degradation of material strength properties that initiate and evolve until fracture is dictated [6]. The failure prediction approach is developing based on the Rice-Tracey (R-T) ductile damage criterion to indicate the damage initiation event. While the linear energy-based relation, is used for damage evolution rule. The employ damage variables can estimate the localized deformation and tolerable stretching of material throughout the degradation process of material.

This mechanics of deformation approach is employed as a remedy to the problem in material failure prediction. The mechanics of deformation is a branch of mechanics that examines the behavior of material to the loading. It is an effort of investigating the non-linear response in the material due to the changes in geometry and internal state behavior throughout the draw forming operation.

## **1.2 Statement of the Research Problem**

How could the mechanics of deformation approach employing damage model and finite element (FE) simulation be used to predict material failure process in draw forming operation.

## **1.3 Objectives**

The aim of this study is to develop a damage-based failure prediction approach on the mechanics of materials deformation. Specific objectives are:

1. To establish a validated framework for FE simulation of draw forming processes.
2. To quantify the limitation of axisymmetric FE model for fracture.
3. To determine the effect of damage and its evolution on the material response.

## 1.4 Scope of Study

The present study covers the following scope of work:

1. Low carbon steel (LCS) is examined as a demonstrator material.
2. Erichsen cup forming machine is used to draw forming LCS into circular cup shape parts.
3. The draw forming test is set at 1 mm/sec slow loading rates with constant BHF to clamp uniformly on the flange part.
4. The FE simulations are carried out at strain rate dependent condition to model the draw forming test.
5. Coulomb friction is applied in every interaction between forming tools and deformable blank throughout the FE simulation.
6. Axisymmetric model with piecewise hardening curve is applied to define the limitation of the geometrical representation of the model when predicting failure.
7. Deformable blank in FE 3D circular cup is modeled using solid elements to determine the thru thickness necking effect.
8. Johnson-Cook (J-C) isotropic hardening parameter incorporated with Rice-Tracey (R-T) ductile damage initiation model and linear energy based model are used to assess hardening and material failure respectively.

## 1.5 Significance of Study

In predicting material failure, FLD shows some disadvantageous which requires new approach. Compared to the propose approach, its failure prediction quality is considered as inaccurate for the complex analysis of draw forming processes. This is due to its criteria that satisfy only for the linear strain path condition. Furthermore, it is highly depending on the recorded experimental test data with less mechanics based consideration. It is also very time consuming because it requires too

many data to be recorded with too many samples involved. As a result, these works suffered high in cost.

On the other hand, the propose failure prediction approach not only able to predict the onset of failure location accurately. Moreover, it is able to quantify the internal states of material from the process of thru thickness necking throughout the damage evolution until fracture. Therefore, the failure prediction results are more realistic compared to classical shop floor approach.

With the advance in numerical simulation to compute virtually the draw forming processes, the propose approach facilitates the assessment of deformation and failure. It computes the mechanics of deformation throughout the formability of material until the point of separation. Thru the understandings on mechanics of deformation and failure processes, the behavior of tolerable stretching of the material are define explicitly. It gives accurate and realistic physical representation of ductile failure at a localized point in the material.

## **1.6 Thesis Layout**

This thesis consists of seven chapters. In Chapter 1, the background and the necessity of the background of the research are bringing out. The issues of material failure in drawing automotive steel parts are based upon. The objectives, scope and significance of the research are present.

In Chapter 2, reviews are presented on the trends in sheet metal forming processes, automotive steel sheet, formability of draw forming processes, mechanics of large plastic deformation, finite element, strain rate dependent models, continuum damage mechanics, mechanism of failure, FE simulation of sheet metal forming processes and summary of literature review.



In Chapter 3, the research methodology is present. The details of the applied research materials, experimental setup and finite element (FE) simulation models are explained.

In Chapter 4, the assessment of deformation and failure processes in draw forming test are presented and discussed. Mechanics deformation of material formability through the punch-force displacement curve is examined and interpreted. Effects of BHF and DC setting in the process are measured. The interrupted draw forming tests at different displacement depth are conducted. The evolution of plastic instability in the interrupted draw-forming test is characterized. Fracture location and failure mechanism is identified.

In Chapter 5, the application of FE simulation to assess the mechanics deformation is addressed. An axisymmetric FE cup draw-forming model is used to simulate the draw forming processes on LCS at uniform BHF. In modeling the hardening behavior, piecewise plastic strain rate hardening parameter are employed. The evolution of plastic instability in the interrupted draw forming simulation is characterized. The calculated fracture location is compared.

In Chapter 6, the application of FE simulation to assess the damage mechanics is address. Using 3D FE cup model, the damage mechanics are examined by incorporating the J-C strain rate dependent criteria and damage variables until the event of fracture. The calculated localized thinning is characterized and compared. The fracture location in 3D FE cup model is demonstrated.

In Chapter 7, the major conclusions of the research are present. Future works for refining the research are recommend.

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