

AN IMPLEMENTATION OF LOSS DETECTION USING SOSS MODEL

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Abstract: Recent studies have shown that malicious Internet traffic such as Denial of Service (DoS) packets introduces distribution error and perturbs the self-similarity property of network traffic. As a result, Loss of Self-Similarity (LoSS) is detected due to the abnormal traffic packets hence degrading the Quality of Service (QoS) performance. In order to fulfill the demand for high speed and accuracy for online Internet traffic monitoring, we propose LoSS detection with second order self-similarity statistical (SOSS) model and estimate the self-similarity parameter using the Optimization Method (OM). We test our approach using synthetic and real traffic data. For the former, we use fractional Gaussian noise (FGN) generator, while for the latter we use FSKSMNet simulation dataset. We investigate the behavior of self-similarity property for normal and abnormal traffic packets with different aggregation sampling level (m). The results show that normal Internet activities preserve exact self-similarity property while abnormal traffic perturbs the structure of self-similarity property. The results also demonstrate that fixed m is not sufficient to detect distribution error accurately. Accordingly, we suggest a multi-level aggregation sampling approach to improve the accuracy of LoSS detection.

Keywords: Loss of Self-Similarity (LoSS) detection, Second Order Self-Similarity (SOSS), Multi-Level Aggregation Sampling.

1. INTRODUCTION

The concept of self-similarity and the related concept of long-range dependent (LRD) in the field of network traffic and performance analysis is introduced in [7] and followed by [8]. Self-similarity

describes the phenomenon in which the behavior of a process is preserved irrespective of scaling in space or time. The knowledge of LRD states that network traffic always exhibit long-term memory such that its behavior across widely separated times is correlated. This finding was in contrast to widely accepted Poisson model of the network traffic, which is memoryless and inter-arrival times are exponentially distributed. The finding challenged the validity of the Poisson assumption and shifted the community's focus from assuming memoryless and smooth behavior network traffic to assuming LRD and bursty behavior.

Previous works had pointed out several causes of the self-similarity phenomenon. One is the mixed behavior of TCP services model such as log-normal, log-extreme and Pareto distributions [13]. Another one is the mixture of actions from individual users, hardware and software in interconnecting networks [2]. The third reason is the heavy-tailed distribution of file sizes where huge transferred files occurred with non-negligible probability [2]. The work done in [3] and [12] showed that congestion due to uncontrolled self-similarity structure degrades Quality of Service (QoS) performance by drastically increasing queuing delay and packet loss.

Protocol intensity distribution plays an important role to the interactions that produce self-similarity behavior [13]. Denial of Service (DoS) attacks with very high bit rate injection packets can dominate the traffic protocol and produce distribution error, hence disturb the property of self-similar behavior [14]. As a result, Loss of Self-Similarity (LoSS) behavior is detected [14] and as shown in [1] and [10], this can be used as a flag to alert security analysts of the possible presence of a malicious action, provided that the normal traffic background is self-similar which is a common network traffic attribute.

The work in [1] has presented a new technique for detecting the possible presence of new DoS attacks without a template of the background traffic. The method used LoSS definition with the self-similarity or Hurst parameter beyond normal LRD self-similarity behavior ($0.5 < H < 1$) using the Periodogram and the Whittle methods. However, new methods of estimating Hurst parameter which is more accurate and faster had been developed such as the Optimization Method (OM) [4], [5] which used the second order self-similarity statistical (SOSS) model. In this paper, we present a new LoSS detection method using SOSS model and OM.

The paper is organized as follows: Section 2 presents mathematical definitions and properties of SOSS and how to estimate its parameter. Section 3 on the other hand, discusses the concept of LoSS detection and related work. Section 4 discusses the datasets that were used in the simulations while Section 5 presents our experiment procedure and the results. Finally our conclusions and future work directions are summarized in Section 6.

2. SOSS STATISTICAL MODEL

Let $X = \{X(t), t = 0, 1, 2, \dots, N\}$ be a second-order stationary process with constant mean μ , finite variance σ^2 , and autocorrelation function $\rho(k)$ that depends only on the integer k . Their definitions are given as follows:

$$\begin{aligned}\mu &= E[X(t)], \quad \sigma^2 = E[(X(t) - \mu)]^2 \\ \rho(k) &= E[(X(t) - \mu)(X(t+k) - \mu)] / \sigma^2\end{aligned}$$

Let $X^{(m)} = \{X^{(m)}(t), t > 0\}$ denote the aggregate process of X at aggregation m , $m = 1, 2, \dots, N$. That

$$\text{is, for each } m, X^{(m)} \text{ is given by } X^{(m)}(t) = \frac{1}{m} \sum_{l=m(t-1)+1}^{mt} X(l), t > 0.$$

Let $\gamma^{(m)}(k)$ and $\rho^{(m)}(k)$ denote the variance and autocorrelation function of $X^{(m)}$ respectively. X is called exactly second-order self-similar (ESOSS) if

$$\rho(k) = \frac{1}{2}[(k+1)^{2-\beta} - 2k^{2-\beta} + (k-1)^{2-\beta}], \quad 0 < \beta < 1, \quad k = 1, 2, \dots, N.$$

X is called long-range dependent (LRD) with $H = 1 - \frac{\beta}{2}$, $0 < \beta < 1$, if its autocorrelation function satisfies $\rho(k) = ck^{-\beta}$, $k \rightarrow \infty$, where c is a positive constant. X is called asymptotical second-order self-similar (ASOSS) with $H = 1 - \frac{\beta}{2}$ and $0 < \beta < 1$, if

$$\lim_{m \rightarrow \infty} \rho^{(m)}(k) = \rho(k), \quad k > 0.$$

Exact self-similar process occurs when $\rho(k) = \rho^{(m)}(k)$ for all $m \geq 1$. Thus, second order self-similarity captures the property of correlation structure preserving under time aggregation and

represented by $\rho(k) = \frac{1}{2}[(k+1)^{2H} - 2k^{2H} + (k-1)^{2H}]$ for ESOSS or

$\lim_{m \rightarrow \infty} \rho^{(m)}(k) = \frac{1}{2}[(k+1)^{2H} - 2k^{2H} + (k-1)^{2H}]$ for ASOSS. In second-order stationary for $0 < H < 1$ and

$H \neq 0.5$, the autocorrelation function $\rho(k)$ satisfies $\rho(k) = H(2H-1)k^{2H-2}$, $k \rightarrow \infty$. In particular,

if $0.5 < H < 1$, $\rho(k)$ asymptotically behaves as $ck^{-\beta}$ for $0 < \beta < 1$ where $c_r > 0$ is a constant and $\beta = 2 - 2H$.

More details about the SOSS model can be found at [7], [8] and [11].

There are several methods to estimate H . In this paper we will be using the Optimization Method (OM) which was developed in [4], [5] and was shown to be comparatively fast and accurate with

respect to other methods. The method is based on how near sample autocorrelation measure fits to ESOSS model. The estimation method defines error fitting function $E_K(\beta)$ as

$$E_K(\beta) = \frac{1}{4K} \sum_{k=1}^K (\rho(k) - \rho_n(k))^2$$

where $\rho(k)$ denotes the autocorrelation function of the model with parameter β that OM would like to fit the data to, $\rho_n(k)$ is the sample autocorrelation function of the data, k is autocorrelation lag and K is the largest value of k for which $\rho_n(k)$ is to be computed to reduce edge effects. The estimation of parameter β is based on optimizing $E_K(\beta)$ with threshold value $\leq 10^{-3}$ is chosen empirically [4].

3. LOSS DETECTION

The ESOSS model preserves the second order distribution property at all levels of time scale aggregation. It is equivalent to distribution ratio of higher scale to lower scale such that:

$$a^{-H} = \frac{x(t)}{x(at)}, \text{ where } x(t) \text{ is distribution at higher scale, } x(at) \text{ is distribution at lower scale}$$

and parameter $a, H > 0$.

It has been proven that in the presence of DoS attacks, the self-similarity property is disturbed hence LoSS is detected as shown in [1], [14] and [14]. The LoSS detection in [14] used the abrupt change property of a^{-H} as an indicator to the existence of distribution error. However, the work did not suggesting at what level of 'a' should be used for revealing the abrupt change of a^{-H} significantly.

Alternatively, instead of using distribution ratio, the work in [1] defines LoSS as Hurst value beyond normal range of LRD which is $0.5 \leq H \leq 0.99$ using Periodogram and Whittle method. The results show that the method can detect new DoS attack pattern without specific normal template. The results also demonstrate that the method has high detection rate with an average of 60% to 84% which depends on the intensity of the attack packets. Recently, a new method of estimating Hurst parameter which is more accurate and faster was developed in [4] and [5]. The method is known as the Optimization Method (OM) and it is based on the SOSS model. Therefore, we propose a new approach of LoSS detection based on SOSS model in order to improve detection accuracy.

The foundation of SOSS model is the stationary concept of higher order distribution. Internet traffic is considered as normal behavior when the traffic is near to self-similarity model while otherwise it is considered as abnormal behavior [14]. In the presence of malicious traffic such as DoS packets, they introduce distribution error and shift the stationary property toward non-stationary as shown in [1], [14] and [14], hence LoSS is detected. Data insufficient probability and detection loss probability are two important attributes that can influence the correctness of anomaly detection [14]. The data insufficient probability is to identify minimum requirement window size to obtain reliable

self-similarity measurement, while detection loss probability is probability where non-stationary data is detected. LoSS is detected if it fulfils two conditions where it must be longer than minimum window size and it must be non-stationary. Experiments have shown in [7] and [8] windows sizes from 15-30 minutes are practical and sufficient for modern LANs Ethernet Internet traffic to comply with data insufficient probability. Self-similarity tests become more sensitive as the window size get smaller and consequently generate false alarms if it gets too small.

A current study on self-similarity measurement used the OM in [4] and [5] provides Hurst estimation with increased calculation speed and maintain high estimation accuracy. In addition the method also provides a technique to identify whether the data tend toward the self-similarity model according to the curve-fitting error value calculated [15]. To this end, we define normal behavior of self-similarity traffic as the estimated Hurst (\hat{H}) with OM is in LRD range such that $0.5 < \hat{H} < 1$, provided data insufficient probability and fitting error $E_k \leq 10^{-3}$ are fulfilled. Otherwise if $E_k > 10^{-3}$ LoSS is detected and we refer this as abnormal behavior for Internet traffic. The ESOSS process refers to $\rho(k) = \rho^{(m)}(k)$ for all $m \geq 1$. Thus, SOSS captures the property of correlation structure which is preserved under time aggregation. Therefore it is required to study the effect of different aggregation sampling value such as $m=10, 100$ and 500 to detect any changes of self-similarity property in order to reveal any hidden distribution error accurately.

4. DATA PREPARATION

We prepare two sets of data to investigate the pattern of normal and abnormal self-similarity behavior. The former used fractional Gaussian noise (FGN) that will generate synthetic traffic which is ESOSS and the latter used FSKSMNet Internet traffic simulation on September 29, 2006 at Faculty of Computer Science and Information (FSKSM) LANs.

4.1 Synthetic Self-Similar Generator with FGN

We generate at random synthetic trace that will exhibit exact self-similarity behavior by using fractional Gaussian noise (FGN) model developed in [6] for $0.5 < H < 1$. The length of the trace is equivalent to 15-30 minute at normal traffic Ethernet LAN as used in [7] and [8]. The synthetic trace is sampled with aggregation level m for $m=10, 100$ and 500 . Then, this dataset is used to investigate the self-similarity property at different aggregation levels of m .

4.2 Simulation of Internet Traffic FSKSMNet

We set an Internet Monitoring Laboratory (InMonLab) with baseline 100BaseFX Fast Ethernet as LAN backbone of FSKSM and connected to main university Gigabit backbone. Network design at FSKSM is constructed with ten proxies of Virtual LANs. There are seven VLAN segments for undergraduate students and one VLAN segment for postgraduate students. Administrators and academic staffs are allocated with one VLAN segment each. The number of students that are currently enrolled at FSKSM is more than one thousand and the number of staff is about one hundred and fifty. We capture internet protocol packets with *tcpdump* software and each of capturing session is about 30 minutes.

We divide our Internet traffic simulation activities into normal and abnormal traffic. For normal Internet activities we define as legal Internet activities as set by faculty network policy. We do not disturb normal Internet activities and do passive sniffing at main router inside InMonLab. For abnormal traffic, we inject at certain rate Denial of Service (DoS) flooding packets into FSKSM network infrastructure such that they will disturb the normal behavior of self-similarity pattern. We launch TCP SYN packets from Packet Injection node to HoneyNet server. However we limit the time stressor for each session to less than two minute to minimize the bandwidth effect. The details simulation traces of synthetic FGN and real traffic of FSKSMNet at FSKSM LANs are shown in Table 1 and each slot contains 30 minutes capturing session.

Table 1. Synthetic FGN and Simulation of FSKSMnet on September29, 2006.

Trace	Class	Capture	Total Packet	DoS Packet
FGN-1	Synthetic	≈ 30min	180,000 (equally $m=10ms$)	
F-Net2	N	12.15pm- 12.45pm	IP=3846328: TCP(97.94%), UDP(1.91%), ICMP(0.11%), IGMP(0.01%), Others(0.03%)	
F-Net3	N	1.45pm- 2.15pm	IP=4197509: TCP(97.87%), UDP(1.69%), ICMP(0.12%), IGMP(0.01%), Others(0.31%)	
F-Net4	AB	3.45pm- 4.15pm	IP=8932254: TCP(93.73%), UDP(1.20%), ICMP(0.04%), IGMP(0.003%), Others(5.021%)	TCP SYN(58.5%)

From Table 1, *F-Net 2* and *F-Net3* traces represent normal traffic activities which do not contain DoS packets. The normal traffic is labeled as N. The total of normal IP packet is about four millions with TCP >95%, UDP < 2%, ICMP, IGMP and others <1%. We simulate abnormal traffic *F-Net4* with TCP SYN attack and labeled as AB. The abnormal traffic contains almost doubles IP packets as compared to normal which is more than eight millions. We sample the traces with $m=10, 100$ and 500 in order to investigate how normal and abnormal traffic preserve self-similarity property. Table 2 shows window sizes of different sampling m values for synthetic FGN and real Internet traffic FSKSMnet datasets. We assume that all simulation traffic traces have fulfilled the minimum windows requirement. Then the estimated Hurst parameter can be used to classify whether or not the traffic follows ESOS model.

Table 2. Aggregation (m) and Window Size.

Level	m	Window Size	
		FGN	FSKSMnet
1	10	180000	173998
2	100	18000	17399
3	500	3600	3479

5. Empirical Analyses

5.1 LoSS Behavior Detection

Our experiments have two purposes. First, to identify the normal traces which follow ESOS model and second, to investigate how self-similarity property is preserved at different levels of sampling m for normal and abnormal Internet traffic. Throughout the experiments, we set threshold fitting error equal to 10^{-3} and estimate Hurst using OM with $K=200$.

Table 3 shows the result of *Hurst* estimation for Synthetic FGN and FSKSMnet traffic while Table 4 shows variance *Hurst* and error for different levels of m . Table 3 shows clearly that synthetic *FGN-1* and *F-Net3* traces follow normal self-similar behavior for all m . However, for *F-Net2* and *F-Net4* traces they have two different classes; at lower $m=10$ and 100 , the traces are categorized as normal self-similar behavior while at higher $m=500$ the traces deviate from normal behavior. In our simulation *F-Net4* trace contains DoS packets and is known as abnormal traffic. The malicious packets of DoS attacks have extremely high bit rate transfer and their structure become dominant hence introduce error to self-similar model. Similarly, legal Internet traffic *F-Net2* trace is also identified as contained

structure that contributes error to the model. However, the error can only be revealed at certain level of m . This can be shown clearly in Table 3 which the error is hidden at $m=10$ and 100 but exposed at $m=500$.

Table 3. Hurst estimation for FGN and FSKSMnet.

Trace	$m=10$		$m=100$		$m=500$	
	Hurst	Error	Hurst	Error	Hurst	Error
FGN-1	0.87	0.00004	0.86	0.00003	0.84	0.00014
F-Net2	0.82	0.00042	0.87	0.00029	0.82	0.00278
F-Net3	0.89	0.00050	0.93	0.00011	0.93	0.00027
F-Net4	0.97	0.00042	0.96	0.00033	0.90	0.01265

5.2 Autocorrelation Structure of Normal and Abnormal Internet Traffic Behavior

We use the ESOS autocorrelation structure of $\rho(k)$ to examine in details how self-similarity structure is preserved at different levels of sampling m . We divide our observation into two categories that are normal-normal and normal-abnormal patterns.

Case I: Normal-Normal

We define normal-normal behavior as the $\rho(k)$ structure preserved the LRD property for all m . Figure 1 (a) and (b) show the $\rho(k)$ structure of *FGN-1* and *F-Net3* traces preserved the LRD structure for $m=10,100$ and 500. The traces have produced normal behavior pattern in two ways. First, *FGN-1* and *F-Net3* traces follows SOSS model at all m which indicate by fitting error less than 10^{-3} . Second, the variance of multi-level sampling *Hurst* value and variance of multi-level fitting error value are small which $Var(m-H)$ is less than 5.5×10^{-4} and $Var(m-Error)$ is less than 10^{-6} . Table 4 shows the details.

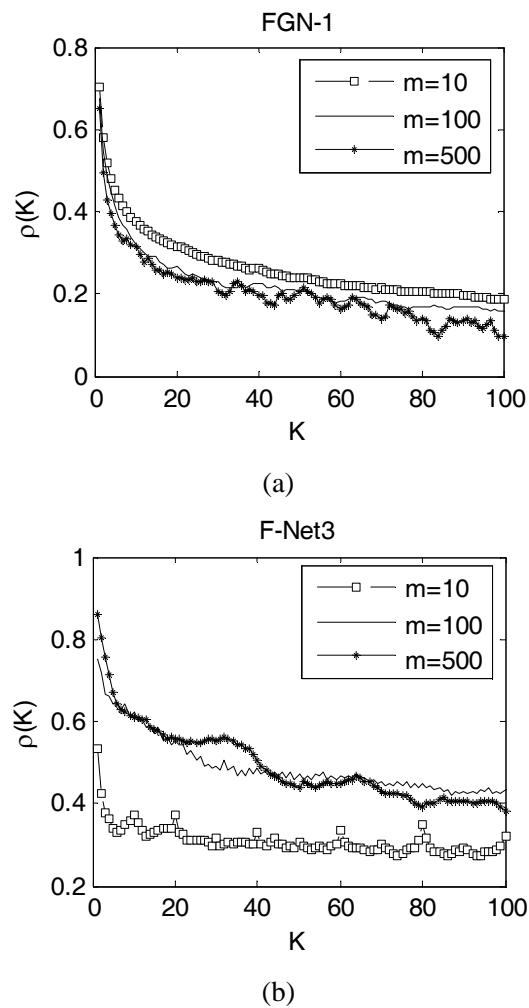


Figure 1. Normal self-similarity property of FGN-1 (a) and F-Net3 (b).

Table 4. Variance of *Hurst* and Fitting Error for different m .

Trace	Var(m-H)	Var(m-Error)
FGN-1	0.000233333	0.00000000370
F-Net2	0.000833333	0.00000196443
F-Net3	0.000533333	0.00000003843
F-Net4	0.001433333	0.00005022723

Case II: Normal-Abnormal

We define normal-abnormal behavior as the $\rho(k)$ structure is preserved at lower m however its lost LRD structure at higher m . As shown in Figure 2(a) and (b), the $\rho(k)$ structure of *F-Net2* and *F-Net4* traces do follow LRD property at lower $m=10$ and 100 , however at higher $m=500$ they don't. Table 2 shows the abnormal traces of *F-Net2* and *F-Net4* have fitting error less than 10^{-3} for $m=10$ and 100 . However, the error exceeds the threshold for $m=500$. The disturbance of $\rho(k)$ structure is shown clearly in Figure 2 (a) and (b). Moreover, the variance of multi-level sampling *Hurst* and variance of multi-level *fitting error* are large which indicate by $Var(m-H)$ bigger than 5.5×10^{-4} and $Var(m-Error)$ bigger than 10^{-6} . The details are shown in Table 4.

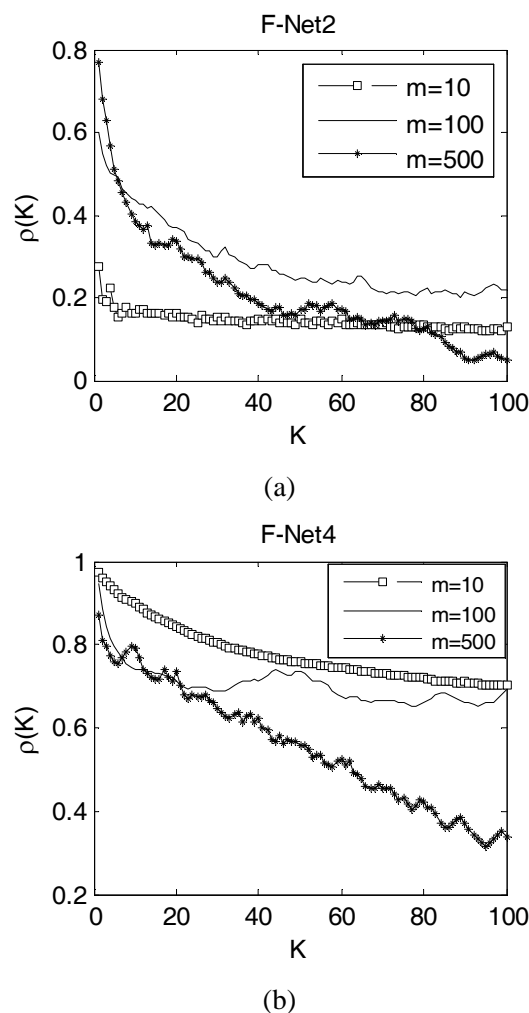


Figure 2. Abnormal self-similarity property of F-Net2 (a) and F-Net4 (b).

It is possible for legal Internet activities to contribute error and disturb the self-similarity property of the network traffic. In our simulation, the disturbance of self-similarity error distribution is hidden at lower sampling value but exposed at higher sampling value. This can be shown by *F-Net2* in Figure 2(a) where the self-similarity is preserved at sampling level $m=10$ and 100 but the error is obviously exposed at sampling level $m=500$. Therefore, it is clearly demonstrated in the experiments that fixed sampling m is not enough to detect anomaly behavior of the traces accurately. The experiments also illustrate that LoSS analysis with multi-level approach is a good direction to improve the accuracy of anomaly traffic behavior detection.

From the observation we can define normal and abnormal Internet traffic behavior based on LoSS detection with multi-level approach. To this end, we consider three parameters to detect LoSS accurately which are LRD property, estimated *Hurst* and *fitting error* at aggregation sampling level m . Let us define the following:

$$A=H \in 0.5 < H < 1,$$

$$B= \textit{fitting error} < \textit{Threshold (at normal } m),$$

$$C= \textit{fitting error} < \textit{Threshold (at higher } m).$$

We define normal behavior as the traffic is following self-similarity LRD property and LoSS is not detected at both normal and multi-level sampling m such that it fulfilled the condition of $A \cap B \cap C$. On the other hand, abnormal behavior is detected when Internet traffic deviates from self-similarity property such that LoSS is detected at either normal or multi-level sampling m such that it follow the condition of $B' \cup C'$. Normal aggregation here refers to $m=10$ ms and 100 ms which is used for Hurst estimation in [4], [5], [7], [8] and [14] while higher aggregation we set m randomly equal to 500 ms.

6. CONCLUSION AND FUTURE WORK

This paper presents the implementation of LoSS detection with SOSS model. From our simulation results, legal and malicious Internet traffic activities are possible to contribute distribution error which deviate autocorrelation structure from self-similarity LRD model. This can be shown clearly when fitting error of autocorrelation structure exceeds the threshold value. However, our simulation results illustrate that the self-similarity distribution error was hidden at lower level of m such as $m=10$ or 100 , but exposed at higher level of m such as $m=500$. We believe this can be possible reason why anomaly detection of Internet traffic behavior which based on LoSS model gives high false alarm detection rate when the self-similarity parameter is estimated only at fixed level of sampling level such as 10 ms or 100 ms. Therefore, our future work we will consider a multi-level sampling aggregation approach in order to increase the accuracy of LoSS detection base on SOSS model. We will also consider a wider range of Internet traffic traces and different types of malicious Internet activities to test the robustness

and reliability of our methods toward development of efficient Internet traffic anomaly detection systems.

ACKNOWLEDGEMENTS

This work was funded by Universiti Teknologi Malaysia (UTM). The authors would like to thanks to Assoc. Prof. Dr. Sulaiman Mohd Noor, Mr. Mohd Hamri at CICT, UTM and Dr. Md. Asri Ngadi, Mr. Firoz at Unit IT, FSKSM for their helps in conducting the simulation of real traffic FSKSMNet dataset.

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