

THERMODYNAMICS EFFECTS ON THE COMPRESSION DYNAMICS OF  
SOFT X-RAY EMISSION IN PLASMA FOCUS

NATASHAH BINTI ABDUL RASHID

A thesis submitted in fulfilment of the  
requirements for the award of the degree of  
Doctor of Philosophy (Physics)

Faculty of Science  
Universiti Teknologi Malaysia

NOVEMBER 2014

*To my beloved parents & family*

## ACKNOWLEDGEMENT

First of all I am greatly thankful to my ALLAH Almighty for enabling me to carry out this research.

I wish to express my sincere gratitude to my respected supervisor Prof. Dr. Jalil bin Ali, Prof. Dr. Lee Sing and Prof. Sor Heoh Saw for their valuable advises, guidance, considerate comments, as well as their continuous encouragement and tremendous motivation along my research period. Their kind supports have helped me accomplished and present this thesis in the current form.

I would like to express my special appreciation to Dr. Kashif Tufail Chaudhary and all colleagues, particularly Saiful Najmee, Ong Shu Teik, Nina Diana and Fairuz Diyana for helping and sharing the ideas throughout this research. Also, great thanks to lab assistants specially Encik Rashid for providing necessary assistance all the time during this research.

Finally, my sincere appreciation goes to my husband for his co-operation, understanding, support and love in the whole course of my time consumed in research as well as to my parents for their unceasing encouragement and support.

## ABSTRACT

In a plasma focus operation, the X-ray radiation properties are dependent on the thermodynamics data such as ion fraction ( $\alpha$ ), effective ion charge number ( $Z_{eff}$ ), and effective specific heat ratio ( $\gamma$ ) at different temperatures. In Corona Model (CM), the value of ion fraction was first obtained from McWhirter's equation and was subsequently used in determining the  $Z_{eff}$  and  $\gamma$  values. The state-of-the-art ion fraction calculation based on Mazzotta's (Mazz) in Modified Corona Model (MOCM) was compared with McWhirter's (McW) computations for neon, argon and nitrogen gases. The implementation of McW's and Mazz's ion fraction calculation in CM and MOCM cases respectively showed deviations in terms of temperatures. The aim of this study is to investigate the  $Z_{eff}$  and  $\gamma$  values based on the ion fraction values determined from Mazz's and McW's computations and applied in numerical experiment of plasma focus device emphasizing on radial compression plasma dynamics and parameters of soft X-ray (SXR) emission. The  $Z_{eff}$  and  $\gamma$  for both computations were incorporated in Lee code for numerical experiment on SXR yield. Lee code version RADPF5.15K has been used with the incorporation of  $Z_{eff}$  and  $\gamma$  computation based on CM and MOCM operating in various gas pressures. The parameters of SXR yield played important role as they were affected by these different thermodynamics data calculation used in CM and MOCM in the Lee Model. Among these three operating gases, argon plasma of MOCM showed tremendous significant effect towards the results in SXR yield which cannot be disregarded. Thus, it is concluded that the ion fraction values derived from Mazz's computation has a significant effects on  $Z_{eff}$ ,  $\gamma$ , higher SXR yield and enhances radial compression phase performance.

## ABSTRAK

Dalam pengendalian plasma fokus, sifat radiasi sinar-X bergantung kepada data termodinamik seperti pecahan ion ( $\alpha$ ), bilangan cas ion berkesan ( $Z_{eff}$ ), dan nisbah haba tentu ( $\gamma$ ) pada suhu yang berbeza. Dalam Model Corona (CM), nilai pecahan ion pada dasarnya diperoleh daripada persamaan McWhirter dan kemudiannya digunakan dalam menentukan nilai  $Z_{eff}$  dan  $\gamma$ . Pengiraan pecahan ion terkini berdasarkan Mazzotta (Mazz) dalam Model Corona Diubahsuai (MOCM) dibandingkan dengan pengiraan McWhirter (McW) untuk gas neon, argon dan nitrogen. Pelaksanaan pengiraan pecahan ion McW dan Mazz dalam CM dan MOCM masing-masing menunjukkan sisihan dari segi suhu. Tujuan kajian ini adalah untuk mengkaji  $Z_{eff}$  dan  $\gamma$  berdasarkan nilai pecahan ion yang ditentukan daripada pengiraan Mazz dan McW dan seterusnya diaplikasikan kepada simulasi peranti plasma fokus khususnya kepada mampatan jejarian dinamik plasma dan parameter pancaran sinar-X lembut (SXR).  $Z_{eff}$  dan  $\gamma$  berdasarkan kedua-dua pengiraan telah dimasukkan dalam kod Lee untuk simulasi hasil SXR. Kod Lee versi RADPF5.15K telah digunakan dengan kemasukan pengiraan  $Z_{eff}$  dan  $\gamma$  berdasarkan CM dan MOCM yang beroperasi dalam pelbagai tekanan gas. Parameter hasil SXR memainkan peranan penting kerana dipengaruhi dengan perbezaan pengiraan data termodinamik yang digunakan dalam CM dan MOCM dalam Model Lee. Antara ketiga-tiga gas beroperasi, plasma argon dalam MOCM menunjukkan kesan yang ketara terhadap keputusan dalam hasil SXR yang tidak boleh diabaikan. Oleh itu, kesimpulannya nilai pecahan ion yang diperoleh daripada pengiraan Mazz ini mempunyai kesan yang besar ke atas  $Z_{eff}$ ,  $\gamma$ , hasil SXR yang lebih tinggi dan meningkatkan prestasi fasa mampatan jejarian plasma.

## TABLE OF CONTENTS

CHAPTER	TITLE	PAGE
	<b>DECLARATION</b>	ii
	<b>DEDICATION</b>	iii
	<b>ACKNOWLEDGEMENT</b>	iv
	<b>ABSTRACT</b>	v
	<b>ABSTRAK</b>	vi
	<b>TABLE OF CONTENTS</b>	vii
	<b>LIST OF TABLES</b>	x
	<b>LIST OF FIGURES</b>	xi
	<b>LIST OF ABBREVIATIONS</b>	xiv
	<b>LIST OF SYMBOLS</b>	xv
<b>1</b>	<b>INTRODUCTION</b>	<b>1</b>
	1.1 Background of research	1
	1.2 Problem Statement	3
	1.3 Objectives of Research	4
	1.4 Scope of Research	4
	1.5 Significance of Research	5
	1.6 Thesis Organization	5
<b>2</b>	<b>LITERATURE REVIEW</b>	<b>7</b>
	2.1 Introduction	7
	2.2 History of research in plasma ionization balance	7
	2.3 Types and designs of plasma focus	10
	2.4 Modelling of plasma focus device	15

2.5	Plasma dynamics in plasma focus device	16
2.6	X-ray emission using plasma focus	18
2.7	Research on modification of thermodynamics parameters in plasma focus	21
<b>3</b>	<b>THEORETICAL FRAMEWORK</b>	<b>23</b>
3.1	Introduction	23
3.2	Plasma Focus Dynamics	24
3.2.1	Breakdown Phase	24
3.2.2	Axial Acceleration Phase	25
3.2.3	Radial Phase	27
	3.2.3.1 Radial inward shock phase	29
	3.2.3.2 Radial reflected shock phase	29
	3.2.3.3 Slow compression phase	30
	3.2.3.4 Expanded column phase	30
3.3	General concept of X-ray emission from plasmas	31
3.3.1	Collisional ionization and radiative recombination rate	31
	3.3.1.1 McWhirter's calculation (McW)	32
	3.3.1.2 Mazzotta's calculation (Mazz)	33
3.3.2	Ionization balance state	35
3.3.3	Effective ion charge number, $Z_{\text{eff}}$	36
3.3.4	Power density of X-ray	37
3.3.5	X-ray emission intensities	40
3.3.6	Effective specific heat ratio, $\gamma$	41
3.4	Plasma focus model equation and process of plasma focus	44
3.4.1	Axial phase	44
	3.4.1.1 Equation of motion	45
	3.4.1.2 Circuit equation	46
3.4.2	Radial inward shock phase	48
	3.4.2.1 Shock front speed	48
	3.4.2.2 Axial elongation speed of the plasma slug	50

	3.4.2.3	Magnetic piston speed	50
	3.4.2.4	Circuit equation of radial phase	52
	3.4.3	Radial reflected shock phase	54
	3.4.3.1	Reflected shock speed	55
	3.4.3.2	Axial elongation speed of the plasma slug	56
	3.4.3.3	Magnetic piston speed	56
	3.4.3.4	Circuit equation	56
	3.4.4	Slow compression phase	56
	3.4.4.1	Axial elongation speed of plasma column	57
	3.4.4.2	Magnetic piston speed	57
	3.4.5	Expanded column axial phase	60
	3.4.5.1	Equation of motion	60
	3.4.5.2	Circuit equation	60
3.5		X-ray emission processes	61
	3.5.1	Bremsstrahlung radiation	62
	3.5.2	Recombination radiation	63
	3.5.3	Line radiation	64
<b>4</b>		<b>RESEARCH METHODOLOGY</b>	<b>65</b>
	4.1	Introduction	65
	4.2	Methodology of thermodynamics data computation in Lee Model	65
	4.3	Methodology of result analysis on thermodynamics data for CM and MOCM cases	68
	4.4	Methodology of current waveform fitting procedure in Lee Model	70
	4.5	Methodology of result analysis on current waveform fitting for CM and MOCM cases in Lee Model	75
	4.6	Methodology of result analysis on SXR yield evaluation for CM and MOCM cases in Lee Model	77



<b>5</b>	<b>RESULTS AND DISCUSSIONS</b>	<b>80</b>
5.1	Introduction	80
5.2	Numerical Experiments on thermodynamics data in Corona Model	81
5.2.1	Results on the ion fraction of Ne, N <sub>2</sub> and Ar	81
5.2.2	Results on the ion charge number $Z_{\text{eff}}$ of Ne, N <sub>2</sub> and Ar	84
5.2.3	Results on the specific heat ratio $\gamma$ of Ne, N <sub>2</sub> and Ar	88
5.2.4	Results on the X-ray emission intensities	90
5.3	Numerical Experiments on current waveform fitting in Lee Model	95
5.3.1	Results of current waveform fitting in Lee Model	95
5.4	Numerical experiments on UNU/ICTP PFF machines	99
5.4.1	Results for neon SXR yield for MOCM and CM	99
5.4.2	Results for nitrogen SXR yield for MOCM and CM	106
5.4.3	Results for argon SXR yield for MOCM and CM	112
<b>6</b>	<b>CONCLUSION</b>	<b>118</b>
	<b>REFERENCES</b>	<b>120</b>
	APPENDIX A	127
	APPENDIX B	131

**LIST OF TABLES**

<b>TABLE NO.</b>	<b>TITLE</b>	<b>PAGE</b>
4.1	Configuration parameters used for RADPF5.15K Lee Model	71
5.1	Model parameters obtained in Lee Model for CM and MOCM cases	96
5.2	Results of numerical experiment of CM using neon gas	100
5.3	Results of numerical experiment of MOCM using neon gas	101
5.4	Results of numerical experiment with CM using nitrogen gas	107
5.5	Results of numerical experiment with MOCM using nitrogen gas	107
5.6	Results of numerical experiment with CM using argon gas	112
5.7	Results of numerical experiment with MOCM using argon gas	113

## LIST OF FIGURES

FIGURE NO.	TITLE	PAGE
2.1	Mather-type plasma focus	12
2.2	Filippov-type plasma focus	12
2.3	Spherical type plasma focus	13
3.1	Plasma focus dynamics at the axial phase	26
3.2	Radial inward shock phase	27
3.3	Radial reflected shock phase	28
3.4	Slow compression phase	28
3.5	Schematic of equivalent electrical circuit for PF device operation	47
3.6	Formation of plasma pinch at time (a) $t_{on-axis}$ (b) $T > t_{on-axis}$	54
3.7	Bound-bound, free-bound and free-free transitions	61
4.1	Flow chart of Corona Model subroutines into Lee Model	66
4.2	Flow chart of thermodynamics data calculations and analysis	69
4.3	Flow chart of current fitting process	72
4.4	GUI of Lee Model with the (a) CM and (b) MOCM	73
4.5	Flow chart of current fitting analysis	76
4.6	Flow chart of SXR yield analysis	78
5.1	Neon ion fraction at different temperature, where IX indicates $Ne^{+8}$ (calculated by Mazz compared with McW)	82
5.2	Nitrogen ion fraction at different temperature, where VI indicates $N^{+5}$ (calculated by Mazz compared with McW)	83
5.3	Argon ion fraction at different temperature, where XVII indicates $Ar^{+16}$ (calculated by Mazz compared with McW)	83
5.4	Comparison between $Z_{eff}$ versus T for neon gas	86
5.5	Comparison between $Z_{eff}$ versus T for nitrogen gas	86
5.6	Comparison between $Z_{eff}$ versus T for argon gas	87
5.7	Comparison between $\gamma$ versus T for neon gas	89
5.8	Comparison between $\gamma$ versus T for nitrogen gas	89

5.9	Comparison between $\gamma$ versus T for argon gas	90
5.10	Calculated X-ray line emission intensities from neon Ly and He lines versus temperature	92
5.11	Calculated X-ray line emission intensities from nitrogen Ly and He lines versus temperature	93
5.12	Calculated X-ray line emission intensities from argon Ly and He lines versus temperature	94
5.13	Fitted model parameters of total computed current waveform at 3.0 Torr to that of experimentally measured waveform at same 3.0 Torr of neon for CM and MOCM cases	97
5.14	Fitted model parameters of total computed current waveform at 1.05 Torr to that of experimentally measured waveform at same 1.05 Torr of nitrogen for CM and MOCM cases	97
5.15	Fitted model parameters of total computed current waveform at 1.5 Torr to that of experimentally measured waveform at same 1.5 Torr of argon for CM and MOCM cases	98
5.16	Neon SXR yield and $T_{\text{pinch}}$ as functions of the pressure, $P_0$ from UNU/ICTP PFF plasma focus	102
5.17	Pinch ion density versus pressure for CM and MOCM cases using neon	103
5.18	Pinch radius versus pressure for CM and MOCM cases using neon	104
5.19	Pinch duration versus pressure for CM and MOCM cases using neon	104
5.20	Pinch elongation length versus pressure for CM and MOCM cases using neon	105
5.21	Efficiency versus pressure for CM and MOCM cases using neon	105
5.22	Nitrogen SXR yield $Y_{\text{sxr}}$ and pinch temperature $T_{\text{pinch}}$ as functions of the pressure, $P_0$ from UNU/ICTP PFF plasma focus	108
5.23	Pinch ion density versus pressure for CM and MOCM cases using nitrogen	109
5.24	Pinch duration versus pressure for CM and MOCM cases using nitrogen	110
5.25	Pinch radius versus pressure for CM and MOCM cases using nitrogen	110
5.26	Pinch elongation length versus pressure for CM and MOCM cases using nitrogen	111
5.27	Efficiency versus pressure for CM and MOCM cases using nitrogen	111

5.28	Argon SXR yield $Y_{\text{sxr}}$ and pinch temperature $T_{\text{pinch}}$ as functions of the pressure, $P_0$ from UNU/ICTP PFF plasma focus	114
5.29	Pinch ion density versus pressure for CM and MOCM cases using argon	115
5.30	Pinch radius versus pressure for CM and MOCM cases using argon	115
5.31	Pinch duration versus pressure for CM and MOCM cases using argon	116
5.32	Pinch elongation length versus pressure for CM and MOCM cases using argon	116
5.33	Efficiency versus pressure for CM and MOCM cases using argon	117

**LIST OF ABBREVIATIONS**

PF	-	Plasma Focus
RADPF	-	Radiative Dense Plasma Focus
UNU/ICTP	-	United Nations University/International Centre for Theoretical Physics
MOCM	-	Modified Corona Model
CM	-	Corona Model
SXR	-	Soft X-ray
NIST	-	National Institute of Standards and Technology
NIFS	-	National Institute for Fusion Science

## LIST OF SYMBOLS

$A$	-	Atomic Weight
$a$	-	Anode Radius
$\alpha_z$	-	The fraction of the plasma which is ionized to the zth ionized
$B$	-	Magnetic Field
$b$	-	Cathode Radius
$c$	-	Ratio of Cathode to Anode Radius
$C_o$	-	Capacitor bank for energy storage
$C$	-	Ionization rate coefficient
$C_p$	-	Specific heat capacity at constant pressure
$C_v$	-	Specific heat capacity at constant volume
$D$	-	Departure coefficient
$dQ$	-	External Input Energy
$EINP$	-	Energy input into plasma
$E_I$	-	The energy stored in the tube inductance
$E_i$	-	Ionization energy
$\xi$	-	Normalized Axial Position
$\zeta$	-	Number of outer electrons
$\chi$	-	Ionization potential
$\gamma$	-	Specific Heat Ratio
$\Gamma$	-	Shock density ratio
$f_m$	-	Axial mass factors
$f_c$	-	Axial current factors
$f_{mr}$	-	Radial mass factors
$f_{cr}$	-	Radial current factors
$f_{AB}$	-	Absorption factor
$f$	-	Degree of freedom

$F_z$	-	the axial force on plasma sheath
$F_{zr}$	-	the radial force on plasma sheath
$h$	-	Focus Enthalpy
$h$	-	Plank's Constant
$h_L$	-	leakage resistance in the plasma tube
$\iota$	-	Normalised Current
$I$	-	Discharge Current
$I_p$	-	Pinch Current
$I_{max}$	-	Peak Discharge Current
$I_{PB}$	-	Pease-Braginskii Current
$I_z$	-	Total energy required to raise one ion from its unionized state to its zth ionized state and
$J$	-	Current Density
$j \times B$	-	driving Magnetic force
$k_B$	-	Boltzman Constant
$k_e V$	-	kilo electron volt
$K_p$	-	Normalised Magnetic Piston Position
$K_s$	-	Normalised Shock Front Position
$l_v$	-	The mean free-path
$L_o$	-	The fixed circuit inductance
$L_p$	-	Changing plasma tube inductance.
$L_e$	-	Plasma Inductance Spark Gap Inductance
$L_o$	-	External (stray) Inductance
$L_1$	-	Inductance of Capacitor C1
$L_2$	-	Inductance of Capacitor C2
$MW$	-	Molecular weight
$M$	-	Photonic excitation number
$m_i$	-	The mass of atom or ion.
$n$	-	Number Density of ions and electrons
$n_i$	-	Ion Density (in the code)
$N_i$	-	Ion number density
$N_e$	-	Electron number density
$N$	-	Line density



$N_{z+1}$	-	State populations of ionization stage $z+1$
$N_z$	-	State populations of ionization stage $z$
$\rho$	-	Mass density
$\rho_o$	-	Ambient gas density
PF	-	Plasma focus
$P_K$	-	Kinetic pressure
$P_B$	-	Magnetic pressure
$P_p$	-	Piston pressure
$P$	-	Rate of Radiation Loss
$P_J$	-	Rate of Joule heating
$P$	-	Pressure
$P_{max}$	-	Maximum pressure
$P(x,t)$	-	The pressure distribution
$P_L$	-	Line radiation power density
$P_b$	-	Bremsstrahlung power density
$P_r$	-	Recombination power density
$P_{rad}$	-	Net power density
$Q$	-	Total electric charge
$r_{min}$	-	Minimum pinch radius
$q_o$	-	Speed of the shocked gas
$q$	-	Speed of the ambient gas
$Q_{rad}$	-	Radiation energy
$Q_s$	-	Radiation loss per unit length
$R_s$	-	Particle position
RC	-	Integration time constant
$r_p$	-	Slug external radius
$r_s$	-	Slug internal radius
$r$	-	The boundary radius of curvature
$r_c$	-	Critical radius
$R_o$	-	The circuit resistance
$R_o$	-	Universal gas constant
$R_p$	-	Plasma resistance
$RR$	-	Radiative recombination rate coefficient

$T$	-	Shock temperature
$t_{p-s}$	-	Transmission time
$t_a$	-	Characteristic axial run down time
$\tau$	-	Confinement time
$\tau$	-	Normalised time
$T$	-	Plasma temperature
$T_e$	-	Electron temperature
$\mu_0$	-	Permeability of Free Space
$V_o$	-	Capacitor voltage
$V_{slug}$	-	Volume of plasma slug
$V$	-	Plasma volume
$U$	-	Internal energy
$v_{Ti}$	-	Thermal velocity of ion
$v_s$	-	Shock front speed
$\omega_g$	-	Statistical weight of the ground state of the ion
$W$	-	Total de-excitation rate could be
$W_e$	-	Collisional de-excitation rate
$Y_{sxr}$	-	Soft X-ray yield
$Z$	-	Atomic number
$z$	-	Instantaneous current sheath position
$Z_{eff}$	-	Effective (average) charge number of one ion
$z_o$	-	Length of anode
$z_f$	-	Radial elongation pinch length

# CHAPTER 1

## INTRODUCTION

### 1.1 Background of research

High current plasma focus (PF) device discharges is a versatile machine known to be the sources of producing high density of plasma with emission of intense radiation such as neutron [1] and abundant amount of soft X-ray (SXR), hard X-ray (HXR), highly energetic ions and electrons [2]. With performance as source of such radiations, the plasma focus machine had gained much interest in the research around the world especially in improving and optimizing the machine for various purposes. Different types of plasma focus devices were discovered by Mather [3] and Filippov [4] in the early 1960's named Mather-type and Filippov-type plasma focus devices.

The dynamical plasma formation and structure of the plasma focus has been examined with a two-dimensional numerical fluid model [5]. A two-dimensional, three-fluid code based on the two-fluid Potter code was developed for simulating the plasma focus discharge and for modelling the ionization and recombination phenomenon by treating neutral gas as plasma medium [6]. A simple plasma focus (3.3kJ) device was specifically designed in earlier work [7, 8] from the prospect of educational value, reliability and cost-effective device.

There are various theoretical models have been generated to simulate plasma dynamics in plasma focus device [9]. In 1984, a 2-phase radiative plasma focus model [10] was developed by S. Lee [7] called Lee Model numerical experiments to characterize any conventional Mather-type plasma focus. The improvement of this model was executed progressively until 1991 with the development of 5-phase model [10]. Based on Corona Model, radiative plasma focus model was established [11] with the capability of yielding trajectory and structure of plasma [12] thus showing good agreement with the experimental measured values.

Corona Model computation for all ionization balance [13] was utilized for thermodynamics data calculations involving specific heat ratio and charge number as function of temperature [10, 14]. The improvement in Lee Model code has been done specifically on the SXR radiation part [12] using line radiation calculation in 1998. The code was then modified for adapting the plasma behaviour in Filippov-type plasma focus operation [15]. Comprehensive range of numerical experiments have been studied to attain scaling laws on neutron yield and neon soft X-ray yield in terms of storage energy and pinch current for optimizing machine parameters and operating parameters [16] in Lee Model.

The modification and improvement of the model is feasibly needed for better continuum and emission processes. The investigation of the calculation of plasma ionization balance for X-ray radiation has become very keen so far [17-22]. In the modelling of plasma focus, the approach used for ionization balance from Corona Mode has been computed using McWhirter's calculation [17].

This had given opportunity for us to continually improve and modify the nominal area of the dependable aspect for SXR radiation, so that predictable altered dynamics in particles emission yields and radiations could be achieved numerically.

Results assembled from the numerical experiments and data collected from actual experimentations are useful to enable in obtaining a greater insight of the physics of the real processes in a plasma focus device. Therefore, the numerical method for improving plasma dynamics in the plasma focus devices that will affect the radiation yields especially for the plasma compression is investigated. This is a highly cost effective method for exploring a lot of complex physical phenomena which are not possible by actual experiments.

## **1.2 Problem statement**

Extensive research in increasing the X-ray yield and expanding its application in the plasma focus has become an interest in the public domain. In spite of this, there is minimal study in the area of plasma thermodynamics data concerning plasma ionization balance effect which requiring more recent data and calculation. Since the production of X-ray is dependent on this thermodynamics data, hence it is feasible to make some modification for this ionization balance to see the effects on X-ray yield that is unobtainable until now. In this study, the analysis of X-ray yield in the plasma focus device is obtained for plasma ionization balance effect and its influence on various parameters in a Mather-type plasma focus. This study will look into how much deviations of plasma ionization balance data for the case of modified calculation and previous calculation as well as other thermodynamics data such as ion charge number and specific heat ratio affected due to the occurred deviations. Also, how much deviations occur in the X-ray yield and its properties as well as the compression dynamics during the pinch phase due to the deviations in plasma ionization balance data.

### 1.3 Objectives of research

The present research is mainly to investigate the deviations of the ionization balance and its effects on thermodynamics data involving ion charge number and specific heat ratio as well as the X-ray emission and its related properties numerically. The study specifically included as below:

- To determine the effects of plasma ionization balance towards the ion charge number and specific heat ratio in Corona Model.
- To find the Lee Model code with the incorporation of modified Corona Model subroutines within the code comprising the modified ion charge number and specific heat ratio.
- To compare the thermodynamics data obtained based on the modified Corona Model and previous Corona Model subroutines in Lee code.
- To characterize the effects of the thermodynamics data in Lee Model emphasizing on radial plasma compression dynamics and related properties of X-ray emission.

### 1.4 Scope of research

This research covered numerical experimentation of plasma thermodynamics data using Corona model which then be further used in the Lee model for plasma focus operation. In this present project, the evaluation of plasma ionization balance corresponding to temperature will be firstly studied. The investigation of the effect of plasma ionization balance towards the ion charge number and specific heat ratio in neon (Ne), argon (Ar) and nitrogen (N<sub>2</sub>) gases will also be included in the Corona Model. The incorporation of Corona Model subroutines within the Lee Model code which comprising the thermodynamics data calculations for Ne, Ar and N<sub>2</sub> will be utilized in this scope. To produce reliable X-ray in this code, the thermodynamics data is the crucial part that needs to be estimated appropriately. Consequently, the effects of these thermodynamics calculations towards X-ray yield will be

investigated emphasizing on the plasma compression dynamics during the final phase and to the related parameters of X-ray yield in Lee Model. Numerical experimentation will be done to study the effects of X-ray yield based on the modified version of Corona Model and then results will be compared with the previous Corona Model used for those three gases.

## **1.5 Significance of research**

The study of plasma focus device has been widely and actively researched for its concept, design, construction, various physics phenomena operation as well as the proper and better improvement of diagnostics techniques for each application purpose. Apart from application purpose, the research is also important to be investigated numerically for development in educational area. Therefore, by incorporating the numerical modification of thermodynamics data based on extensive improvement of plasma ionization balance calculation, more realistic design and product is possibly achieved for better yield and energy resolution in plasma focus study. This study will improvise the calculations in consideration which was yet to be explored. Thus, it contributes to the comprehension of the ionization balance concept by providing a demonstration in the numerical experiments and explaining the uncovered aspects of this phenomenon.

## **1.6 Thesis Organization**

In chapter 1, the introductory description is covered with the background, brief history of the plasma focus research, followed by the problem statement, objectives of research, scope of research and its significance to the current research. In chapter 2, the review of different approaches of plasma ionization balance and plasma dynamics in plasma focus as well as soft X-ray compression dynamics of

plasma focus will be discussed regarding the literature review. In chapter 3, the theoretical aspects of plasma and plasma focus devices are covered including the dynamics of plasma focus operation, general concepts of X-ray emission from plasmas including the collisional ionization balance theory. In chapter 3, the methodology used in numerical experiments of Lee Model along with the proposed modification in the existing Corona Model is presented. The results presentation of the numerical experiments in graphical and tabulated form is included in chapter 4 and depicts an elaborated discussion by interpreting the obtained data. In chapter 6, the conclusion of the research findings is included. It also suggests some aspects to be investigated for the future study in the area of research of the plasma focus devices.



## REFERENCES

1. Saw, S. H., M. Akel, P. C. K. Lee, S. T. Ong, S. N. Mohamad, F. D. Ismail, N. D. Nawi, K. Devi, R. M. Sabri, A. H. Baijan, J. Ali, and S. Lee. Magnetic Probe Measurements in INTI Plasma Focus to Determine Dependence of Axial Speed with Pressure in Neon. *J Fusion Energ.* 2012. 31 (5): 411-417.
2. Mohammadi, M. A., S. Sobhanian, C. S. Wong, S. Lee, P. Lee, and R. S. Rawat. The effect of anode shape on neon soft x-ray emissions and current sheath configuration in plasma focus device. *Journal of Physics D: Applied Physics.* 2009. 42 (4): 045203.
3. Mather, J. W. and A. H. Williams. Some Properties of a Graded Vacuum Spark Gap. *Review of Scientific Instruments.* 1960. 31 (3): 297-303.
4. Filippov, N. V., T. I. Filippova, and V. P. Vinogradov. Dense high temperature plasma in a non-cylindrical Z-pinch compression. *Journal Name: Nucl. Fusion, Suppl.; Other Information: Orig. Receipt Date: 31-DEC-63.* 1962. (2): 577-587.
5. Potter, D. E. Numerical Studies of the Plasma Focus. *Physics of Fluids (1958-1988).* 1971. 14 (9): 1911-1924.
6. Behler, K. and H. Bruhns. Three-fluid magnetohydrodynamical simulation of plasma focus discharges. *Physics of Fluids (1958-1988).* 1987. 30 (12): 3767-3776.
7. Lee, S. Radiation in plasmas. *Proceedings of Spring College in Plasma Physics 1983, ICTP.* World Scientific Pub Co, Singapore, 1984. 1984. 978-987.
8. Lee, S., T. Y. Tou, S. P. Moo, M. A. Eissa, A. V. Gholap, K. H. Kwek, S. Mulyodrono, A. J. Smith, Suryadi, W. Usada, and M. Zakauallah. A simple facility for the teaching of plasma dynamics and plasma nuclear fusion. *American Journal of Physics.* 1988. 56 (1): 62-68.
9. Tan, L. C. *Simulation studies of plasma dynamics and radiation yield in plasma focus device.* National Institute of Education, Nanyang Technological University. Singapore; 2010.
10. Lee, S. Description of Radiative Dense Plasma Focus Computation Package RADPFV5.15 and Downloads - Lee model code 2014. Available: <http://www.plasmafocus.net/IPFS/modelpackage/File1RADPF.htm>
11. Lee, S. A sequential plasma focus. *Plasma Science, IEEE Transactions on.* 1991. 19 (5): 912-919.
12. Liu, M. H. and S. Lee, *SXR Radiation Modeling for Neon Plasma Focus*, in *ICPP&25th EPS Conf. On Contr. Fusion and Plasma Physics 1998:* Praha. 2169-2172.

13. Lee, S. C1 Introduction file for Corona Calculation. 2014. Available:<http://www.plasmafocus.net/IPFS/modelpackage/Corona%20Calculations/C1coronaIntroduction.htm>.
14. Akel, M., S. Al-Hawat, and S. Lee. Numerical Experiments on Soft X-ray Emission Optimization of Nitrogen Plasma in 3 kJ Plasma Focus SY-1 Using Modified Lee Model. *J Fusion Energ.* 2009. 28 (4): 355-363.
15. Siahpoush, V., M. A. Tafreshi, S. Sobhanian, and S. Khorram. Adaptation of Sing Lee's model to the Filippov type plasma focus geometry. *Plasma Physics and Controlled Fusion.* 2005. 47 (7): 1065.
16. Saw, S. H. and S. Lee. Scaling Laws for Plasma Focus Machines from Numerical Experiments. *Energy and Power Engineering.* 2010. 2 (1): 65-72.
17. McWhirter, R. W. P. in *Plasma diagnostic techniques*. R.H. Huddlestone and S.L. Leonard. Editors. 1965. Academic Press: New York.
18. Shull, J. M. and M. Van Steenberg. The Ionization Equilibrium of Astrophysically Abundant Elements. *The Astrophysical Journal Supplement Series.* 1982. 48 95-107.
19. Mazzotta, P., G. Mazzitelli, S. Colafrancesco, and N. Vittorio. Ionization balance for optically thin plasmas: Rate coefficients for all atoms and ions of the elements H to Ni. *Astronomy and Astrophysics Supplement Series.* 1998. 133 (3): 403-409.
20. Bryans, P., N. R. Badnell, T. W. Gorczyca, J. M. Laming, W. Mitthumsiri, and D. W. Savin. Collisional ionization equilibrium for optically thin plasmas. I. updated recombination rate coefficients for bare through sodium-like ions. *Astrophysical Journal, Supplement Series.* 2006. 167 (2): 343-356.
21. Dere, K. P. Ionization rate coefficients for the elements hydrogen through zinc. *Astronomy & Astrophysics.* 2007. 466 771-792.
22. Landi, E., P. R. Young, K. P. Dere, G. Del Zanna, and H. E. Mason. CHIANTI—An Atomic Database for Emission Lines. XIII. Soft X-Ray Improvements and Other Changes. *The Astrophysical Journal.* 2013. 763 (86): 1-9.
23. Burgess, A. Dielectronic Recombination. *The Formation of Spectrum Lines. Proceedings of the Second Harvard-Smithsonian Conference on Stellar Atmospheres. SAO Special Report* 1965. 47-59.
24. Seaton, M. J. Radiative Recombination of Hydrogenic Ions. *Monthly Notices of the Royal Astronomical Society.* 1959. 119 81-89.
25. Jalufka, N. W. Investigation of forbidden transitions in argon ions. *Astrophysical Journal.* 1976. 203 279-283.
26. De Michelis, C. and M. Mattioli. Soft-X-ray spectroscopic diagnostics of laboratory plasmas. *Nuclear Fusion.* 1981. 21 (6): 677.
27. Raymond, J. C. in *Hot Thin Plasmas in Astrophysics*. R. Pallavicini. Editor. 1988. Springer Netherlands. 434.
28. Arnaud, M. and R. Rothenflug. An updated evaluation of recombination and ionization rates. *Astronomy and Astrophysics Supplement Series.* 1985. 60 425-457.
29. Arnaud, M. and J. Raymond. Iron ionization and recombination rates and ionization equilibrium. *Astrophysical Journal.* 1992. 398 (1): 394-406.
30. Luo, Y. and T. Fang. On the Origin of Highly Ionized X-ray Absorbers Detected in the Galactic X-ray Binaries. *Astrophysical Journal.* 2013.
31. Dere, K. P., E. Landi, P. R. Young, G. DelZanna, M. Landini, and H. E. Mason. CHIANTI – an atomic database for emission lines IX. Ionization

- rates, recombination rates, ionization equilibria for the elements hydrogen through zinc and updated atomic data. *Astronomy & Astrophysics*. 2009. 498 915-929.
32. Bernard, A., H. Bruzzone, P. Choi, H. Chuaqui, V. Gribkov, J. Herreras, K. Hirano, A. Krejčí, S. Lee, C. Luo, F. Mezzetti, M. Sadowski, H. Schmidt, K. Ware, C. S. Wong, and V. Zoita. Scientific status of plasma focus research. *Journal of the Moscow Physics*. 1998. 8 93-170.
  33. Paduch, M. *The Diagnostics Problems at Implementation of Plasma Focus Technique in Material and Environmental Sciences*. Institute of Mathematics and Natural Sciences, Tallinn University, Estonia. Tallinn; 2009.
  34. Kl'ir, D. *Generation of Fusion Neutrons in Z-Pinches*. Habilitation Thesis. Faculty of Electrical Engineering, Department of Physics. Czech Technical University. Prague; 2013.
  35. Marshall, J. Performance of a Hydromagnetic Plasma Gun. *Journal Name: Physics of Fluids (U.S.); Journal Volume: Vol: 3; Other Information: Orig. Receipt Date: 31-DEC-60*. 1960. (3): 134-135.
  36. Tendys, J. *Dense plasma focus : a literature review*. Place published: Australian Atomic Energy Commission Research Establishment. 1976.
  37. Patrick, R. M. High-Speed Shock Waves in a Magnetic Annular Shock Tube. *Physics of Fluids (1958-1988)*. 1959. 2 (6): 589-598.
  38. Mather, J. W. Investigation of the High-Energy Acceleration Mode in the Coaxial Gun. *Physics of Fluids (1958-1988)*. 1964. 7 (11): 5- 28.
  39. Willenborg, D. L. and C. D. Hendricks, *Design and construction of a dense plasma focus device, part 1*. 1976, University of Illinois: Urbana, Illinois.
  40. Mather, J. W. Formation of a High-Density Deuterium Plasma Focus. *Physics of Fluids (1958-1988)*. 1965. 8 (2): 366-377.
  41. Ghanei, V., M. R. Abdi, and B. Shirani. Design and construction of a 20- kJ filippov-type plasma focus *American Journal of Physics and Applications*. 2014. 2 (1): 31-34.
  42. Wong, D., A. Patran, T. L. Tan, R. S. Rawat, and P. Lee. Soft X-ray optimization studies on a dense plasma focus device operated in neon and argon in repetitive mode. *Plasma Science, IEEE Transactions on*. 2004. 32 (6): 2227-2235.
  43. Sing, L., P. Lee, Z. Guixin, F. Xianping, V. A. Gribkov, L. Mahe, A. Serban, and T. K. S. Wong. High rep rate high performance plasma focus as a powerful radiation source. *Plasma Science, IEEE Transactions on*. 1998. 26 (4): 1119-1126.
  44. Tafreshi, M. A. A Theoretical Study of the Effect of Discharge Parameters on the Plasma Layer in a Filippov Type Plasma Focus Device. *J Fusion Energ*. 2014. 1-6.
  45. Abd Al-Halim, M. A. Simulation of Plasma Focus Devices with Hemisphere Electrodes. *J Fusion Energ*. 2010. 29 (2): 134-140.
  46. Garanin, S. F. and V. I. Mamyshev, *Two-Dimensional MHD Simulations of a Plasma Focus with Allowance for the Acceleration Mechanism for Neutron Generation*. 2008, Russian Federal Nuclear Center-All-Russia Research Institute of Experimental Physics: Sarov, Nizhni Novgorod oblast. 639-649.
  47. Saw, S. H., P. C. K. Lee, R. S. Rawat, and P. Lee. Optimizing UNU/ICTP PFF Plasma Focus for Neon Soft X-ray Operation. *Plasma Science, IEEE Transactions on*. 2009. 37 (7): 1276-1282.

48. Lee, S. and C. S. Wong. Initiating and strengthening plasma research in developing countries. *Print edition*. 2006. 59 (5): 31-36.
49. Shirani, B. and F. Abbasi. Construction and experimental study of a 2.5kJ, simply configured, mather type plasma focus device. *Brazilian Journal of Physics*. 2010. 40 125-130.
50. Verma, R., R. S. Rawat, P. Lee, S. V. Springham, T. L. Tan, and M. V. Roshan. A fast miniature plasma focus based compact and portable nanosecond pulsed neutron source *Journal of Plasma and Fusion Research SERIES*. 2009. 8 1283-1286.
51. Khan, M. Z., S. L. Yap, and C. S. Wong. Variation of Radiation Emission with Argon Gas Pressure in UM Plasma Focus with the Hollow Anode *Journal of Applied Sciences*. 2013. 3 194-201.
52. Gribkov, V. A., A. Banaszak, B. Bienkowska, A. V. Dubrovsky, I. Ivanova-Stanik, L. Jakubowski, L. Karpinski, R. A. Miklaszewski, M. Paduch, M. J. Sadowski, M. Scholz, A. Szydlowski, and K. Tomaszewski. Plasma dynamics in the PF-1000 device under full-scale energy storage: II. Fast electron and ion characteristics versus neutron emission parameters and gun optimization perspectives. *Journal of Physics D: Applied Physics*. 2007. 40 (12): 3592.
53. Damideh, V., M. A. Tafreshi, A. Heidarnia, A. Asle-Zaeem, and A. Sadighzadeh. Design and Construction of the 5 kJ Filippov-Type Plasma Focus with Brass Anode. *J Fusion Energ*. 2011. 30 (6): 462-465.
54. Bures, B. L. and M. Krishnan. An efficient snow plow model to deduce plasma focus macroscale parameters. *Plasma Science (ICOPS), 2012 Abstracts IEEE International Conference on*. 8-13 July 2012. 2012. 1P-162-161P-162.
55. Lee, S. Plasma Focus Radiative Model: Review of the Lee Model Code. *J Fusion Energ*. 2014. 1-17.
56. Frignani, M. *Simulation of Gas Breakdown and Plasma Dynamics in Plasma Focus Devices*. Department of Nuclear Energy Engineering and Environmental Control. University of Bologna. Genoa Area, Italy; 2007.
57. Lee, S. Energy balance and the radius of electromagnetically pinched plasma columns. *Plasma Physics*. 1983. 25 (5): 571-576.
58. Potter, D. The formation of high-density z-pinchs. *Nuclear Fusion*. 1978. 18 (6): 813.
59. Lee, S., S. H. Saw, A. E. Abdou, and H. Torreblanca. Characterizing Plasma Focus Devices—Role of the Static Inductance—Instability Phase Fitted by Anomalous Resistances. *J Fusion Energ*. 2011. 30 (4): 277-282.
60. Al-Hawat, S. and M. Akel. Numerical Calculation of a 2.8 kJ Plasma Focus Characteristics Using a Five-Phase Model *Proceedings of the International Workshop On Plasma Computations & Applications (IWPCA2008)*. 14-15 July 2008. 2008.
61. Lee, S., S. H. Saw, and J. Ali. Numerical Experiments on Radiative Cooling and Collapse in Plasma Focus Operated in Krypton. *J Fusion Energ*. 2013. 32 (1): 42-49.
62. Liu, M., X. Feng, S. V. Springham, and P. Lee. Soft X-ray yield measurement in a small plasma focus operated in neon. *Plasma Science, IEEE Transactions on*. 1998. 26 (2): 135-140.

63. Bing, S. *Comparative Study of Dynamics and X-ray Emission of Several Plasma Focus Devices*. Ph.D. dissertation. National Institute of Education, Nanyang Technological University. Singapore; 2000.
64. Rafique, M. S. *Compression dynamics and radiation emission from a deuterium plasma focus*. National Institute of Education, Nanyang Technological University. Singapore; 2000.
65. Zhang, G. *Plasma soft X-ray source for microelectronic lithography*. National Institute of Education, Nanyang Technological University. Singapore; 1999.
66. Mather, J. W. and A. H. Williams. Image Converter Observations of the Development of the Dense Plasma Focus Discharge. *Physics of Fluids (1958-1988)*. 1966. 9 (10): 2080-2082.
67. Bostick, W. H., W. Prior, L. Grunberger, and G. Emmert. Pair Production of Plasma Vortices. *Physics of Fluids (1958-1988)*. 1966. 9 (10): 2078-2080.
68. Lovberg, R. H. and H. R. Griem. *Plasma Physics*. Place published: Elsevier Science. 1971.
69. Ware, K. D., J. W. Mather, A. H. Williams, P. J. Bottoms, and J. P. Carpenter. Design and Operation of a Fast High-Voltage Vacuum Switch. *Review of Scientific Instruments*. 1971. 42 (4): 512-518.
70. Saw, S. H., S. Lee, F. Roy, P. L. Chong, V. Vengadeswaran, A. S. M. Sidik, Y. W. Leong, and A. Singh. In situ determination of the static inductance and resistance of a plasma focus capacitor bank. *Review of Scientific Instruments*. 2010. 81 (5): -.
71. Mohanty, S. R., N. K. Neog, H. Bhuyan, R. K. Rout, R. S. Rawat, and P. Lee. Effect of Anode Designs on Ion Emission Characteristics of a Plasma Focus Device. *Japanese Journal of Applied Physics*. 2007. 46 (5A): 3039-3044.
72. Ali, Z., J. Ali, S. H. Saw, and S. Lee. Numerical Experiments for Radial Dynamics and Opacity Effect in Argon Plasma Focus. *Progress In Electromagnetics Research Symposium (PIERS)*. 2012. 1875-1879.
73. Allam, T. M., G. M. El- Kashef, and T. F. Emar. Study of the Correlation between the Plasma Sheath Dynamical Behavior and the Best Focus Action. *Arab Journal of Nuclear Science and Applications*. 2013. 46 (1): 163-171.
74. Beg, F. N., I. Ross, A. Lorenz, J. F. Worley, A. E. Dangor, and M. G. Haines. Study of x-ray emission from a table top plasma focus and its application as an x-ray backlighter. *Journal of Applied Physics*. 2000. vol. 88 (no. 6): pp. 3225-3230.
75. Liu, M. *Soft X-rays from compact plasma focus*. National Institute of Education. Nanyang Technological University. Singapore; 1996.
76. Akel, M., S. Lee, and S. H. Saw. Numerical Experiments in Plasma Focus Operated in Various Gases. *Plasma Science, IEEE Transactions on*. 2012. 40 (12): 3290-3297.
77. Lee, S. Radius Ratios of Argon Pinches. *Australian Journal of Physics*. 1983. 36 (6): 891-896.
78. Yanagidaira, T., T. Yamamoto, B. Shan, and K. Hirano. Spectroscopic Investigation of Z-Pinch with a Spatial and Temporal Resolution. *Journal of the Physical Society of Japan*. 1999. 68 (3): 852-856.
79. Mohanty, S. R., M. P. Srivastava, and R. S. Rawat. Study of X-ray emission of dense plasma focus device in the presence of external magnetic field. *Physics Letters A*. 1997. 234 (6): 472-476.

80. Moo, S. P., C. S. Wong, and A. C. Chew. Twelve Years of UNU/ICTP PFF-A Review. *Proceedings of Satellite Meeting of the International Meeting on Frontiers of Physics* October 30, 1998. 1998. 98.
81. Lee, S., R. S. Rawat, P. Lee, and S. H. Saw. Soft x-ray yield from NX2 plasma focus. *Journal of Applied Physics*. 2009. 106 (2):
82. Akel, M. and S. Lee. Soft X-Ray Emission in the Water Window Region with Nitrogen Filling in a Low Energy Plasma Focus. *J Fusion Energ*. 2013. 32 (1): 121-127.
83. Akel, M. Numerical Experiments on Oxygen Plasma Focus: Scaling Laws of Soft X-Ray Yields. *J Fusion Energ*. 2013. 32 (4): 464-470.
84. Akel, M., S. Al-Hawat, S. H. Saw, and S. Lee. Numerical Experiments on Oxygen Soft X-Ray Emissions from Low Energy Plasma Focus Using Lee Model. *J Fusion Energ*. 2010. 29 (3): 223-231.
85. Kramida, A., Y. Ralchenko, J. Reader, and N. A. Team. National Institute of Standards and Technology (NIST). 2013. Available:<http://physics.nist.gov/asd>.
86. Lee, S. and S. H. Saw, *Multi radiation modelling of the plasma focus*, in *5th International Conference on the Frontiers of Plasma Physics and Technology*. 2011: Singapore 17.
87. Seng, L. L. *Lee's Radiative Plasma Focus Model - An Improved Implementation with Auto-tuning of Model Parameters* National Institute of Education, Nanyang Technological University. Singapore; 2009.
88. Akel, M., S. A. Salo, and C. S. Wong. Numerical Study of Radiation Emission from the Argon Plasma Focus. *J Fusion Energ*. 2013. 32 (2): 242-246.
89. Favre, M., P. Silva, H. Chuaqui, E. Wyndham, P. Choi, and C. Dumitrescu-Zoita. Studies of Plasma Dynamics in a Small Plasma Focus Operating in Hydrogen-Argon Mixtures. *Astrophysics and Space Science*. 1997. 256 (1-2): 473-478.
90. Sor Heoh, S., C. Perk Lin, R. S. Rawat, C. T. L. Ching, P. Lee, A. Talebitaher, and L. Sing. The Effect of Specific Heat Ratio on Neutron Yield. *Plasma Science, IEEE Transactions on*. 2014. 42 (1): 99-104.
91. Lee, S. A current-stepping technique to enhance pinch compression. *Journal of Physics D: Applied Physics*. 1984. 17 (4): 733.
92. Lee, S. Institute for Plasma Focus Studies. 2013. Available:<http://www.plasmafocus.net/>.
93. Saw, S. H. and S. Lee. Scaling Laws for Plasma Focus Machines from Numerical Experiments. *Energy and Power Engineering*. 2010. vol. 2 (no. 1): pp. 65-72.
94. Lee, S., R. S. Rawat, P. Lee, and S. H. Saw. Soft x-ray yield from NX2 plasma focus. *J. Appl. Phys*. 2009. vol. 106 (no. 2):
95. Ali, Z., S. Lee, F. D. Ismail, Saktioto, J. Ali, and P. P. Yupapin. Radiation Self Absorption Effect in Ar Gas NX2 Mather Type Plasma Focus. *Procedia Engineering*. 2011. 8
96. Bates, D. R., A. E. Kingston, and R. W. P. McWhirter. Recombination Between Electrons and Atomic Ions. I. Optically Thin Plasmas. *Proceedings of the Royal Society of London. Series A. Mathematical and Physical Sciences*. 1962. 267 (1330): 297-312.
97. Verner, D. A. and G. J. Ferland. Atomic Data for Astrophysics. I. Radiative Recombination Rates for H-like, He-like, Li-like, and Na-like Ions over a

- Broad Range of Temperature. *Astrophysical Journal Supplement*. 1996. 103-467.
98. Hutchinson, I. H. *Principles of Plasma Diagnostics*. Place published: Cambridge University Press. 2005.
  99. Akel, M. and S. Lee. Dependence of Plasma Focus Argon Soft X-Ray Yield on Storage Energy, Total and Pinch Currents. *J Fusion Energ*. 2012. 31 (2): 143-150.
  100. Mazzotta, P., G. Mazzitelli, S. Colafrancesco, and N. Vittorio. National Institute of Fusion Science (NIFS). 1998. Available: <http://dpc.nifs.ac.jp/ionfracdata/>.
  101. Akel, M. Yield Optimization of Helium and Lyman Emissions in Low Energy Plasma Focus Operated with Argon. *J Fusion Energ*. 2012. 31 (5): 473-479.
  102. Lee, S. and S. H. Saw. Numerical Experiments Providing New Insights into Plasma Focus Fusion Devices. *Energies*. 2010. 3 (4): 711-737.
  103. Akel, M., S. Al-Hawat, and S. Lee. Pinch Current and Soft X-Ray Yield Limitations by Numerical Experiments on Nitrogen Plasma Focus. *J Fusion Energ*. 2010. 29 (1): 94-99.