

MATHEMATICAL MODELS FOR MITIGATING ENERGY HOLES IN
CORONA-BASED WIRELESS SENSOR NETWORK

HASSAN ASADOLLAHI

A thesis submitted in fulfilment of the
requirements for the award of the degree of
Doctor of Philosophy (Computer Science)

Faculty of Computing
Universiti Teknologi Malaysia

June 2014

I dedicate this thesis to my wife. Without her patience, understanding, support, and most of all love, the completion of this work would not have been possible.

ACKNOWLEDGMENT

In the name of Allah, Most Gracious, Most Merciful. I thank Allah s.w.t for granting me perseverance and strength I needed to complete this thesis.

This research would have not been done without the support of greatest scientists I have ever met in my life. I would also like to thank Prof. Dr. Abdul Samad Haji Ismail, for his outstanding scientific support during my study. I would like to give my immense appreciation to Dr. Shukor Abd. Razak for his time and daily helps and updates which makes possible to accomplish this thesis I would like to thank my parents which their support and encouragement create such great possibility to finish my PhD. Last but not the least, my wife Faezeh and who is the strength and support for me in all these years with her devotion.

ABSTRACT

Wireless sensor network (WSN) nodes are usually battery-driven devices with limited power supply and the network lifetime has undoubtedly become a crucial issue. Normally, in WSNs, the data are sent to a base station or cluster heads through multi-hop routing. Under the condition of multiple hops, the sensor nodes closer to the base station or cluster heads tend to die faster because of the imbalance traffic among sensor nodes that consequently lead to an energy hole problem. For mitigating the problem, a mathematical formula to calculate the optimal number of coronas in both random uniform and non-uniform deployment nodes is proposed in circular networks also known as corona-based networks. To formulate it, the energy consumption was calculated for each corona. Besides that, a lemma and two propositions have been proven in this research. Based on this lemma, the critical corona can be identified. In addition, the two proposed propositions can determine the situation in which the interior corona is the one with the greatest energy hole. In addition, an energy-balanced method, Intermittent Varied Range (IVR) data transmission method is proposed to prolong the overall network lifetime and simulations showed that the second inner-most corona has the most positive effect. For IVR method, only two transmission ranges could increase the network lifetime. There would be an increase more than doubled for environment with path loss exponent of two. In this research, a new relay nodes deployment technique is also proposed to balance the energy consumption in the coronas. Using the proposed mathematical equations, the number of relay nodes for maximizing the lifetime of corona-based WSNs could be calculated.

ABSTRAK

Nod rangkaian penerima tanpa wayar (WSN) lazimnya merupakan peranti pacuan bateri dengan bekalan kuasa yang terhad dan tempoh hayat rangkaian tanpa diragui menjadi isu kritikal. Biasanya, dalam WSN, data dihantar ke stesyen pangkalan atau kepala kluster melalui penghalaan multi lompatan. Di bawah situasi multi lompatan, nod penerima berdekatan dengan stesyen pangkalan atau kepala kluster cenderung untuk mati lebih awal kerana ketidakseimbangan trafik antara nod penerima yang akhirnya menyebabkan masalah lubang tenaga. Untuk menangani masalah ini, rumus matematik untuk mengira bilangan korona yang optimal dalam kedua-dua letak atur nod seragam rawak dan bukan seragam dicadangkan dalam rangkaian membulat yang dikenali juga sebagai rangkaian berasaskan korona. Untuk merumuskannya, penggunaan tenaga dikira pada setiap korona. Selain itu, satu lema dan dua proposisi telah dibuktikan dalam kajian ini. Berdasarkan lema ini, korona kritikal boleh dikenal pasti. Dua proposisi tersebut boleh menentukan situasi bila mana korona dalaman menghadapi lubang tenaga terbesar. Sebagai tambahan, kaedah tenaga seimbang yang dinamakan sebagai kaedah penghantaran data Julat Berselang Ubah (IVR) dicadangkan untuk memanjangkan keseluruhan tempoh hayat rangkaian dan simulasi menunjukkan korona kedua dalam mendapat kesan terbaik. Dengan kaedah IVR, dua julat penghantaran sahaja mampu meningkatkan tempoh hayat rangkaian. Dalam kajian ini juga, teknik letak atur nod geganti dicadangkan untuk menyeimbangkan penggunaan tenaga dalam korona. Dengan persamaan matematik yang dicadangkan, bilangan nod geganti untuk memaksimumkan tempoh hayat rangkaian WSN berasaskan korona dapat dikira.

TABLE OF CONTENTS

CHAPTER	TITLE	PAGE
	DECLARATION	ii
	DEDICATION	iii
	ACKNOWLEDGEMENTS	iv
	ABSTRACT	v
	ABSTRAK	vi
	TABLE OF CONTENTS	vii
	LIST OF TABLES	xi
	LIST OF FIGURES	xiii
	LIST OF ABBREVIATIONS	xv
	LIST OF SYMBOLS	xvi
	LIST OF APPENDICES	xvii
1	INTRODUCTION	1
	1.1 Overview	1
	1.2 Background of the Study	3
	1.2.1 Optimizations Strategies	4
	1.2.2 Transmission Range Control Strategies	5
	1.2.3 Using Relay Nodes Strategies	6
	1.3 Statement of the Problem	6
	1.4 Purpose of the Study	7
	1.5 Objectives of the Study	8
	1.6 Contributions of Research	8
	1.7 Scope of the Study	9
	1.8 Significance of the Study	10

1.9	Thesis Organization	11
2	LITERATURE REVIEW	12
2.1	Introduction	12
2.2	Network Lifetime	13
2.2.1	Individual Energy Consumption	14
2.2.2	Computation and Communication Overhead	15
2.2.3	Energy Balancing	15
2.3	Corona-based WSN	16
2.4	Clustering with Dynamic Cluster Head Selection	17
2.5	Sink Mobility	20
2.6	Non-uniform Node Distribution Strategies	21
2.6.1	Homogeneous Non-uniform Node distribution	21
2.6.2	Nodes Energy Provisioning	23
2.6.3	Relay Nodes Deployment Strategies	24
2.6.4	Heterogeneity on Sensors Coverage	26
2.7	Energy-Balanced Transmission Schemes	27
2.7.1	Hybrid of Multi-hop and Single-hop	27
2.7.2	On the Probabilistic Data Propagation	30
2.7.3	K-levels Transmission Range	31
2.7.4	Combination of Several Energy-Balanced Schemes	33
2.8	Determining Optimal Number of Coronas	36
2.8.1	Random Uniform Nodes Deployment	37
2.8.2	Non-uniform Nodes Deployment	39
2.9	Related Mathematical Review	40
2.9.1	Path Loss Exponent	42
2.9.2	Connectivity and Coverage in Corona-based WSN	43
2.9.3	Optimum Number of Hops in the Multi-hop Sensor Networks	45
2.9.4	Optimum Number of Cluster in a Clustered WSN	46

2.10	Summary	47
3	METHODOLOGY	48
3.1	Introduction	48
3.2	Operational Framework	49
3.2.1	Analysis of Existing Methods	50
3.2.2	Design and Development	50
3.2.3	Evaluation	54
3.2.4	Simulations	55
3.3	Summary	61
4	MATHEMATICAL MODEL FOR DETERMINING OPTIMAL NUMBER OF CORONAS	62
4.1	Introduction	62
4.2	Energy Consideration in the Coronas	63
4.3	Exponential Nodes Deployment Strategy	68
4.4	Optimal Number of Coronas	72
4.5	Lower Bound for the Energy Consumption	76
4.6	Results	78
4.7	Summary	81
5	ENERGY-BALANCED METHODS FOR MITIGATING ENERGY HOLES	83
5.1	Introduction	83
5.2	Intermittent Varied Range method	84
5.2.1	Energy Consideration	84
5.2.2	Intermittent Varied Range Ratio	85
5.3	Results	91
3.4.1	Scenario 1	92
3.4.2	Scenario 2	94
3.4.3	Scenario 3	97
5.4	Energy-Balanced Relay Nodes Deployment Method	97
5.4.1	Relay Nodes Deployment Strategy	98

5.4.2	Results	101
5.6	Summary	103
6	CONCLUSION	104
6.1	Introduction	104
6.2	Contributions	105
6.2.1	Mathematical Model for Determining Optimal Number of Coronas	105
6.2.2	Intermittent Varied Range Method	107
6.2.3	Energy-Balanced Deployment Method Using Relay Nodes	108
6.3	Direction for Future Work	109
	REFERENCES	111
	Appendices A	121-133

LIST OF TABLES

TABLE NO.	TITLE	PAGE
1.1	Research contributions	9
2.1	Summary of relay nodes / energy provisioning strategies	25
2.2	Methods that analyzed by Azad and Kamruzzaman	34
2.3	Summary of multi-level transmission range strategies	35
2.4	Summary of finding the optimal number of coronas	39
2.5	Advantages and disadvantages of the energy-balanced methods	41
2.6	Path loss exponents for different environments	42
3.1	The overall research plan	54
3.2	Simulation setup parameters	58
3.3	Nodes structure fields	60
4.1	Parameters employed in the model	63
4.2	The number of nodes in the coronas with different values of x in a network with five coronas using exponential deployment	71
5.1	Simulation setup parameters	92
5.2	Intermittent sending ratio for the simulation extracted from figure 5.3 per ten packet	92
5.3	Simulations Setup in the different scenarios	93
5.4	Network lifetime in different methods	94
5.5	Ratio of sending packet intermittently from corona 2 in the IVR method in ten packets periodically with in different network radius	96

5.6	The number of relay nodes requirement in each corona is the some examples situations	100
-----	---	-----

LIST OF FIGURES

FIGURE NO.	TITLE	PAGE
1.1	Strategies for mitigating the energy holes problem	4
1.2	Organization of the thesis	11
2.1	Relationship Among Parameters	13
2.2	Approaches for prolonging the network lifetime	14
2.3	Methods employed for increasing network lifetime	16
2.4	A corona-based WSN consisting of five coronas	17
2.5	Dynamic cluster formation during two different rounds of LEACH.	19
2.6	Types of heterogeneous nodes deployment	23
2.7	Types of the energy-balanced transmission schemes	27
2.8	Direct sending, multi-hop and fixed hop size transmission	33
2.9	Determining the optimal number of coronas	37
2.10	Introducing K-1 relay nodes between A and B to reduce energy needed	45
3.1	Operational framework of the research	49
3.2	Process of formulating the optimal number of coronas	51
3.3	Process of designing the IVR method	52
3.4	Process of designing the relay nodes deployment strategy	53
3.5	Evaluation process in the research	56
3.6	Data forwarding process Construction	57
3.7	Simulation flow chart	59
4.1	An example for the number of nodes required in the	

	exponential and q-switch deployment strategies	71
4.2	A circular network with radius R area, k coronas and the corona width R	72
4.3	Optimal number of corona for different network radius	74
4.4	Introducing $K-1$ relay nodes between A and B to reduce the energy that is required to transmit a bit	75
4.5	Similar patterns of transmissions when $x=1$	75
4.6	Optimal number of coronas for path loss equal to two	80
4.7	The ratio of lifetime prolongation in upper bound on the Lifetime	80
5.1	Effective of each corona for using intermittent varied data sending	85
5.2	A circular area in which the radius is R and the width of the corona is R .	86
5.3	Intermittent sending ratio to balance the energy in corona 1 and corona 2 in the IVR method	89
5.4	Lifetime increase ratio	90
5.5	Network Lifetime Comparison Using the IVR Method and the normal multi-hop ($n=2$)	90
5.6	Number of transmission range required in different methods	93
5.7	Optimum number of coronas with in different path loss exponent	95
5.8	Network lifetime comparison (theoretically)	95
5.9	Network life time comparison in Simulation	96
5.10	Multiply energy requirements in each corona to balance the energy throughout the network	101
5.11	Lifetime ratio by multiplying the energy using the proposed relay nodes deployment strategy	102

LIST OF ABBREVIATIONS

AI	-	Artificial Intelligence
AVHS	-	Asynchronous Variable Hop Size
BECR	-	Biased Energy Consumption Rate
BS	-	Base Station
CH	-	Cluster Head
EPND	-	Energy Proportional Node Distribution
ESPDA	-	Efficient Secure Pattern based Data Aggregation
FHS	-	Fixed Hop Size
GND	-	Geometric Node Distribution
HEED	-	Hybrid Energy-Efficient Distribution
H-AVHS	-	Heuristic Asynchronous Variable Hop Size
H-SVHS	-	Heuristic Synchronous Variable Hop Size
IVR	-	Intermittent Varied Range
LEACH	-	Low-Energy Adaptive Clustering Hierarchy
MAC	-	Medium Access Control
MISO	-	Multi-Input Single-Output
MOP	-	Multi-Objective Optimization Problem
NLM	-	Network Lifetime Maximization
NP-Hard	-	Non-deterministic Polynomial-time Hard
RN	-	Relay Node
SAPC	-	Secure Aggregation Protocol for Cluster-Based
SN	-	Sensor Node
SVHS	-	Synchronous Variable Hop Size
WSN	-	Wireless Sensor Network

LIST OF SYMBOLS

A_i	-	The energy required to be added to C_i aimed to balancing the energy
C_i	-	Corona i
E_{Ci}	-	Energy consumption in corona i
E_{elec}	-	Electronic energy consumption
E_d	-	Energy of sensing
E_{rx}	-	Reception energy
E_{Tx}	-	Transmission energy
$E_S(i)$	-	Energy consumption of each node in C_i
G_i	-	Energy consumption ratio in C_i
k	-	Number of coronas in the network
K_{opt}	-	Optimal number of coronas
L_{Ci}	-	Life time of the nodes in the corona i
l	-	Packet length
M	-	Number of nodes in the network
N_i	-	Number of nodes in corona i
n	-	Path loss exponent
R	-	Node transmission range
R_{area}	-	Network radius
α	-	Energy dissipated in the op-amp
ε_0	-	Initial energy of each sensor node
ε_R	-	Initial energy of each relay node
P	-	Nodes density

LIST OF APPENDICES

APPENDIX	TITLE	PAGE
A	Simulation Code	121

CHAPTER 1

INTRODUCTION

1.1 Overview

A wireless sensor network (WSN) consists of spatially distributed sensors to monitor environmental or physical conditions. There are various applications on WSNs such as the environmental monitoring, tracing and tracking mobile objects, telemedicine and applications for military domains. A sensor network consists of many inexpensive, sensor nodes that are small-sized and low-powered devices equipped with radio, a micro processor, a power supply, memory, and an actuator. The sensed data is sent from sensor nodes to a sink. Unlike the traditional networks, WSNs are designed based on the applications and the environments within which they are to be used. They suffer from some constraints including limited communication range, limited bandwidth and limited processing and memory resources. Thus, the WSN application is designed to be closely related to the environment to be observed.

When the energy of a node is depleted, it dies and will be disconnected from the sensor network. Thus, the application on the network cannot be fully operational. Network lifetime depends on the active nodes and connectivity. Therefore, the energy should be conserved in an efficient way.

Battery is the main power supply of the sensors. Sensors are usually deployed in unattended area and the batteries cannot be replaced easily, and rechargeable

battery might not be practical in some environments. Consequently, energy-efficient methods should be used in the networking protocols to prolong the network lifetime. Thus, the network lifetime is one of the most significant issues to be studied in WSN field.

In some situations, to save the energy and prolong the network lifetime, multi-hop transmissions are employed for transmitting the data from the sensor nodes to the sink (Bhardwaj *et al.*, 2001). However, for large-scale sensor networks, a clustering method is more suitable (Bandyopadhyay and Coyle, 2004). In a clustering architecture, each sensor node forwards data to its cluster-head (CH) and after aggregation, the CH sends data to the sink. Also data transmission from the sensors to CH or from CH to the sink can be directly or through multi-hop transmissions mode. It also depends on distance from source to destination or restriction on the radio range of the sensors (Abbasi and Younis, 2007).

In multi-hop transmission traffic pattern (or many-to-one), the energy consumption of the nodes is imbalance among the sensors and the sensor nodes which are closer to the sink/cluster-head dissipate more energy than others. Thus, they die earlier and create the energy holes. Alternatively, if the multi-hops are not employed and all sensors transmit data directly to the sink, the nodes deployed far from the sink die much faster than those deployed closer to the sink due to long distance. The energy holes partition the network and, consequently, the network cannot monitor completely and this problem reduces considerably the network lifetime. Therefore, some techniques are required to avoid the energy holes problems. Among current techniques for mitigating energy holes include transmission range control techniques, using mobile sink, and using non-uniform node deployment strategy (Xiaobing *et al.*, 2008).

By mitigating the energy holes, the network lifetime will be increased. In addition, to prolong the network lifetime energy efficient designs for the network layers are needed. The wireless sensor network protocols consist of five layers: physical layer, data-link layer, network layer, transport layer, and application layer that are designed for coverage, localization, synchronization, data aggregation, data compression, security and storage. Designing and implementing efficient algorithm

and communication protocol in the sensor network layers protocols could also increase the total network lifetime.

1.2 Background of the Study

In many-to-one pattern, the nodes located around the sink relay the data of other sensor nodes and have heavier traffic loads. Therefore, the nodes nearer to the sink consume more energy than others and their energy depletes faster; this problem is known as an energy hole problem (Xiaobing *et al.*, 2008) and the place is named hot spot area (Perillo *et al.*, 2005). When the energy hole appears, data cannot be sent from other sensors to the sink even though most the sensors still have energy. Thus, prematurely the network lifetime ends and considerable amount of energy is wasted. Lian *et al.* (2006) found that up to 90% of energy is left unused when the nodes are uniformly distributed due to the hot spot and energy hole problem.

There are some parameters that have effect on the energy hole problem and the network lifetime. These include the width of each corona, the number of coronas, the node transmission range, the nodes distribution strategy and the network area. Based this parameters, there are many approaches to mitigate the energy hole problem including the node or sink mobility, non-uniform sensor distribution strategy, adjustable transmission range, dynamic energy balancing, using relay nodes and optimization (see figure 1.1) and the most of the strategies are modeled by corona-based model. In the mobility strategy, the mobile sink moves to hot spot places in order to avoid the energy hole problem (Wu and Chen, 2007, Marta and Cardei, 2008).

Some strategies have been proposed to decrease the energy hole problem through non-uniform node deployment strategies (Lian *et al.*, 2006, Liu *et al.*, 2006, Xiaobing *et al.*, 2008). In a non-uniform distribution strategy, additional sensors are located in the area that have energy holes problem in order to prolong the lifetime of the network (Xiaobing *et al.*, 2006, Ferng *et al.*, 2011).

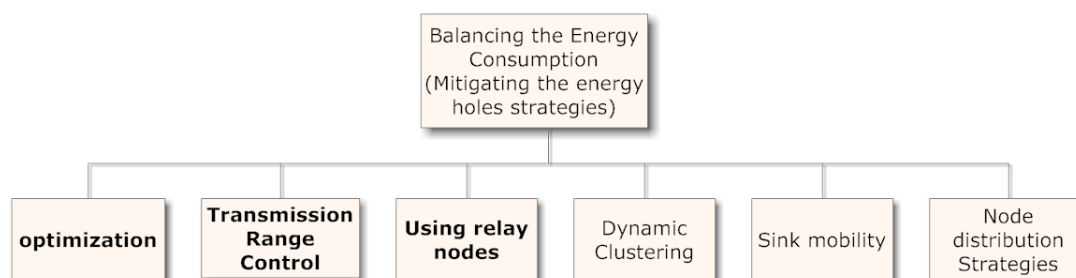


Figure 1-1. Strategies for mitigating the energy holes problem

And in the relay nodes strategy, some relay nodes are located in the hot spot area for mitigating the energy hole problem (Wang *et al.*, 2006, Quanhong *et al.*, 2007). Perillo *et al.* (2004) showed that the transmission range control could affect on the network lifetime and the strategy of adjusting transmission range is used for balancing the energy and avoiding energy hole (Cardei *et al.*, 2005; Olariu and Stojmenovic, 2006; Perillo *et al.*, 2004; Song *et al.*, 2009; Tang *et al.*, 2006). Also, many dynamic algorithms have been designed to balance the energy consumption in the network. The dynamic algorithms usually are used in clustered WSN, e.g. LEACH (Heinzelman *et al.*, 2002), MLEACH (Xiangning and Yulin, 2007) and HEED (Ossama Younis, 2004), UCR (Chen *et al.*, 2009). In this strategies, the cluster heads are rotated and changed their tasks among the other sensors from time to time, for balancing the energy depletion and mitigating the energy hole problem. In addition, by optimization of the parameters that has effect on the energy holes problem and the network life time, the mitigation of energy holes problem could be achieved (Olariu and Stojmenovic, 2006). This thesis is focused on improvement of the strategies including the optimization strategies, transmission range control strategies and using relay nodes strategies in the corona-based WSN.

1.2.1 Optimization Strategies

Optimizing some parameters such as width of each corona, number of coronas, node transmission range, nodes distribution strategy and the network area, have effect on mitigating the energy hole problem. Optimal number of the coronas for random uniform nodes deployment has been formulated by Olariu and

Stojmenovic (2006). However, for non-uniform node deployment the optimal number of coronas has been obtained from some numerical algorithms and there is no mathematical formulation. Haibo and Hong (2009) computed the optimal number of corona by the Simulated Annealing algorithm for their non-uniform strategy. Xiaobing *et al.* (2008) used the uniform equation of Olariu and Stojmenovic (2006) for finding the optimal number of corona approximately in their proposed strategy. In this thesis, a mathematical formula to calculate the optimal number of coronas in both random uniform and non-uniform deployment nodes is proposed. To formulate it, the energy consumption was calculated for each corona and a lemma and two propositions have been proven.

1.2.2 Transmission Range Control Strategies

Energy-balanced transmission schemes are a type of energy-balanced schemes such that controlling the transmission range helps to mitigating the energy holes problem. Many researchers attempted to find a solution for the energy-balanced transmission schemes in WSNs (Charilaos *et al.*, 2006, Jarry *et al.*, 2006 Azad and Kamruzzaman, 2011, Thanigaivelu and Murugan, 2012). These strategies are not feasible because they need many different transmission ranges and that is the main drawback of the strategies. In this research, a new strategy is proposed based on only two transmission ranges such that the proposed strategy can be feasible and only two transmission ranges could increase the network lifetime significantly. Accordingly, it has analytically obtained the corona that has the most effect for using transmission range control (second innermost corona is the most effective) and the nodes in the second innermost corona transfer data with a range of R or $2R$.

1.2.3 Using Relay Nodes Strategies

Using the relay nodes in the network significantly affect the lifetime and connectivity of WSN systems (Wang *et al.*, 2006, Quanhong *et al.*, 2007, Ammari and Das, 2008, Halder *et al.*, 2011). Moez *et. al.* (2007) investigated the relationship between the network lifetime and the network density. Ammari (2008) proposed a sensor deployment strategy based on energy heterogeneity with a goal that all the sensors deplete their energy at the same time. In this research, a new relay nodes deployment technique is proposed to balance the energy consumption in the coronas. In the relay node deployment scheme, by adding the extra nodes to relay, the energy balancing will be achieved and relay nodes deployed with priority from interior corona. In addition, relationship between the network lifetime and needed extra energy and relationship between the network lifetime and the number of relay nodes that are required, has been formulated. Using the proposed mathematical equations, the number of relay nodes for maximizing the lifetime of corona-based WSNs could be calculated.

1.3 Statement of the Problem

In the corona-based networks, nodes deployed closer to the sink consume more energy and die sooner than other nodes. This ultimately leads to what is known as energy holes. The energy holes problem significantly reduces the network life time. Many approaches were discussed in the research background for mitigating the energy hole problem. In the optimization strategies, there is no mathematical model to identify the optimum number of coronas to maximize the network lifetime in non-uniform deployment strategy. The questions related to this problem are as follows:

- (i) What are the parameters that provide significant effects to the network lifetime in corona-based WSN?
- (ii) How to formulate the optimum number of coronas in both the uniform and the non-uniform deployment in corona-based WSN?

- (iii) How to find upper bound on the lifetime of corona-based WSN?

In mitigating energy holes problem strategies, the transmission range control strategies are not feasible (Xiaobing *et al.*, 2008), the questions related to this problem are as follows:

- (iv) How to develop a feasible method using adjustable transmission range for the mitigation of energy holes problem?
- (v) How to mitigate energy hole using only two different transmission ranges?
- (vi) How much is the best ratio to transmit data to balance energy in the coronas?

Another approach for mitigating the energy hole problem is using relay nodes. Currently there is no formula for relationship between the network lifetime and the initial energy for extending the network lifetime maximally. The questions related to this problem are as follows:

- (vii) What is the relationship between energy (capacity of batteries) and lifetime in a corona-based WSN.
- (viii) What is the best deployment strategy for relay nodes to maximize the network lifetime in corona-based WSN?

1.4 Purpose of the Study

This research aims to mitigate energy holes problem by proposing several methods in a corona-based WSN. This study is conducted to analytically formulate the optimum number of coronas generally in both random uniform and non-uniform node deployment, propose a feasible method based on the transmission range control, and propose a relay node deployment strategy in order to mitigate the energy holes problem.

1.5 Objectives of the Study

The main aim of this research is to mitigate energy hole in corona-based WSNs. Accordingly, the research objectives are as follow:

- I) To analytically formulate the optimum number of coronas in a corona-based wireless sensor network in both random uniform and non-uniform node deployments.
- II) To design and implement a feasible method for mitigating the energy holes problem based on the transmission range control (using adjustable transmission range) in the corona-based WSN.
- III) To design and implement a relay node deployment strategy to mitigate energy holes problem in corona-based WSN such that by adding a relay node, the network life time could be extended maximally.

1.6 Contributions of Research

The first part of this research contributions is formulas to obtain the optimum number of coronas in the corona-based WSN. One lemma, two propositions, two theorems, an exponential non-uniform node deployment and a formula to acquire lower bound of energy consumption of the first corona for obtaining the upper bound of the network lifetime have been proposed (see Table 1.1).

Another contribution of this research is a novel feasible method to mitigate energy holes problem based on transmission range control. The contribution is named Intermittent Varied Range (IVR) method to balance the energy consumption in the interior corona (corona 1) and second interior corona (corona 2). In addition, finding the ratio of intermittent data transmission in the method is the second part of these contributions.

Table 1.1: Research contributions

Chapter Number		Contribution
Chapter 4	Optimum number of coronas	A lemma and two propositions to formulate optimum number of corona.
		An exponential non-uniform deployment of nodes.
		A formula for identifying the optimum number of corona generally in random uniform and non-uniform node deployment (theorem 1)
		The upper bound of the lifetime in the first corona has been calculated.
		A formula for identifying the optimum number of corona in uniform corona-based WSN with adjustable transmission range (theorem 2)
Chapter 5	IVR Method	The ratio of the intermittent data sending for energy balancing in the coronas has been found.
		The IVR method to mitigate energy holes feasibly.
	Non-uniform Relay Nodes deployment method	A new solution for finding the initial energy (battery capacity) required for a node in each corona to maximize the network lifetime
		An equation to relay node deployment by adding a number of relay node and maximum prolonging the network lifetime

Finally, a non-uniform relay node strategy to mitigate the energy holes problem has been proposed. The strategy suggests a method to deploy relay nodes such that by adding a relay node, the network lifetime could be prolonged maximally. In this strategy relay nodes deployed with a priority from interior corona to outer coronas. In addition, the initial energy required for a node in each corona have been obtained with new solution for maximizing the network lifetime (see Table 1.1).

1.7 Scope of the Study

In this research, The network is the corona-based WSN (Sink/Cluster-head located at the center of the circle) with a radius of R_{area} . The circular area is divided into k adjacent coronas with a fixed heterogeneous sink and the sink is assumed to be

located at the center of the circle and the width of each corona is R . Nodes in corona C_i (C_i denotes for i th corona) generates and sends l bits data per unit of time to corona ($C_{i-1} | i \geq 2$) however in the IVR method, nodes in C_2 can send data with transmission range of R and $2R$. Other research scopes are as follow:

- (i) The transmission range of each node is R ; however, in IVR method, two adjustable transmission range (R and $2R$) are assumed for each node.
- (ii) Connectivity requirement on the network is assumed and data aggregation has not assumed.
- (iii) The area is in environment with the path lost exponent n and the communication environment is contention-and error-free.
- (iv) Each node has ε_0 initial energy, and the sink/cluster-head has no energy limitation.

1.8 Significance of the Study

This research is conducted to find a way for mitigating the energy hole in corona-based WSN. There are many ideas to mitigate the energy hole but none of them formulates optimum number of coronas in non-uniform nodes deployment. In addition, there is no any feasible method based on energy-balanced transmission scheme (using adjustable transmission range), due to the fact that usually the real node has not many different transmission ranges. The IVR method in this research is a new feasible energy-balanced transmission method for mitigating the energy holes problem using only two levels of adjustable transmission range. Since there are real sensor nodes with two different transmission range, IVR method could be a feasible method. IVR can also be applied to multi-hop routing. In addition, in this research, a new real node deployment strategy by maximum increasing the network life time has been proposed.

1.9 Thesis Organization

Chapter 1 is an introduction to the thesis and the research problem. Chapter 2 reviews the literature about the energy holes and related works conducted to solve this problem. In Chapter 3, the research methodology is presented. In Chapter 4 the optimum number of coronas is formulated in both uniform and non-uniform sensor deployments. Chapter 5 proposes and evaluates two new methods to mitigate the energy holes problem. Finally, Chapter 6 concludes the research including contributions and many suggestions for future works. The thesis organization is shown in Figure 1.2.

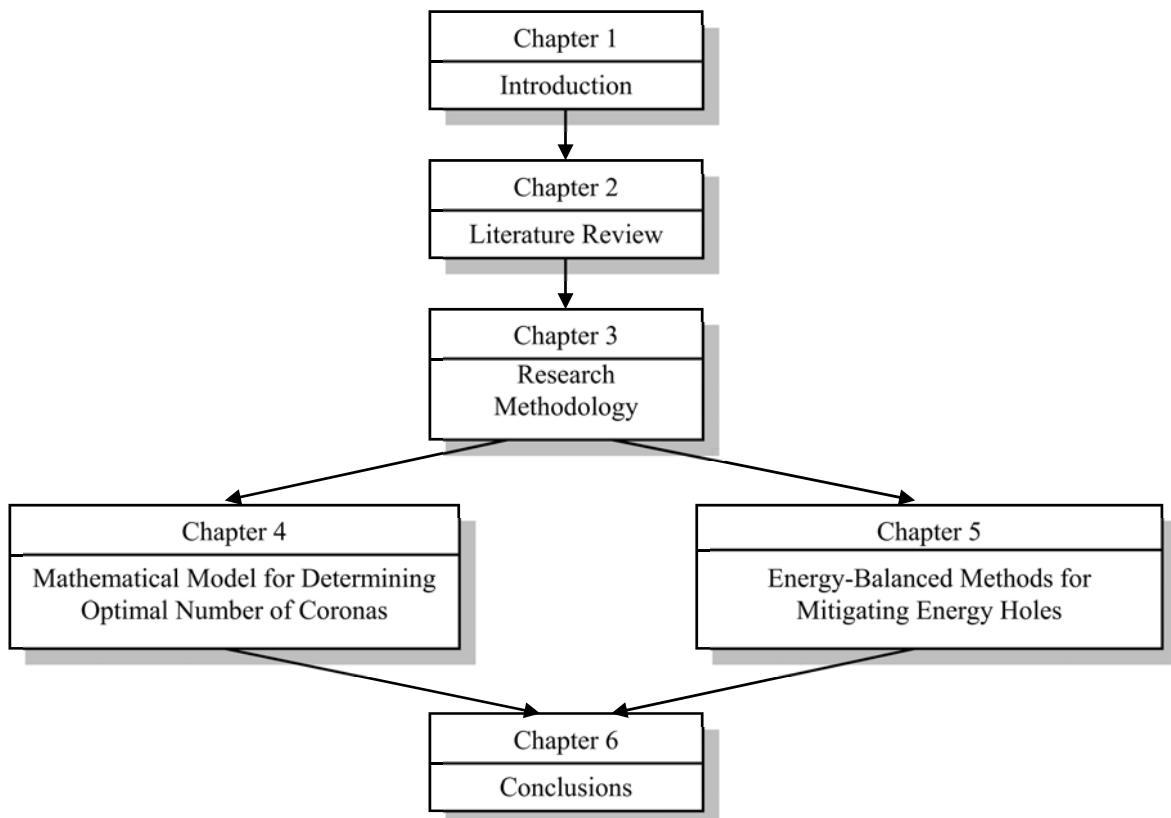


Figure 1.2: Organization of the thesis

REFERENCES

- Akham, H., Azdemir, S., Nair, P., Muthuavina, D. and Ozgur Sanli, H. (2006). Energy-Efficient Secure Pattern Based Data Aggregation for Wireless Sensor Networks. *Computer Communications*, 29, 446-455.
- Abbasi, A. A. and Younis, M. (2007). A Survey on Clustering Algorithms for Wireless Sensor Networks. *Computer Communications*, 30, 2826-2841.
- Alzaid, H., Foo, E. and Nieto, J. G. (2008). Secure Data Aggregation in Wireless Sensor Network: a Survey. *In: Proceedings of the sixth Australasian conference on Information security-Volume 81, 2008*. Australian Computer Society, Inc., 93-105.
- Ammari, H. M. and Das, S. K. (2008). Promoting Heterogeneity, Mobility, and Energy-Aware Voronoi Diagram in Wireless Sensor Networks. *Parallel and Distributed Systems, IEEE Transactions on*, 19, 995-1008.
- Anastasi, G., Conti, M., Di Francesco, M. and Passarella, A. (2009). Energy conservation in wireless sensor networks: A survey. *Ad Hoc Networks*, 7, 537-568.
- Atiq U, R., Hasbullah, H. and Najm Us, S. (2012). Impact of Gaussian deployment strategies on the performance of wireless sensor network. *In: Computer and Information Science (ICCIS), 2012 International Conference on, 12-14 June 2012*. 771-776.
- Azad, A. K. M. and Kamruzzaman, J. (2011). Energy-Balanced Transmission Policies for Wireless Sensor Networks. *Mobile Computing, IEEE Transactions on*, 10, 927-940.
- Banyopadhyay, S. and Coyle, E. J. (2004). Minimizing Communication Costs in Hierarchically-Clustered networks of Wireless Sensors. *Computer Networks*, 44, 1-16.

- Bekara, C., Laurent-Maknavicius, M. and Bekara, K. (2007). SAPC: A Secure Aggregation Protocol for Cluster-Based Wireless Sensor Networks. *Mobile Ad-Hoc and Sensor Networks*, 784-798.
- Bharwaj, M. and Chandrakasan, A. P. (2002). Bounding the Lifetime of Sensor Networks Via Optimal Role Assignments. *In: INFOCOM 2002. Twenty-First Annual Joint Conference of the IEEE Computer and Communications Societies. Proceedings. IEEE, 2002.* 1587-1596 vol.3.
- Bharwaj, M., Garnett, T. and Chandrakasan, A. P. (2001). Upper Bounds on the Lifetime of Sensor Networks. *Communications, 2001. ICC 2001. IEEE International Conference on.*
- Brazil, M., Ras, C. and Thomas, D. (2013). Relay Augmentation for Lifetime Extension of Wireless Sensor Networks. *arXiv preprint arXiv:1301.4728.*
- Cardei, M., Wu, J., Lu, M. and PERVAIZ, M. O. (2005). Maximum Network Lifetime in Wireless Sensor Networks with Adjustable Sensing Ranges. *In, 2005. Ieee, 438-445 Vol. 3.*
- Charilaos, E., Sotiris, N. and Jose, R. (2006). Energy Balanced Data Propagation in Wireless Sensor Networks. *Wirel. Netw., 12,* 691-707.
- Chen, G., Li, C., Ye, M. and Wu, J. (2009). An Unequal Cluster-Based Routing Protocol in Wireless Sensor Networks. *Wireless Networks, 15,* 193-207.
- Chen, Y., Li, Q., Fei, L. and Gao, Q. (2012). Mitigating energy holes in wireless sensor networks using cooperative communication. *In: Personal Indoor and Mobile Radio Communications (PIMRC), 2012 IEEE 23rd International Symposium on, 9-12 Sept. 2012.* 857-862.
- Chen, Y. and Zhao, Q. (2005). On the Lifetime of Wireless Sensor Networks. *Communications Letters, IEEE, 9,* 976-978.
- Cheng, P., Chuah, C. N. and Liu, X. (2004). Energy-Aware Node Placement in Wireless Sensor Networks. *In: Global Telecommunications Conference, 2004. GLOBECOM'04. IEEE, 2004. IEEE, 3210-3214.*
- Demirkol, I., Ersoy, C. and Alagoz, F. (2006). MAC Protocols for Wireless Sensor Networks: a Survey. *Communications Magazine, IEEE, 44,* 115-121.
- Dietrich, I. and Dressler, F. (2009). On the Lifetime of Wireless Sensor Networks. *ACM Trans. Sen. Netw., 5,* 1-39.
- Esseghir, M., Bouabdallah, N. and Pujolle, G. (2007). Energy Provisioning Model for Maximizing Wireless Sensor Network Lifetime. *In: Global Information*

- Infrastructure Symposium, 2007. GIIS 2007. First International, 2007. IEEE, 80-84.
- Fahmy, Y. A. S. (2004). Distributed Clustering in Ad Hoc Sensor Networks: A Hybrid, Energy-Efficient Approach. *IEEE Transactions*.
- Ferentinos, K. P. and Tsiligiridis, T. A. (2007). Adaptive Design Optimization of Wireless Sensor Networks Using Genetic Algorithms. *Computer Networks*, 51, 1031-1051.
- Ferng, H., Hadiputro, M. and Kurniawan, A. (2011). Design of Novel Node Distribution Strategies in Corona-Based Wireless Sensor Networks. *Mobile Computing, IEEE Transactions on*, 1-1.
- Fragouli, C., LE Boudec, J. Y. and Widmer, J. (2006). Network Coding an Instant Primer. *ACM SIGCOMM Computer Communication Review*, 36, 63-68.
- Gatzianas, M. and Georgiadis, L. (2008). A Distributed Algorithm for Maximum Lifetime Routing in Sensor Networks with Mobile Sink. *Wireless Communications, IEEE Transactions on*, 7, 984-994.
- Giridhar, A. and Kumar, P. (2005). Maximizing the Functional Lifetime of Sensor Networks. *In*, 2005. IEEE Press, 2.
- Guo, W., Liu, Z. and Wu, G. (2003). An Energy-Balanced Transmission Scheme for Sensor Networks. *In: Proceedings of the 1st international conference on Embedded networked sensor systems*, 2003. ACM, 300-301.
- Gupta, G. and Younis, M. (2003). Fault-Tolerant Clustering of Wireless Sensor Networks. *In: Wireless Communications and Networking. WCNC 2003*. IEEE, 20-20 March 2003. 1579-1584 vol.3.
- Gupta, P. and Kumar, P. R. (1998). Critical Power for Asymptotic Connectivity In Decision and Control, 1998. Proceedings of the 37th IEEE Conference on, 1998. 1106-1110 vol.1.
- Haibo, Z. and Hong, S. (2009). Balancing Energy Consumption to Maximize Network Lifetime in Data-Gathering Sensor Networks. *Parallel and Distributed Systems, IEEE Transactions on*, 20, 1526-1539.
- Halder, S., Ghosal, A. and Bit, S. D. (2011). A Pre-Determined Node Deployment Strategy to Prolong Network Lifetime in Wireless Sensor Network. *Computer Communications*, 34, 1294-1306.

- Heinzelman, W. B., Chandrakasan, A. P. and Balakrishnan, H. (2002). An Application-Specific Protocol Architecture for Wireless Microsensor Networks. *Wireless Communications, IEEE Transactions on*, 1, 660-670.
- Heo, J., Hong, J. and Cho, Y. (2009). EARQ: Energy Aware Routing for Real-Time and Reliable Communication in Wireless Industrial Sensor Networks. *Industrial Informatics, IEEE Transactions on*, 5, 3-11.
- HOSSAIN, A., CHAKRABARTI, S. and BISWAS, P. (2013). Equal energy dissipation in wireless image sensor network: A solution to energy-hole problem. *Computers and Electrical Engineering*, 39, 1789-1799.
- Hou, Y. T., Shi, Y., Sherail, H. D. and Midkiff, S. F. (2005). On Energy Provisioning and Relay Node Placement for Wireless Sensor Networks. *Wireless Communications, IEEE Transactions on*, 4, 2579-2590.
- Iranli, A., Maleki, M. and Pedram, M. (2005). Energy Efficient Strategies for Deployment of a Two-Level Wireless Sensor Network. *In: Proceedings of the 2005 international symposium on Low power electronics and design*, 2005. ACM, 233-238.
- Jae-joon, L., Krishnamachari, B. and Kuo, C. C. J. (2004). Impact of Heterogeneous Deployment on Lifetime Sensing Coverage in Sensor Networks. *In: Sensor and Ad Hoc Communications and Networks*, 2004. IEEE SECON 2004. First Annual IEEE Communications Society Conference on, 4-7 Oct. 2004 2004. 367-376.
- Jarry, A., Leone, P., Powell, O. and Rolim, J. (2006a). An Optimal Data Propagation Algorithm for Maximizing the Lifespan of Sensor Networks. *Distributed Computing in Sensor Systems*, 405-421.
- Jennifer Yick, B. M., Dipak Ghosal (2008). Wireless Sensor Network Survey. *ELSEVIER*.
- Jing, L., Kefel, L., Xiaodong, C. and Murthi, M. N. (2009). Regenerative Cooperative Diversity With Path Selection and Equal Power Consumption in Wireless Networks. *Wireless Communications, IEEE Transactions on*, 8, 3926-3932.
- Jiucan, Z., Song, C., Sharif, H. and Alahmad, M. (2009). A Battery-Aware Deployment Scheme for Cooperative Wireless Sensor Networks. *In: Global Telecommunications Conference. GLOBECOM 2009. IEEE*, Nov. 30 2009-Dec. 4 2009. 1-5.

- Johnson, M., Healy, M., Van De Ven, P., Hayes, M. J., Nelson, J., Newe, T. and Lewis, E. (2009). A Comparative Review of Wireless Sensor Network Mote Technologies. *In: Sensors, 2009 IEEE, 25-28 Oct. 2009* 2009. 1439-1442.
- Kenan, X., Hassanein, H., Takahara, G. and Quanhong, W. (2010). Relay Node Deployment Strategies in Heterogeneous Wireless Sensor Networks. *Mobile Computing, IEEE Transactions on*, 9, 145-159.
- Koushanfar, F., Taft, N. and Potkonjak, M. (2006). Sleeping Coordination for Comprehensive Sensing Using Isotonic Regression and Domatic Partitions.
- Kredo, K. and Mohapatra, P. (2007). Medium Access Control in Wireless Sensor Networks. *Computer Networks*, 51, 961-994.
- Leone, P., Nikolettseas, S. and Rolim, J. (2010). Stochastic Models and Adaptive Algorithms for Energy Balance in Sensor Networks. *Theory of Computing Systems*, 47, 433-453.
- Leone, P. and Rolim, J. (2004). Towards a Dynamical Model for Wireless Sensor Networks. *Algorithmic Aspects of Wireless Sensor Networks*, 98-108.
- Li, H., Liu, Y., Chen, W., Jia, W., Li, B. and Xiong, J. (2013). COCA: Constructing Optimal Clustering Architecture to Maximize Sensor Network Lifetime. *Computer Communications*, 36, 256-268.
- Lian, J., Chen, L., Naik, K., Otzu, T. and Agnew, G. (2004). Modelig and Enhancing the Data Capacity of Wireless Sensor Networks. *IEEE Monograph on Sensor Network Operations*.
- Lian, J., Naik, K. and Agnew, G. B. (2006). Data Capacity Improvement of Wireless Sensor Networks Using Non-uniform Sensor Distribution. *International Journal of Distributed Sensor Networks*, 2, 121-145.
- Lindsey, S., Raghavendra, C. and Sivalingam, K. M. (2002). Data Gathering Algorithms in Sensor Networks Using Energy Metrics. *Parallel and Distributed Systems, IEEE Transactions on*, 13, 924-935.
- Lindsey, S. and Raghavendra, C. S. (2002). PEGASIS: Power-Efficient Gathering in Sensor Information Systems. *In: Aerospace Conference Proceedings, 2002. IEEE, 2002. 3-1125-3-1130 vol.3*.
- LIN, F.-T., SHIU, L.-C., LEE, C.-Y. and YANG, C.-S. (2013). A method to analyze the effectiveness of the holes healing scheme in wireless sensor network. *International Journal of Distributed Sensor Networks*, 2013.

- Liu, X. and Mahapatra, P. (2005). On the Deployment of Wireless Sensor Nodes. *In: Proceedings of the 3rd International Workshop on Measurement, Modeling, and Performance Analysis of Wireless Sensor Networks, in Conjunction with the 2nd Annual International Conference on Mobile and Ubiquitous Systems, 2005.*
- LIU, A., LIU, Z., NURUDEEN, M., JIN, X. and CHEN, Z. (2013). An elaborate chronological and spatial analysis of energy hole for wireless sensor networks. *Computer Standards and Interfaces*, 35, 132-149.
- LIU, T. (2013). Avoiding Energy Holes to Maximize Network Lifetime in Gradient Sinking Sensor Networks. *Wireless Personal Communications*, 70, 581-600.
- LIU, Y., NGAN, H. and NI, L. M. 2006. Power-aware node deployment in wireless sensor networks. *In*, 2006. IEEE, 8 pp.
- Liu, Z., Xiu, D. and Guo, W. (2005). An Energy-Balanced Model for Data Transmission in Sensor Networks. *In: Vehicular Technology Conference, 2005. VTC-2005-Fall. 2005 IEEE 62nd, 2005. IEEE, 2332-2336.*
- Luo, J. and Hubaux, J. P. Year. Joint Mobility and Routing for Lifetime Elongation in Wireless Sensor Networks. (2005). *In: INFOCOM 2005. 24th Annual Joint Conference of the IEEE Computer and Communications Societies. Proceedings IEEE, 2005. IEEE, 1735-1746.*
- Luo, J., Panchard, J., Piorowski, M., Grossglauser, M. and Hubaux, J. P. (2006b). Mobiroute: Routing Towards a Mobile Sink for Improving Lifetime in Sensor Networks. *Distributed Computing in Sensor Systems*, 480-497.
- MA, G. and TAO, Z. (2013). A Nonuniform Sensor Distribution Strategy for Avoiding Energy Holes in Wireless Sensor Networks. *International Journal of Distributed Sensor Networks*, 2013.
- Mak, N. H. and Seah, W. K. G. (2009). How Long is the Lifetime of a Wireless Sensor Network? *In: Advanced Information Networking and Applications, 2009. AINA'09. International Conference on, 2009. IEEE, 763-770.*
- Bhardwaj, T. G., Ananthap P. Chandrakasan 2001. Upper Bounds on the Lifetime of Sensor Networks. *IEEE*.
- Marta, M. and Cardei, M. (2008). Using Sink Mobility to Increase Wireless Sensor Networks Lifetime. *In: World of Wireless, Mobile and Multimedia Networks, International Symposium on a, 2008. IEEE, 1-10.*

- Mhatre, V. and Rosenberg, C. (2004). Design Guidelines for Wireless Sensor Networks: Communication, Clustering and Aggregation. *Ad Hoc Networks*, 2, 45-63.
- Mhatre, V. P., Rosenberg, C., Kofman, D., Mazumdar, R. and Shroff, N. (2005). A Minimum Cost Heterogeneous Sensor Network With a Lifetime Constraint. *Mobile Computing, IEEE Transactions on*, 4, 4-15.
- Olariu, S. and Stomenovic, I. (2006). Design Guidelines for Maximizing Lifetime and Avoiding Energy Holes in Sensor Networks With Uniform Distribution and Uniform Reporting. *In*, 2006. 24-25.
- Ossama Younis, S. F. (2004). HEED: A Hybrid, Energy-Efficient, Distributed Clustering Approach for Ad-hoc Sensor Networks. *IEEE Transactions on Mobile Computing*.
- Perillo, M., Cheng, Z. and Heinzelman, W. (2004). On the Problem of Unbalanced Load Distribution in Wireless Sensor Networks. *In*, 2004. IEEE, 74-79.
- Perillo, M., Cheng, Z. and Heinzelman, W. (2005). An Analysis of Strategies for Mitigating the Sensor Network Hot Spot Problem. *In: Mobile and Ubiquitous Systems: Networking and Services*, 2005. MobiQuitous 2005. The Second Annual International Conference on, 17-21 July 2005 2005. 474-478.
- Perillo, M. and Heinzelman, W. (2009). An Integrated Approach to Sensor Role Selection. *Mobile Computing, IEEE Transactions on*, 8, 709-720.
- Powell, O., Leone, P. and Rolim, J. (2007). Energy Optimal Data Propagation in Wireless Sensor Networks. *Journal of Parallel and Distributed Computing*, 67, 302-317.
- Pradhan, S. and Ramchandran, K. (2003). Distributed Source Coding Using Syndromes (DISCUS): Design and Construction. *Information Theory, IEEE Transactions on*, 49, 626-643.
- Quanhong, W., Kenan, X., Takahara, G. and Hassanein, H. (2006). On Lifetime-Oriented Device Provisioning in Heterogeneous Wireless Sensor Networks: Approaches and Challenges. *Network, IEEE*, 20, 26-33.
- Quanhong, W., Kenan, X., Takahara, G. and Hassanein, H. (2007). Transactions Papers - Device Placement for Heterogeneous Wireless Sensor Networks: Minimum Cost with Lifetime Constraints. *Wireless Communications, IEEE Transactions on*, 6, 2444-2453.

- Rappaport., T. (1996). *Wireless Communications: Principles and Practice*. Englewood Cliffs, NJ: Prentice-Hall.
- Ritesh, M., Shuguang, C., Sanjay, L. and Andrea, J. G. (2007). Modeling and Optimization of Transmission Schemes in Energy-Constrained Wireless Sensor Networks. *IEEE/ACM Trans. Netw.*, 15, 1359-1372.
- Santi, P. (2005). Topology Control in Wireless Ad hoc and Sensor Networks. *ACM Computing Surveys (CSUR)*, 37, 164-194.
- Schurgers, C., Tsiatsis, V. and Srivastava, M. B. (2002). STEM: Topology Management for Energy Efficient Sensor Networks. *In: Aerospace Conference Proceedings, 2002*. IEEE, 3-1099-3-1108 vol. 3.
- Shakkottai, S., Srikant, R. and Shroff, N. (2003). Unreliable Sensor Grids: Coverage, Connectivity and Diameter. *INFOCOM 2003*.
- Sheldon, M., Deji, C., Nixon, M. and Mok, A. K. (2005). A practical Approach to Deploy Large Scale Wireless Sensor Networks. *In: Mobile Adhoc and Sensor Systems Conference, 2005*. IEEE International Conference on, 7-7 Nov. 2005 2005. 8 pp.-250.
- Shio Kumar, M P Singh and Singh, D. K. (2010). A Survey of Energy-Efficient Hierarchical Cluster-Based Routing in Wireless Sensor Networks. *Int. J. of Advanced Networking and Applications*.
- Song, C., Liu, M., Cao, J., Zheng, Y., Gong, H. and Chen, G. (2009). Maximizing Network Lifetime Based on Transmission Range Adjustment in Wireless Sensor Networks. *Computer Communications*, 32, 1316-1325.
- Soro, S. and Heinzelman, W. B. (2005). Prolonging the Lifetime of Wireless Sensor Networks Via Unequal Clustering. *In: Parallel and Distributed Processing Symposium, 2005*. Proceedings. 19th IEEE International, 4-8 April 2005 2005. 8 pp.
- Suganthi, K. and Sundaram, B. V. (2012). A Constraint Based Relay Node Deployment in Heterogeneous Wireless Sensor Networks for Lifetime Maximization. *In: Advanced Computing (ICoAC), 2012 Fourth International Conference on, 13-15 Dec. 2012*. 1-6.
- Tang, C. and Raghavendra, C. (2004). Compression Techniques for Wireless Sensor Networks. *Wireless sensor networks*, 207-231.
- Tang, J., Hao, B. and Sen, A. (2006). Relay Node Placement in Large Scale Wireless Sensor Networks. *Computer Communications*, 29, 490-501.

- Thanigaivelu, K. and Murugan, K. (2012). K-level Based Transmission Range Scheme to Alleviate Energy Hole Problem in WSN. *In: Proceedings of the Second International Conference on Computational Science, Engineering and Information Technology*, 2012. ACM, 476-483.
- Wang, Q., Xu, K., Takahara, G. and Hassanein, H. (2006). On Lifetime-Oriented Device Provisioning in Heterogeneous Wireless Sensor Networks: Approaches and Challenges. *Network, IEEE*, 20, 26-33.
- Wang, Y. and Jing, Y. (2012). An Optimal Energy Balance Strategy to Maximize Network Lifetime in Wireless Sensor Networks*. *Journal of Computational Information Systems*, 8, 107-114.
- Wu, X. and Chen, G. (2007). Dual-sink: Using Mobile and Static Sinks for Lifetime Improvement in Wireless Sensor Networks. *In: Computer Communications and Networks*, 2007. ICCCN 2007. Proceedings of 16th International Conference on, 2007. IEEE, 1297-1302.
- Xiangning, F. and Yulin, S. (2007). Improvement on LEACH Protocol of Wireless Sensor Network. *In*, 2007. IEEE, 260-264.
- Xiaobing, W., Guihai, C. and Das, S. K. 2008. Avoiding Energy Holes in Wireless Sensor Networks with Nonuniform Node Distribution. *Parallel and Distributed Systems, IEEE Transactions on*, 19, 710-720.
- Xiaobing, W., Guihai, C. and Sajal, K. D. (2006). On the Energy Hole Problem of Nonuniform Node Distribution in Wireless Sensor Networks. *In: Mobile Adhoc and Sensor Systems (MASS)*, 2006 IEEE International Conference on, Oct. 2006. 180-187.
- Yadav, R., Varma, S. and Malaviya, N. (2009). A Survey of MAC Protocols for Wireless Sensor Networks. *UbiCC journal*, 4, 827-833.
- Ye, W., Heidemann, J. and Estrin, D. (2002). An energy-Efficient MAC Protocol for Wireless Sensor Networks. *In: INFOCOM 2002. Twenty-First Annual Joint Conference of the IEEE Computer and Communications Societies. Proceedings.* IEEE, 2002. IEEE, 1567-1576.
- Yunhual, L., Hoilun, N. and Ni, L. M. 2006. Power-Aware Node Deployment in Wireless Sensor Networks. *In: Sensor Networks, Ubiquitous, and Trustworthy Computing*, 2006. IEEE International Conference on, 5-7 June 2006 2006. 8 pp.

Zhang, H., Shen, H. and Tan, Y. (2007). Optimal Energy Balanced Data Gathering in Wireless Sensor Networks. *In: Parallel and Distributed Processing Symposium. IPDPS 2007. IEEE International, 26-30 March 2007 2007.* 1-10.