

SIMULATION METHODOLOGY FOR FRACTURE PROCESSES OF
COMPOSITE LAMINATES USING DAMAGE-BASED MODELS

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To my beloved

Prof. Mohd Nasir, Dad and Mom, my wonderful wife Atefeh, my brother Mustafa,
and my sisters Maryam and Masoomeh.

To my friends for their endless love and supports...

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ABSTRACT

Fiber-reinforced polymer composite (FRP) laminates have found increasing use in advanced industrial applications. However, the limited knowledge and validated material models of the failure processes of the laminated composites continue to pose challenges in ensuring reliability and integrity of the structures. This research aims at establishing a validated simulation methodology for fracture assessment of FRP composite laminates. The approach accounts for the failure processes and the associated damage mechanisms through finite element (FE) simulations. The FE model development considers the existence of the physical interfaces between the laminae due to the manufacturing processes. A hybrid experimental-computational approach is developed for systematic implementation of the simulation methodology. Different combinations of the failure modes were observed, including matrix cracking-crushing, fiber/matrix interface debonding, interface multi-delamination, and fiber fracture-buckling. Local material failure is modeled by a damage initiation event followed by the evolution of the damage to fracture. Two types of damage-based models are investigated; the continuum damage model encompassing the multi-damage criteria for the FRP composite lamina and the cohesive zone model for interface delamination. A full derivation of the continuum damage model for the anisotropic material is given and employed for prediction of the damage evolution in the lamina. A series of experiments on CFRP and GFRP composite laminate specimens are conducted to establish the flexural and fracture behaviors of the materials. Complementary 3D FE models of the specimens and test setups are developed. Two different FE-based models, namely the *conventional* and *Prepreg* model, are developed and examined for GFRP and CFRP composites. Results show that accurate prediction of elastic-damage behavior and the progressive damage process in FRP composites depend on the chosen FE-based model of the FRP composite laminates and the damage-based material model used. The flexural test of a 12-ply antisymmetric CFRP composite beam specimen under four-point bending displayed the occurrence of multiple failure events. These include matrix cracking at lamina No. 9 (90°), and delamination at interfaces No. 8 ($-45^\circ/90^\circ$) and No. 9 ($90^\circ/45^\circ$). In addition, intralaminar multi-failure events are predicted in lamina No. 1 (-45°) due to matrix shear and fiber buckling failures. FE simulation of the test predicted an accurate flexural response with less than 4% average error when compared with measured data, along with similar multiple failure zones in the specimen. Damage dissipation energy is used to illustrate the quantity of the overall progressive damage in FRP laminae, interfaces and the laminated composite. The simultaneous use of lamina and interface damage models in the FE simulation of the FRP composite laminate is recommended in view of the occurrence of multiple intralaminar-interlaminar failure modes and fractures under general loading conditions.

ABSTRAK

Penggunaan laminat komposit polimer bertetulang gentian (FRP) dalam industri termaju didapati telah meningkat. Walau bagaimanapun, pengetahuan yang terhad dan model bahan tervalidasi untuk proses kegagalan laminat komposit tersebut terus memberi cabaran dalam memastikan kebolehharapan dan integriti sesuatu struktur. Kajian ini bertujuan untuk menghasilkan suatu metodologi simulasi tervalidasi bagi penilaian patah laminat komposit FRP. Pendekatan ini mengambil kira proses kegagalan dan mekanisme kerosakan yang berkaitan melalui simulasi unsur terhingga (FE). Pembangunan model FE mengambil kira kewujudan lapisan fizikal di antara lamina-lamina yang terhasil dari proses pembuatan. Suatu pendekatan eksperimen-komputeraan hibrid dibangunkan untuk pelaksanaan metodologi simulasi yang sistematik. Gabungan mod kegagalan yang berbeza telah diperhatikan termasuk retak-hancur matrik, lekangan gentian/matrik, berbilang lekangan antara-muka dan ledingann-patah gentian. Kegagalan setempat bahan dimodel oleh kejadian kerosakan permulaan dan diikuti oleh evolusi kerosakan sehingga patah. Dua jenis model berasaskan kerosakan telah disiasat; model kerosakan kontinum yang merangkumi kriteria pelbagai kerosakan untuk lamina komposit FRP dan model zon kohesif untuk lekangan antara-muka. Suatu terbitan penuh model kerosakan kontinum untuk bahan anisotropik telah disediakan dan diguna pakai untuk ramalan evolusi kerosakan dalam lamina. Suatu siri eksperimen ke atas spesimen laminat komposit CFRP dan GFRP telah dijalankan untuk mewujudkan gaya laku lenturan dan patah bahan. Model pelengkap FE 3D untuk spesimen dan tentuatur ujian telah dibangunkan. Dua model FE yang berbeza; iaitu model *conventional* dan *prepreg* telah dibangunkan dan diteliti untuk komposit GFRP dan CFRP. Keputusannya menunjukkan bahawa ramalan tepat kelakuan anjal-rosak dan proses kerosakan yang progresif dalam komposit FRP bergantung kepada model FE yang dipilih untuk laminat komposit FRP tersebut dan model berasaskan kerosakan yang diguna pakai. Ujian lenturan ke atas specimen rasuk komposit CFRP 12-lapis yang antisimetri di bawah beban titik-empat lenturan menunjukkan berlakunya kejadian pelbagai kegagalan. Ini termasuk keretakan matrik pada lamina No. 9 (90°), dan lekangan pada antara-muka No. 8 ($-45^\circ/90^\circ$) dan No. 9 ($90^\circ/45^\circ$). Tambahan lagi, kejadian pelbagai kegagalan dalam-lamina diramal berlaku dalam lamina No.1 (-45°) disebabkan oleh ricih matrik dan kegagalan ledingan gentian. Simulasi FE ujian tersebut meramalkan respon lenturan yang tepat dengan ralat purata kurang daripada 4% berbanding dengan data yang diukur, berserta zon kegagalan yang serupa di dalam specimen. Tenaga pelepasan rosak boleh digunakan untuk menggambarkan kuantiti keseluruhan proses kerosakan yang progresif dalam lamina-lamina FRP, antara-muka dan laminat komposit. Penggunaan serentak model kerosakan lamina dan antara-muka dalam simulasi FE bagi laminat komposit FRP adalah disyorkan memandangkan boleh berlakunya pelbagai mod kegagalan dalam-lamina/antara-lamina dan keretakan di bawah keadaan pembebanan umum.

TABLE OF CONTENTS

CHAPTER	TITLE	PAGE
	DECLARATION	ii
	DEDICTAION	iii
	ACKNOWLEDGEMENTS	iv
	ABSTRACT	vi
	ABSTRAK	vii
	TABLE OF CONTENT	viii
	LIST OF TABLES	xv
	LIST OF FIGURES	xvi
	LIST OF ABBREVIATIONS	xxviii
	LIST OF SYMBOLS	xxx
	LIST OF TERMINOLOGIES	xxxiv
	LIST OF APPENDICES	xxxv
1	INTRODUCTION	1
	1.1 Introduction	1
	1.2 Problem Background and Rationale	2
	1.3 Statement of the Research Problem	6
	1.4 Research Questions	6
	1.5 Objectives of Study	6
	1.6 Scope of Study	7
	1.7 Layout of the Thesis	9
2	LITRTURE REVIEW	12
	2.1 Composite Materials Definition	12

2.2	Physical Identification of FRP Laminate Composites for Analysis and Failure Aspects	14
2.2.1	A General View of Failure Modes in Composite Materials	16
2.3	Advanced Applications of FRP Composite Materials	17
2.4	Manufacturing Process of FRP Composite Materials	21
2.4.1	Prepreg/Autoclave Manufacturing Process	22
2.4.2	Vacuum Infusion Manufacturing Process	23
2.4.3	Manufacturing Issue and Modeling of FRP laminated Composites	24
2.5	FE Method and Simulation Practices in FRP Laminated Composites	26
2.6	Mechanics of Composite Materials	27
2.7	Damage Mechanism of Composite Laminates	30
2.8	Continuum Damage Mechanics	32
2.8.1	Damage Mechanics-based Models	33
2.8.2	Mechanical Representation of Damage	35
2.8.3	Continuum Damage Mechanics and FRP Laminate Composites	38
2.9	Failure of FRP Laminate Composites	39
2.9.1	Damage Modes and Failure Criteria of FRP Lamina	39
2.9.2	Progressive FRP Lamina Damage Process	45
2.9.3	Interlaminar Damage Evolution of FRP Laminate Composite	46
2.9.4	Multiple Damage and Fracture of FRP Laminate Composite	48
2.10	Summary of the Literature Review and Outlines	50
3	RESEARCH METHODOLOGY	53
3.1	Introduction	53
3.2	Research Framework	54
3.3	Specimen Design and Experiment for Failure Study of	

FRP Composites	57
3.3.1 Specially-Designed Experiment for FRP Laminate Composites	57
3.3.2 Fractographic Analysis	63
3.4 Physical Simulation of FRP Composite Materials	63
3.5 Finite Element Simulation of FRP Laminated Composites	64
3.5.1 FRP Composite Manufacturing Issue and FE Model-based Construction	68
3.6 FE Mesh Configuration of FRP Composite System and Mesh Convergence Study	74
3.7 Hybrid Experimental-Computational Approach, and Validation of the FE Models	79
3.8 Layout of the FE Models and Experiments	82
3.9 Summary of the Research Methodology and Outlines	83
4 THEORETICAL BACKGROUND OF CONTINUUM DAMAGE MODELS OF FRP COMPOSITE LAMINATES	85
4.1 Introduction	85
4.2 Constitutive Model of Anisotropic Damage in FRP Laminated Composites	87
4.2.1 Orthotropic Behavior of FRP Lamina	89
4.2.2 Damage Initiation Criteria	91
4.2.3 Post-Damage Initiation Model and Concept	96
4.2.3.1 Equivalent Elastic Constitutive Behavior of Anisotropic Material for Prediction of Stress Level of Damage Initiation Criteria	109
4.2.4 Softening Behavior and Damage Evolution of Anisotropic Materials	113
4.2.5 Multiple Constitutive Models of Anisotropic FRP Lamina	121
4.3 Physically-based Model of Interface Failure in FRP	

Composites	125
4.3.1 A Constitutive Motion-Based Model to Relate Nodes Contact in Plies Interfaces	126
4.3.2 Continuum Theory of Cohesive Zone Model	128
4.3.2.1 Mixed-Mode Interface Damage Initiation	132
4.3.2.2 Mixed-Mode Interface Damage Propagation	134
4.3.2.3 Constitutive Equation for Mixed-Mode Behavior	136
4.3.3 Preliminary FE Modeling of Interface for FRP Composite Laminates	137
4.4 Internal Energy Terms	140
4.5 Summary and Outlines	145
5	
MECHANICAL RESPONSE AND MULTI-DAMAGE PROCESSES OF FRP COMPOSITE LAMINATES MANUFACTURED USING VIP AND PREPREG/AUTOCLAVE METHODS	147
5.1 Introduction	147
5.2 Materials and Experimental Procedures	148
5.3 Finite Element Modeling	150
5.4 Results and Discussion	152
5.4.1 Mechanical Response and Failure Process of Prepreg CFRP Composite Laminates	153
5.4.1.1 Structural Response and Fractographic Study Aspects	153
5.4.1.2 Mesh Convergence Study Aspect	155
5.4.1.3 Validation of FE Simulation Process	158
5.4.1.4 Critical Structural Deformation	160
5.4.1.5 Matrix Damage Initiation Process	162
5.4.1.6 Variation of Critical Stresses	164
5.4.1.7 Progressive Matrix Damage Process	173
5.4.1.8 Progressive Fiber Damage Process	178

5.4.1.9	Assessment of Critical Energy Terms	181
5.4.2	Mechanical Response of GFRP Composite Manufactured by Vacuum Infusion Process	185
5.4.2.1	Structural Response and Validation of FE Simulation Process	185
5.4.2.2	Assessment of Critical Strain and Stress Parameters	186
5.4.2.3	Progressive Damage Process and Assessment of Critical Energy Terms	188
5.5	Summary and Outlines	192
6	INTERLAMINAR DAMAGE AND FRACTURE PROCESSES OF CFRP COMPOSITE LAMINATES	193
6.1	Introduction	193
6.2	Mode-I Fracture Characterization of CFRP Laminate Composite	194
6.2.1	Material and Experimental Procedures	195
6.2.2	Results and Discussion	196
6.2.2.1	DCB Structural Response	196
6.2.2.2	Delamination Resistance Curve	199
6.2.2.3	Interface Delaminated Region	200
6.3	Mode-II Interlaminar Damage and Fracture Characterizations of CFRP Laminate Composites	201
6.3.1	Problem Description and Hybrid Experimental- Computational Approach	202
6.3.2	Experiments Method	204
6.3.3	FE Simulation Process	205
6.3.4	Results and Discussion	208
6.3.4.1	Validation of the Mechanics of System Responses, and Mechanism of Damage	208
6.3.4.2	Sequence of Interface Damage and Fracture Processes	213
6.3.4.3	Stress Distribution in Laminas	214

6.3.4.4	Evolution of Interface Damage	219
6.3.4.5	Progressive Interface Damage Process	223
6.3.4.6	Interface Damage Accumulation	225
6.3.4.7	Interlaminar Failure Characteristics	227
6.3.4.7.1	Fractographic Analysis of Delaminated Interface (Stable Case)	228
6.3.4.7.2	Fractographic Analysis of the Unstable Interface Failure of CFRP Composite	231
6.3.4.8	Structural Response and Interlaminar Fracture Process using Hybrid Experimental-Computational Technique	233
6.3.4.8.1	Mechanical Behavior in Relation with Structural Response Using Hybrid Experimental- Computational Technique	244
6.3.5	Summary and Outlines	247
7	FAILURE OF CFRP COMPOSITE LAMINATES BY MULTIPLE DAMAGE AND FAILURE PROCESSES	250
7.1	Introduction	250
7.2	Material and Experimental Procedure	252
7.3	Finite Element Modeling Process	253
7.4	Results and Discussion	256
7.4.1	Structural Response and Multiple Failure Events	257
7.4.2	Structural Response and FE Model Validation Process	263
7.4.3	Multiple Damage Initiations Processes	266
7.4.4	Variation of the Effective Stresses	271
7.4.5	Evaluation of Critical Energy Terms	273
7.4.6	Mechanisms of Multiple Failures of CFRP Composite Laminates	277

7.5 Summary and Outlines	286
8 CONCLUSION AND RECOMMENDATION	289
8.1 Conclusion	289
8.2 Recommendations	294
REFERENCES	295
Appendices A-B	326-330

LIST OF TABLES

TABLE NO.	TITLE	PAGE
3.1	Characterization of specimens geometry and loading rates.	59
3.2	Specimen configurations for tensile and flexural loading tests.	60
3.3	Elastic properties and damage model parameters of unidirectional GFRP and CFRP1 laminas.	62
3.4	Elastic properties of unidirectional CFRP2 lamina and interlaminar elastic-damage properties of CFRP2 and CFRP1.	62
3.5	Steps for modeling, solution and post-processing phases and the corresponding procedures implemented in the FE software according to FE simulation process.	66
3.6	Summary of the FE model and experimental test through the present study	83
6.1	FE Models of CFRP composite for ENF test setup.	207
6.2	Sequence of interface damage evolution and fracture of CFRP composite under ENF loading condition.	214
7.1	Location and time to fiber and matrix damages in each lamina of CFRP composite under four-point bending test.	270

LIST OF FIGURES

FIGURE NO.	TITLE	PAGE
2.1	Composite material construction.	13
2.2	Composite material systems and configurations.	14
2.3	The levels of analysis in FRP laminated composite structures according to their micro-to-macro construction.	15
2.4	Various failure modes in FRP laminate composites at different scales.	17
2.5	(Left) Young's modulus versus density, and (Right) specific stiffness versus specific strength of various materials.	18
2.6	The new Boeing 787 and the total different types of materials that is used in the airplane body.	19
2.7	(Top) the materials distribution (weight breakdown) and, (Bottom) major monolithic CFRP composite and thermoplastics applications in Airbus-A380.	20
2.8	Global axis (x,y) and local axis (1,2) of an angle lamina.	28
2.9	Variation of strain and stress parameters through the thickness of the FRP laminate composites.	30
2.10	Mechanism of damage in FRP laminate composite under tensile loading condition (lateral cross-section view).	31
2.11	Mechanics of solid materials and analysis domains classification.	34

2.12	Monotonic deformation and the continuum damage process in an isotropic material.	36
2.13	Matrix cracking under pure and mixed-mode loading condition.	42
2.14	Multiple failure events in CFRP composite beam under tension load.	49
3.1	The framework of the research methodology.	55
3.2	Interlaminar fracture toughness tests under Modes I (left) and II (right) loading conditions.	58
3.3	The specimens configuration for three- and four-point bending, and tensile tests on GFRP and CFRP composites.	60
3.4	General sequence of FE simulation steps.	67
3.5	Meso-scale construction of [45/0/90] composite laminate that show different manufacturing process of, (a) VIP method represented by Conventional FE model and (b) Prepreg/Autoclave Method represented by Prepreg FE model.	69
3.6	FE based-model construction of multidirectional FRP composite, representing the conventional (VIP manufacturing process) and Prepreg (Prepreg/Autoclave fabrication method) models.	70
3.7	Flowchart of the method to specify the correct FE model construction for FRP composite laminates that manufactured using different methods.	71
3.8	Identical spring view of FRP laminate composites that are modeled using different constructions of: (a) conventional (b) Prepreg, (c) Prepreg model with interface decohesion element models.	74
3.9	FE mesh configuration of CFRP composite under three-point bending condition.	76

3.10	Mesh convergence study of CFRP composite under three-point bending condition, by monitoring the effective stresses variation at a critical point.	77
3.11	Outcomes of the two-tier FE mesh convergence study (a) Load-deflection and (b) flexural stiffness curves.	78
3.12	Flowchart of mesh convergence study for damage analysis of FRP composite system.	79
3.13	Flowchart of experimental-computational approach implementation.	81
4.1	Progression of failure in multidirectional FRP composite in the form of micro-macro scale damage, illustrated in meso-scale at unidirectional FRP lamina level.	86
4.2	Bilinear softening constitutive model for each failure mode in material point of the continuum lamina.	88
4.3	(a) Schematic view of failure surfaces, (b) failure modes, and failure planes (b).	93
4.4	Schematic multi-surface of Hashin's failure criteria.	95
4.5	Continuum orthotropic material under external loading, and orthotropic elements under different types of internal loads (a), the effective stresses resultant on orthotropic element (b).	96
4.6	Deformation and the continuum damage concept in a lamina (longitudinal or transverse direction) under tensile (or compression) load.	98
4.7	The physical concept of post-damage initiation and schematic stiffness behavior of orthotropic FRP material.	111
4.8	Elastic constitutive behavior of anisotropic materials based on damage modes.	113
4.9	The schematic view of the constitutive damage model for mixed-mode elastic-damage behavior in a material point of	

	unidirectional lamina.	115
4.10	Variation of equivalent stress versus damage dissipation energy in softening process of each damage mode.	117
4.11	Damage variable as a function of equivalent displacement.	118
4.12	Linear softening law versus damage dissipation energy through softening process.	119
4.13	Multiple constitutive damage models for elastic-damage behavior of FRP lamina (assumption; matrix damage initiates as the first mode).	122
4.14	Failure surface of orthotropic FRP lamina based on (a) critical equivalent stress, and (b) critical equivalent deformations (assumption; matrix damage initiates as the first mode).	124
4.15	Constitutive motion-based linear damage evolution law.	127
4.16	Constitutive model for interface damage and related pure modes of loading.	130
4.17	Mixed-mode traction-displacement law in continuum damage process of interface material point.	133
4.18	Mixed mode loading and softening law in an equivalent form.	136
4.19	Single lap joint model for meso-scale simulation of interface using different FE-based model constructions.	138
4.20	FE simulation results as stiffness curve of single lab joint sample based on three different interface configurations.	139
4.21	Stress distribution based on different FE construction.	139
5.1	Lateral cross-section of the GFRP (Left) and CFRP (Right) composite laminates.	149
5.2	GFRP (Left) and CFRP (Right, top) composite specimens under three-point bending load condition. Permanent	

	bending deformation of the CFRP specimen after unloading (Right, bottom).	150
5.3	FE model of GFRP composite beam under three-point bend test setup (a), Lateral cross-sections view of mesh (b), Anti-symmetric top view of lamina mesh (c).	151
5.4	Measured load central-deflection curves of the CFRP composite.	154
5.5	Microscopic images of lateral cross-section of CFRP composite under three-point bending test.	155
5.6	Mesh study and FE model verifications, (Left) Load-deflection responses, (Right) Flexural Stiffness.	156
5.7	Effective mechanical parameters of load-deflection curve.	157
5.8	Element size sensitivity to fiber damage initiation of CFRP lamina (No. 1) under compression loading condition.	158
5.9	Comparisons of predicted results with experiment data of the CFRP composite beam under three-point bending test, (a) Load-deflection and, (b) Flexural stiffness responses.	159
5.10	Simulation and experimental results of the strain variation versus the monotonic deflection of the CFRP composite beam.	160
5.11	(Top) Contour of deformation at lamina twelve in both FE models, (bottom) Downward deformation of CFRP beam width at center on the first lamina under loading-roller.	161
5.12	Variation of effective stress and matrix damage evolution parameters at a point on lamina with 45o of CFRP composite.	162
5.13	Onset of matrix cracking predicted based on Prepreg and conventional FE models.	164
5.14	Critical locations for evaluation of stress and strain variation.	165

- 5.15 Variations of the maximum and minimum principal stresses in each lamina of the conventional and Prepreg models; (a) Elastic condition when the structure under 4.8mm deflection, (b) Damaged structure at 20.6mm deflection. 166
- 5.16 Variation of Local longitudinal and transverse normal and shear stresses across the width of the CFRP composite specimen. (Solid and dashed lines represent stresses in laminas No. 1 and 12, respectively; E– Elastic case, D – Damage case). 168
- 5.17 Contour of longitudinal normal stress σ_{11} on first and last three laminas, and transverse normal stress σ_{22} on first and last laminas of CFRP composite beam under three-point bending test. 169
- 5.18 Contour of longitudinal normal stress σ_{11} and Von Mises stress through-thickness at the center of width of CFRP composite beam under three-point bending test. 171
- 5.19 Variation of average stress through width of laminas in CFRP composite beam under three-point bending test. 172
- 5.20 Matrix damage initiation and propagation at lateral cross-section of CFRP composite laminate in edge and central locations of the width, based on different FE constructions. 174
- 5.21 Distribution of matrix damage initiation and propagation in each CFRP lamina at the end of the flexural test of both FE model constructions. 176
- 5.22 Distribution of matrix damage initiation and propagation in each CFRP lamina at the end of the flexural test (deflection of 28 mm) using Prepreg FE construction, and matrix damage-induced delamination in CFRP laminate composite. 178
- 5.23 Distribution of Fiber damage initiation and propagation in cross-section of CFRP laminate composite (a), and in laminas No. 4 and 9 (b) of conventional and Prepreg FE

	model constructions.	180
5.24	(a) Comparison of internal (Int), strain (Str) and damage dissipation (DD) energies of CFRP composite under three-point bending condition for conventional and Prepreg FE model constructions, (b) Flexural stiffness and damage dissipation energy of CFRP composite modeled using Prepreg construction.	182
5.25	Comparison of strain and damage dissipation energies evolvment in each lamina of conventional and prepreg constructions for CFRP laminate composite.	184
5.26	Load-deflection and flexural response of GFRP composite under three-point bending test.	186
5.27	Through-thickness variation of stress and logarithmic strain of GFRP composite beam under three-point load for different states of bending loads.	188
5.28	Microscopic image of lateral cross-section of the GFRP composite in comparison with FE result of distribution of damage initiation and propagation.	190
5.29	(a) Distribution of fiber damage evolution in first and last laminas of GFRP composite under bending condition, (b) Level of damage propagation through the width of first lamina.	191
5.30	The evolvment of damage dissipation energy of GFRP composite laminate and laminas under flexural loading condition.	192
6.1	(a) Half of longitudinal cross section of CFRP composite, (b) Configuration of the composite specimen for DCB test.	196
6.2	Structural response of DCB tests as load-displacement curves of the composite specimen with different initial cracks.	197

6.3	Variation of compliance parameter of CFRP composite in DCB test with respect to normalized delamination length.	198
6.4	Variation of load at onset of interface delamination with respect to normalized delamination length.	199
6.5	Delamination resistance curve of CFRP composite under DCB test loading condition.	200
6.6	Micrograph of delaminated region at mid-plane of the CFRP composite.	201
6.7	(a) ENF test set-up, (b) Crack-tip microscopic image, and ENF test set-up of CFRP composite for (c) stable and (d) unstable conditions.	205
6.8	FE model geometry of CFRP composite beam for ENF test setup (Case ID; ENF1 at Table 3.1).	206
6.9	FE results and experiment data as load-deflection responses of CFRP composites for stable and unstable ENF loading conditions.	209
6.10	Comparison of predicted flexural stiffness responses of both models with measured curve for the CFRP composite beams under ENF loading conditions.	210
6.11	(a) Load–deflection response of CFRP composite with and without initial crack, (b) Comparison of observed crack grows in the experiment and the predicted FE of the stable model.	212
6.12	Sequence of interface damage evolution depicted on load-deflection responses of CFRP composite beam under ENF loading condition.	213
6.13	Effective stress distribution at cross-section of CFRP composite at center of width around crack-tip of (a) stable and (b) unstable cases.	215

6.14	Through-thickness evolution of laminate longitudinal stress before and after interface fracture.	217
6.15	Distribution of longitudinal stress and the evolution of the zero-level stress zone in CFRP composite under ENF loading condition.	218
6.16	Stress S_{13} variation at crack-front in term of overall deflection of the beam.	219
6.17	Evolution of critical stresses and damage parameters on individual point on the interface bonded region from crack-front.	221
6.18	Damage and shear stress evolutions at a path from center of crack-front toward composite beam length.	222
6.19	Contour plot of damage initiation (QUADSCRT) and propagation (SDEG) at interface of the stable CFRP composite beam under ENF loading condition.	225
6.20	Rate of damage accumulation and dynamic nature of the interface crack.	226
6.21	Isometric view and top image of the Fractured CFRP composite under ENF loading condition.	229
6.22	SEM images of the fractured interface of CFRP composite under stable ENF loading condition.	230
6.23	Macro and meso images of the crack-jump event in the CFRP composite beam under unstable ENF loading condition.	231
6.24	Fractographic images of the shear-dominated interface failure of CFRP composite due to crack-jump event.	232
6.25	Relation between stiffness responses of CFRP composites under ENF loading condition.	234

6.26	Prediction of the stiffness curve of four models indicated in Table 6.1, with the interface definition of elastic and elastic-damage, of CFRP composite under ENF loading condition.	236
6.27	Level of SLSSZ parameter and maximum deflection of CFRP composite structure with different lengths under ENF loading condition.	237
6.28	Predicted monotonic variation of total strain energies of CFRP laminate and laminas of the stable case (No. 1, Table 6.1).	238
6.29	Through thickness variation of maximum strain energy in each lamina and interface of (a) model No. 1, at the time before and after fracture and (b) model No. 1, 2, 4 prior to interface fracture.	240
6.30	Monotonic variation of total strain energy of CFRP composite models No. 1, 2 and 4 (Table 6.1) with respect to system deflection	241
6.31	Monotonic variation of critical energies in interface of CFRP composite (model No. 1) under ENF loading condition.	242
6.32	Monotonic variation of damage dissipation energy in the interface of CFRP composite model No. 1, 2 and 4 based on the system deflection.	243
6.33	Monotonic variation of damage dissipation energy in the interface of CFRP composite model No. 1, 2 and 4 based on the system deflection.	243
6.34	Critical point in mechanical behavior of CFRP composite model No. 1, 2 and 4 (Table 6.1) under ENF loading condition.	244
6.35	Individual variation of force and deflection parameters with respect to CFRP composite support span length under ENF loading condition.	245

6.36	Variation of flexural stiffness with respect to deflection and support span length of CFRP composite model No. 1, 2 and 4 (Table 6.1) under ENF loading condition.	246
7.1	Lateral cross-section of the multidirectional CFRP laminate composite.	252
7.2	CFRP composite specimens under four-point bending (a) at beginning and (b) end of loading process.	253
7.3	Overall view of the FE model of CFRP composite beam under four-point bend test setup.	254
7.4	Through-thickness creation of lamina and interface constituents.	255
7.5	CFRP composite beam response under four-point bending condition.	257
7.6	(a) Macro images of CFRP composite under four-point bending test, Microscopic image of the lateral cross section (b) before damage, (c) after damage at side of the edge and (d) at middle of the edge.	258
7.7	(a) Macroscopic image of the CFRP composite under four-point bending test after unloading, (b) mesoscopic image of multiple failures at lateral cross-section.	259
7.8	Individual microscopic images of the failure from lateral cross-section of CFRP composite under four-point bending test.	260
7.9	Meso/microscopic images of multi-failure at lamina No.1 of CFRP composite under four-point bending test.	261
7.10	Experiment and FE results as system response of the CFRP composite beam under four-point bending test, (a) Load-deflection and, (b) Flexural stiffness responses.	263
7.11	(a) A schematic view of beam saddle deformation under flexural loading, (b) Macroscopic image of CFRP composite	

	beam after four-point bending condition, and microscopic image of scratching marks from the beam touch-points with the loading supports, (c) Contour of deformation (along loading direction) of CFRP composite structure.	265
7.12	Evolution of matrix damage initiation for each lamina at center of the length of CFRP composite beam under four-point bending condition.	267
7.13	Time to onset of damage in (a) fiber, matrix and (b) interface of CFRP composite beam under four-point bending test.	269
7.14	Damage initiation and propagation in each lamina of CFRP composite beam under four-point bending test for (a) matrix and (b) interface failures.	271
7.15	Variation of effective stress S_{22} at edge/middle of length of CFRP composite beam under four-point bending test.	273
7.16	Evolution of critical energies (per unit volume) of CFRP composite under four-point bending test.	274
7.17	Evolution of (a) strain and (b) damage dissipation energies in laminas of CFRP composite under four-point bending test.	276
7.18	Evolution of strain energy in each interface of CFRP composite under four-point bending test.	277
7.19	Comparison of FE result of the multiple failures at lateral cross-section of CFRP composite with experiment data.	278
7.20	Contour of damage evolution in lamina No. 9 and interfaces No. 8 and 9 of CFRP composite beam under four point bending test.	279
7.21	Comparison of FE result of the multi-failure at lamina No. 1 of CFRP composite with experiment data.	280
7.22	Fiber (Left) and matrix (Right) damage initiations at laminas, and interfaces failure (Center) of CFRP composite beam under four-point bending.	285

LIST OF ABBREVIATIONS

AFR	-	Automated fiber replacement
ASTM	-	American society of testing method
ATL	-	Automated tape laying
CDM	-	Continuum damage model
CFRP	-	Carbon fiber reinforced polymer
CNC	-	Carbon nanocoil
CNF	-	Carbon nanofiber
CNT	-	Carbon nanotubes
CVD	-	Chemical vapor decomposition
CZM	-	Cohesive zone model
DCB	-	Double cantilever beam
DI	-	Damage initiation
DP	-	Damage propagation
DPL	-	Deviation point from linearity
ELS	-	End loaded split
ENF	-	End-notched flexure
FE	-	Finite element
FEM	-	Finite element method
FLF	-	First lamina failure
FRP	-	Fiber-reinforced polymer
GFRP	-	Glass fiber reinforced polymer
GLARE	-	Glass laminate aluminum reinforced epoxy
HME	-	Hypothesis of mechanical equivalence
HSE	-	Hypothesis of strain equivalence
LEFM	-	Linear elastic fracture mechanics
LSL	-	Linear softening law

MBT	-	Modified beam theory
ML	-	Maximum load
PR	-	Poisson's ratio effect
RFI	-	Resin film infusion
RTM	-	Resin transfer molding
SLSSZ	-	Stable limit of shear stretch zone
SEM	-	Scanning electron microscope
microCT	-	micro computer tomography
VAP	-	Vacuum-assisted Resin process
VIP	-	Vacuum infusion process
WWFE	-	worldwide failure exercises
3D	-	Three-dimensional

LIST OF SYMBOLS

E	-	Young's modulus
ν	-	Poisson's ratio
\bar{Q}_{ij}	-	Element of the transformed reduced stiffness matrix
Z	-	Distance from the central line
ε^0	-	Strain at $Z = 0$ (center-line of the composite beam)
E_0	-	Original material stiffness
$E_{(D)}$	-	Elastic modulus of the material at damaged state
D	-	Scalar damage variable
σ	-	Nominal, true or Cauchy stress tensor
$\hat{\sigma}_{ij}$	-	Effective stress component
$E_{(D)}$	-	Elastic modulus of the structure at damaged state
Y_C	-	Normal strength perpendicular to fiber direction under compression loading condition
S_{12}	-	Shear strength
α	-	Shear direction
Y_T	-	Normal strength perpendicular to fiber direction under tension loading condition
σ_{22}^m	-	Normal stress in 2D kinking frame
τ_{12}^m	-	Shear stress in 2D kinking frame
$\bar{\sigma}$	-	Effective normal stress
$\bar{\tau}$	-	Effective shear stress
φ	-	Matrix crack density
ζ	-	Curve fitting parameter
Z_T	-	Traction strength along through-thickness of interface
K	-	Curve fitting parameter

k	-	Number of nodes in a lamina
f	-	Number of nodes in one surface of a lamina
h	-	Number of elements through a lamina thickness
n	-	Number of the laminas
K_{Conv}	-	Number of nodes in lcomposite aminate with conventional model
K_{Prep}	-	Number of nodes in composite laminate with prepreg model
ϵ_{ij}	-	Normal strain compoinent of strain tensor
γ_{ij}	-	Shear strain compoinent of strain tensor
σ_{ij}	-	Normal stress compoinent of stress tensor
τ_{ij}	-	Shear stress compoinent of stress tensor
ϵ_i^0	-	Midplane normal strain of composite laminate
γ_{ij}^0	-	Midplane shear strain of composite laminate
K_i	-	Midplane curvature of composite laminate
$f_{(\sigma_{ij})}$	-	Function of stress tensor component
Y	-	Yield stress of a bar under uniaxial tension load
d_{11}^t	-	Internal damage variable of lamina in fiber direction under tension load
d_{11}^c	-	Internal damage variable of lamina in fiber direction undercompression load
d_{22}^t	-	Internal damage variable of lamina perpendicular to fiber direction under tension load
d_{22}^c	-	Internal damage variable of lamina perpendicular to fiber direction under compression load
X^T	-	Lamina normal strength in fiber direction under tension load
Y^T	-	Lamina normal strength perpendicular to fiber direction under tension load
X^C	-	Lamina normal strength in fiber direction under compression load
Y^C	-	Lamina normal strength perpendicular to fiber direction under compression load
S^L	-	Lamina longitudinal shear strength

S^T	-	Lamina transverse shear strength
G_{XT}	-	Longitudinal tensile fracture energy
G_{XC}	-	Longitudinal compressive fracture energy
G_{YT}	-	Transverse tensile fracture energy
G_{YC}	-	Transverse compressive fracture energy
M	-	Damage effect tensor
k_{eq}^0	-	Original equivalent stiffness prior to damage initiation
δ_{eq}^0	-	Equivalent displacement at damage initiation
δ_{eq}^f	-	Equivalent displacement at failure
σ_{eq}	-	Equivalent stress of failure modes
σ_{eq}^f	-	Equivalent stress at failure
C_o	-	Elastic compliance tensor
D_P	-	Damage propagation parameter
G	-	Strain energy release rate
L^c	-	Characteristic length in the reference surface of shell elements
G_C	-	Critical energy release rate
G_T	-	Total energy release rate
G_{DDE}	-	Damage dissipation energy
F_i	-	Force in i^{th} node
u_j	-	Motion of the node j^{th}
T_i	-	Component of traction
δ_{Shear}	-	Equivalent relative shear displacement
β	-	Mode mixity in interface material point
G_{Shear}	-	Energy release rate of mixed shear loading in modes II and III
G_I	-	Energy release rate in mode I
G_{II}	-	Energy release rate in mode II
G_{III}	-	Energy release rate in mode III
G_{IC}	-	Critical energy release rate in mode I
G_{IIC}	-	Critical Energy release rate in mode II
G_{IIIC}	-	Critical Energy release rate in mode III
G_{TC}	-	Total critical strain energy release rate in mixed-mode loading condition

$\delta_{i_m}^f$	-	Relative displacement at failure under mixed-mode loading for each mode of interface damage
D_{sr}	-	Operator of the interface constitutive model
$\bar{\delta}_{sr}$	-	Kronecker delta
P	-	Current mass density
\mathbf{u}	-	Velocity field vector
U	-	Internal energy per unit mass
\mathbf{t}	-	Surface traction vector
\mathbf{f}	-	Body force vector
E_U	-	Dissipated portions of the internal energy
E_K	-	Kinetic energy
E_F	-	Energy dissipated by contact friction forces between the contact surfaces
E_W	-	Work of a body by external forces
E_{QB}	-	Energy dissipated by the damping effect of solid medium infinite elements
σ^v	-	Viscous stress
σ^c	-	Stress derived of a constitutive equation
$\dot{\epsilon}^{el}$	-	Elastic strain rate
$\dot{\epsilon}^{pl}$	-	Plastic strain rate
$\dot{\epsilon}^{cr}$	-	Creep strain rate
E_S	-	Applied elastic strain energy
G_U	-	Internal energy
G_E	-	Strain energy
G_D	-	Dissipated energy

LIST OF TERMINOLOGIES

- | | | |
|---|---|---|
| Multi-damage or -failure | - | Various types of damage or failure events that occur in a FRP lamina as a solid continuum part. |
| Multi-delamination | - | Occurrence of several delamination events in FRP composite laminates. |
| Multiple damage, failure, fracture or crack | - | Simultaneous occurrence of several damage, Failure, fracture or cracking events in intralaminar and interlaminar constituents of FRP composite laminates. |
| Crack-jump phenomenon | - | An initial interlaminar crack in FRP composite laminate under mode I or II loading condition, which propagated suddenly with large size. |

LIST OF APPENDICES

APPENDIX	TITLE	PAGE
A	The formulation of finite-displacements between two nodes at interface, in the constitutive motion-based model	326
B	Flowchart of the hybrid experimental-computational technique	329

CHAPTER 1

INTRODUCTION

1.1 Introduction

Fiber-reinforced polymer (FRP) composite laminate materials are increasingly replaced by metal materials in advanced structural application in defense, transport and etc. industries. Therefore, a correct comprehension about failure phenomena in FRP composite is necessary for the design and analysis of such structures. The knowledge of failure in composites normally obtained using numerical and experimental approaches. The experimental procedures normally are expensive and time consuming for complex loading condition which rarely can be used for design stages of composite structures. The numerical methods involve the mathematical derivation of structural behavior, failure phenomena and energy absorption of composites, which normally provide a deeper insight on structural failure for the design phase, however it is incomplete to define a response map of the three-dimensional (3D) structures. In the past three decades, development of *Simulation Methodologies* has been considered as one of the most effective method in bridging the mathematical models and experiments for realistic design and analysis of advanced industrial structures. Simulation procedures are benefit scientists to characterize the mechanical properties, to define the response map, and to enhance the final design of the composite structures using the lowest number of expensive samples and tests.

At the current state of development, an extensive analytical models have been introduced for numerical investigation of failure in composites, however the simulation methodology in prediction of complex multiple failure is still considered as an open topic for investigation. The present study uses the finite element method (FEM) as the most used approach, to develop a simulation methodology for prediction of multiple failure in multidirectional FRP composite laminates. The theory of continuum damage mechanics is used to develop the constitutive models for prediction of elastic-damage and fracture behaviors. Simulation of several tests on unidirectional/multidirectional FRP composites with and without pre-cracks are performed to examine the considered models and the methodology procedure.

1.2 Problem Background and Rationale

In the past few decades, advanced industries demand for materials with both light and strong features has been the main force to develop composite materials (Dempster D., 2003; Taylor, 2008). Advanced composite materials are constructed of two or more separate phases, mainly consisted of matrix phase, reinforcement phases and matrix/reinforcement interface that is known as interphase region. Fiber Reinforced Polymer (FRP) composites as one of the important advanced composites are created using polymeric matrix phase (thermoplastic, thermoset and etc.) which typically reinforced with fibrous (glass, carbon, aramid and etc.) materials. The design flexibility of FRP laminate composites through variation of matrix/reinforcement phase types, adjustment of reinforcement volume fraction in micro-scale and modification of laminas orientation in meso-scale, highlighted the capability of these materials for creation of superstructures with preferable solidity in various directions. The great advantages of FRP composites including high stiffness-strength combined with low weight bring a steady increase of investment in transport, aerospace and green industries on continuous replacement of metallic structures to composites. For this reason, the development of reliable and well-validated mathematical-physical models to describe the linear and nonlinear behavior of composites, become essential. Therefore, development of continuum damage

model (CDM) for anisotropic material is important (Baker et al., 2004; Kaw, 1997; S. Murakami, 2012).

Mechanics of FRP composite materials is classified based on the level of the analysis in micro-, meso- or macro-scales. Therefore, damage and failure analyses of composite structures are practiced in different scales too. In this respect, the influences of mechanical features and properties in the microstructure of lamina have to be considered in the constitutive elastic-damage model parameters when it viewed in meso-macro scales too. Therefore, bridging between micro-to-macro mechanics is always one of the factors that is used prediction of mechanical behavior in composite materials (Baker, et al., 2004; R. Talreja and Singh, 2012).

In constructional view, FRP composites are created with a soft polymeric phase that is reinforced with stiff fibrous phase with almost 30-95% (e.g. Typical glass fiber reinforced polymer (GFRP), carbon fiber reinforced polymer (CFRP)) elastic-stiffness properties differences. Likewise, the anisotropic strength of the FRP composites normally shows up to 90% difference in the fiber direction compared with transverse to the fiber direction. Such big differences in elastic-strength properties accelerate early failure in weaker phases while structural performance is considered to be in the safe zone. In a FRP composite structure, fibers are assumed to be responsible for load bearing due to high stiffness, but in the other hand consideration of Poisson's ratio influences as a part of anisotropic continuum behavior is undeniable. Therefore, occurrence of matrix failure in high strength FRP composites such as CFRP is likely, which has to be considered as one the factors in design FRP composite structures. Therefore, understanding of yielding phenomena in composite lamina in meso-scale and laminate in macro-scale and also the related criteria with respect to yield surface is important. The present study, is attempting to introduce an overall yielding point in FRP *lamina* and *laminate*, using damage mechanics concept by considering a certain value of accumulated irrecoverable energy in the structure over total damage dissipation energy (Dempster D., 2003; R. Talreja and Singh, 2012; Taylor, 2008).

Most of the existing knowledge of damage and failure in FRP composites obtained through experimental and numerical methods. Normally, experimental data are limited due to the high value of cost for tests implementation and less diversity of data which rarely can be utilized in earlier design methods. In the other hand, internal analysis of structures in terms of deformation and damage zone is hardly possible, which most of the time considered as important knowledge that have to be obtained for design and analysis of composite superstructures. Numerical methods are normally cost saving in comparison with the experimental method, which is enabling a huge amount of data on mechanical parameters that lead to a deep insight into the design and failure analysis of composite structure. In the other hand, once a model is established, it could be used for various analyses, including different types of loads and boundary conditions. These results can be used in defining the responses map of the material as a support for enhancing the final design of the structure at low cost (Baker, et al., 2004; R. Talreja and Singh, 2012). However, at the current state, numerical models are not developed fully to cover the failure behavior of composite materials under complex loading condition. Several constitutive elastic-damage models based on continuum mechanics approach are derived to overcome this challenge, including a series of studies called the worldwide failure exercises (WWFE) that is made to describe the foremost theories for FRP composites (Chamis et al., 2013; Hinton, Kaddour and Soden, 2004; Kaddour et al., 2013; Labeas et al., 2011; Varna, 2013). In this exercise, a huge number of comparisons have been made on the capability of different mathematical models in order to predict the evolution of damage and failure events under various types of loading consist of biaxial, bending, thermal loadings and loading-unloading condition (Hinton, et al., 2004; Kaddour, et al., 2013). Several approaches including multi-scale hybrid damage and failure (Laurin et al., 2013), micromechanics based model (Chamis, et al., 2013), shear lag and equivalent constraint model (Kashtalyan and Soutis, 2013), enhanced damage meso-model (Daghia and Ladeveze, 2013), energy methodology (McCartney, 2013a, 2013b), constitutive damage model (Schuecker and Pettermann, 2013), plasticity-based theory (S. Pinho, Vyas and Robinson, 2013), classical damage model (Sapozhnikov and Cheremnykh, 2013), synergistic damage mechanics (Singh and Talreja, 2013), global-local cracking approach (Varna, 2013), structural damage modeling framework (Forghani et al., 2013) and its, are used to make comparison between the models and the experimental data. The conclusion of this research was

that, out of 12 leading theories and 13 challenging tests for prediction of failure evolution, "*Only three groups solved all the 13 challenging problems and approximately 30% of the test cases were not solved*" (Kaddour, et al., 2013). It is noted that in general, the lack of consensus appears regarding the effects of ply thickness and lay-up sequences, influences of unloading-reloading behavior, and interaction in multiple crack locations and matrix crack-delamination (Kaddour, et al., 2013). Miscomprehension of the complex physics of FRP composite failure also commented as one of the reasons for low accuracy in prediction of failure (Silvestre Taveira Pinho, 2005). Most of the mathematical models are stress-based models computed at local material point through damage criteria to address the local failure process. Variation of effective stresses in FRP composites depend on assumed construction based on FEM and also the theoretical basis. One of the aspects, which have not been paid enough attention, is the influences of manufacturing processes in micro-meso construction of FRP composites through computational method. The present work investigated on the finite element (FE)-based model construction that could represent the actual construction of the composite created through different fabrication processes. This point is recommended for further investigation in previous works as multi-layer modeling methodology for failure analysis of FRP laminate composites (Kaddour, et al., 2013; Siromani, 2013). In other study, investigation on the physical properties reduction of composite structure due to damage and multiple failure is recommended for future work (Lasn, 2015). Full set of CDMs is reviewed and applied to address the progressive damage processes of FRP composites. FEM as an affective approximate method is used for predicting the complex response of composite structures. Implementation procedure of FEM is described extensively through a hybrid experimental-computational approach in order to combine the FE and test data for a comprehensive understanding of the failure process. Emphasis is placed on engineering aspects, such as the analytical descriptions, effective analysis tools, modeling of physical features and evaluation of approaches used to formulate and predict the actual response of composite structures (Ochoa and Reddy, 1992).

1.3 Statement of the Research Problem

How to identify and characterize the fracture processes of FRP laminate composites using damage-based models and finite element method under quasi-static monotonic loads?

1.4 Research Questions

The relevant research questions to the problem statement of the present study can be sorted out as follow:

1. What are the dominant damage mechanisms of FRP composites?
2. What models are suitable for simulating the observed linear-nonlinear deformation and fracture of FRP composites?
3. How does damage, initiate and propagate in matrix, interface and fiber of FRP composites?
4. How to evaluate the mechanics and mechanism of multiple damage processes (matrix cracking/crushing, multi-delamination and fiber breakage/buckling) in FRP composite materials under quasi-static monotonic loading condition?
5. How would the damage models and failure process be validated?

1.5 Objectives of Study

The aims of the present study are to develop a validated simulation methodology for failure processes of the FRP laminate composite under quasi-static monotonic loads. In this respect, the objectives of the study are defined in the main

fields of mathematical-physical modeling, FE simulation and experimental works to solve the problem, which are develop and completed in the next chapters. The objectives are linked and highlighted throughout the research in the result and discussion chapters, which a short summery of them is listed in the conclusion remarks (Chapter 8).

The specific objectives of this study are:

1. To develop and derive bilinear physically-based damage model for FRP lamina.
2. To establish FE-based model constructions of FRP composite based on different manufacturing processes.
3. To identify the mechanics and mechanism of failure of FRP laminate composites under quasi-static loading.
4. To investigate on the effect of different constructions on the progressive damage processes of FRP laminate composites
5. To predict the elastic-plastic behavior and mechanism of multiple failure in FRP composite beams under flexural loading.
6. To represent the FE implementation of damage and failure in FRP composite using a hybrid experimental-computational approach.
7. To validate the damage-based FE model using experimental results.

1.6 Scope of Study

The present study is concentrating on the simulation methodology to identify and characterize the mechanics and mechanisms of failure in FRP laminate composites under monotonic loading condition. The scope of this research is restricted to unidirectional FRP laminate composites as:

1. Only, the two manufacturing processes of Prepreg/Autoclave method and vacuum infusion process (VIP) are considered, to fabricate multidirectional FRP composite laminates.
2. To prepare CFRP composite manufactured using Prepreg/Autoclave method, with uni/multi-directional ply sequences, and with/without pre-crack.
3. To manufacture anti-symmetric GFRP composites using VIP method, and machining into beam samples for mechanical test.
4. To perform mechanical tests on the FRP composite beams, to obtain the structural response and mechanical properties as follow:
 - a. Three and four-point bending tests on anti-symmetric CFRP and GFRP composite laminates.
 - b. Double cantilever beam (DCB) and end-notched flexure (ENF) tests on CFRP composite to obtain the critical fracture energy of interface in modes I & II loading condition.
 - c. To perform critical ENF test on a specially designed specimen to capture unstable crack-jump.
5. To identify the various types of intralaminar and interlaminar fracture events in FRP composite laminates, using fractographic investigation on the tests performed in the above cases (No. 3).
6. To develop and describe the theories as bilinear CDMs for FRP lamina and interface.
7. To create FE models using ABAQUS 6.9EF software, in order to simulate the following cases:
 - a. To develop FE model-based constructions that represent the construction of FRP composite laminates, which are manufactured using VIP and Prepreg/Autoclave methods.
 - b. To develop individual FE models of FRP composite laminate, to simulate laminas failure using CDM, and also interface delamination using cohesive zone model (CZM).
 - c. To develop a FE model that comprises both CDM and CZM models to simulate multiple fracture in CFRP composite laminates manufactures using Prepreg/Autoclave methods.

8. To validate the damage theories and FE models (above cases, No. 6) using experimental data, in both aspects of mechanics and mechanism of damage.
9. To establish the simulation methodology for fracture processes of FRP composites using hybrid experimental-computational approach throughout of the present study.

1.7 Layout of the Thesis

In this thesis, chapters are arranged to address the FE simulation methodology for prediction of the mechanics and mechanism failure in FRP laminate composites. Assessment of progressive multiple damage processes through laminas and the interface of the composite are the main interest. In this respect, the content of the chapters is classified to explain the objectives and scope of the research as follow.

Chapter 1 gives an overview on the background of laminate composites and the challenges in simulation and analysis for real applications. Then the problem statement, objectives and the scope of the research are described. The limits of what this study is restricted to, are notified.

Chapter 2 provides a summary of the literature and previous researches about FRP composite specification, properties and manufacturing methods. The applications of FRP composites in advanced industries are investigated. The use of FEM in simulation of mechanical cases is studied. A brief description of the mechanics deformation and mechanism of failure in FRP composite laminates is provided. Continuum damage mechanics of composite materials are explained to represent a physical view of the damage phenomena. The various modes of failure in FRP composite are studied, and the related damage models, available numerical tools and FE procedures to estimate and predict damage modes are described. Multiple

failure phenomena in FRP composite are demonstrated using fractographic image of a CFRP beam sample under tension loading condition. The missing points and the gaps to previous researches are highlighted.

Chapter 3 discusses about research methodology of the present work. The research framework of the study is provided based on the three activities of modeling, computation and experiment. Types of the specimen, test procedure and the related material properties are provided. The steps for FE simulation of a composite system are described. The manufacturing issues of FRP composite laminates and the related FE model-based constructions are discussed. A hybrid experimental-computational approach is introduced, which is used entirely through the research investigation. The basis of FE implementation of the damage and fracture analyses on different FE constructions of FRP composite is described.

In *chapter 4*, the physically-based continuum models for prediction of multiple failures of FRP laminate composites are described. The phenomena of CDM of lamina and its physical interpretation is discussed. The physical influences of interlaminar region are described for the modeling of FRP composites in the conditions, where perfect laminas bonding or interface debonding are targeted. FE implementation of the model is illustrated through FE simulation by describing the evolution of effective stresses and variation of damage parameters.

Chapter 5 illustrates the FE simulation methodology of FRP composite lamina by introducing specific FE based-model construction for different manufacturing processes. The influences of different constructions in the computation of progressive intralaminar damage process are described. The validated FE models are used to describe the mechanics of system response and mechanisms of multi-damage processes in FRP composite laminates.

Chapter 6 works on the mechanics of interface delamination in CFRP composite in the presence of initial crack. Experimental investigation on CFRP

composite under mode-I test is provided (DCB Test) to discuss about delamination phenomenon. FE simulation and experiment of CFRP composite under mode-II loading is provided (ENF test) to study on the mechanism of interface delamination using CZM theory. The capability of the governing law in prediction of the crack growth and crack-jump phenomena are examined. The concept of stable and unstable crack-jump is developed.

Chapter 7 demonstrates the FE simulation methodology for prediction of multiple failure events in FRP composites by applying CDM and CZM theories in intralaminar/interlaminar parts. The predictive capability of these models in the simultaneous prediction of various failure modes in the lamina and interface of anti-symmetric multidirectional CFRP specimen is examined under four-point bending load condition. Validation of the damage mechanics and mechanism of failure is the main concern.

Chapter 8 explains the conclusion related to the FE simulation methodology and failure mechanism of FRP composites in the present study. The future work on the development of the failure models for fatigue mechanics and etc. of FRP composites are recommended.

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