

A COMPUTATIONAL FLUID DYNAMIC FRAMEWORK FOR MODELING
AND SIMULATION OF PROTON EXCHANGE MEMBRANE FUEL CELL

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A COMPUTATIONAL FLUID DYNAMIC FRAMEWORK FOR MODELING
AND SIMULATION OF PROTON EXCHANGE MEMBRANE FUEL CELL

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To my beloved parents

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ABSTRACT

This thesis describes the development and application of a framework for model and analysis of proton exchange membrane fuel cells (PEMFCs) using computational fluid dynamics (CFD). The developed framework addresses the formulation, solution, and analysis of the PEMFCs systems in a systematic manner. This PEMFCs modelling framework helps to generate problem-system specific models describing a step by step proton exchange membrane (PEM) fuel cell model. Accordingly, the problem-system specific model generation procedure consists of three main steps. In the first step the problems and scope of the study are defined. The PEM fuel cell modelling procedure is done in the next step 2. This second step contains three sub-sections which are geometry definition, model definition and numerical solution and validation. In the step 3, the developed model is validated using available experiment/industrial data. A general, three-dimensional, non-isothermal, multi-phase numerical model has been developed to simulate and examine the fluid flow, heat and mass transfer, species transport, electrochemical reaction, and current density distribution of a PEMFC. The validation results of the PEM fuel cell model developed by using this framework has been successfully done. In addition, applications of the validated model with respect to advanced grid analysis, anisotropic properties investigation, and PEMFCs electrochemistry parameter have been successfully implemented. With respect to grid analysis, the results have shown that grid independence analysis using polarization curve is not accurate, where the concentration of fuel cell reactants and product showed more sensitivity for checking the grid independency. In terms of anisotropic properties investigation, the results have shown that increasing the value of anisotropy in thermal conductivity mitigates the gradient of liquid water between the area underneath the ribs and channels in PEMFCs. With respect to PEMFCs electrochemistry parameter, it has been shown that the new derived of the Kazemi-Jahandideh (K-J) approximation is able to reduce the numerical calculation to find electrochemistry parameters with a higher accuracy.

ABSTRAK

Tesis ini menerangkan pembangunan dan aplikasi rangka kerja untuk model dan analisa sel bahan api membran pertukaran proton (PEMFCs) menggunakan dinamik bendalir berkomputer (CFD). Rangka kerja ini telah dibangunkan untuk menangani masalah formula, penyelesaian, dan analisa sistem PEMFCs secara sistematik. Rangka kerja model PEMFCs dapat menghasilkan model khusus terhadap masalah-masalah sistem yang wujud dengan menerangkan secara terperinci bagi model sel bahan api membran pertukaran proton (PEM). Masalah-sistem terhadap prosedur penghasilan model adalah terdiri daripada tiga langkah utama. Dalam langkah pertama, masalah dan skop kajian ini telah ditakrifkan. Prosedur model bagi sel bahan api PEM telah dijalankan pada langkah kedua. Prosedur ini mengandungi tiga sub-bahagian iaitu definisi geometri, definisi model dan penyelesaian berangka dan pengesahan. Dalam langkah ketiga, model yang dibangunkan telah disahkan berdasarkan data eksperimen/industri. Model simulasi yang umum, tiga dimensi, bukan isoterma dan mempunyai pelbagai fasa model berangka telah dibina untuk memeriksa aliran cecair, pemindahan haba dan jisim, pengangkutan spesies, tindakbalas elektrokimia, dan kepadatan taburan bagi PEMFC. Pengesahan rangka kerja terhadap model sel bahan api PEM telah berjaya dibangunkan. Selain itu, model aplikasi analisis grid, penyelidikan sifat anisotropik, dan parameter elektrokimia PEMFCs telah berjaya dilaksanakan. Berkenaan dengan analisis grid, keputusan telah menunjukkan bahawa analisis kebebasan grid menggunakan keluk polarisasi adalah tidak tepat, di mana kepekatan bahan tindak balas sel bahan api dan produk menunjukkan kesan sensitiviti terhadap kebebasan grid. Dari segi penyelidikan sifat anisotropik, keputusan kajian telah menunjukkan bahawa peningkatan nilai anisotropik dalam konduksi terma dapat mengurangkan kecerunan cecair di antara kawasan tulang rusuk dan saluran dalam PEMFCs. Berkenaan PEMFCs parameter elektrokimia PEMFC, ia juga telah menunjukkan bahawa anggaran baru Kazemi-Jahandideh (K-J) dapat mengurangkan pengiraan berangka untuk mencari parameter elektrokimia dengan ketepatan yang lebih tinggi.

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LIST OF ABBREVIATIONS

CAD	-	Computer Aided Design
CFD	-	Computational Fluid Dynamic
CL	-	Catalyst Layer
EIS	-	Electrochemical Impedance Spectroscopy
GDL	-	Gas Diffusion Layer
HOR	-	Hydrogen Oxidation Reaction
ORR	-	Oxygen Reduction Reaction
PEM	-	Proton Exchange Membrane
PEMFC	-	Proton Exchange Membrane Fuel Cell

LIST OF SYMBOLS

a	-	Water Activity
A_{ch}	-	Gas Channel Cross-Sectional Area
A_m	-	Membrane Active Area
C_i	-	Concentration of Specie i
C_p	-	Heat Capacity
$-D$	-	Dimensional
D^{eff}	-	Effective Diffusion Coefficient
e^-	-	Electron
E_0	-	Cell Thermodynamic Potential
F	-	Faraday Constant
H^+	-	Proton
i	-	Current Density
i_0	-	Exchange Current Density
I_{cell}	-	Cell Current Density
k^{eff}	-	Effective Thermal Conductivity
M	-	Molar Mass
n	-	Electron Number
n_d	-	Electro-Osmotic Drag Coefficient
P	-	Pressure
R	-	Gas Constant
R_m	-	Membrane Resistance
S_e	-	Source Term/Sink of Electrical Conservation Equation
S_g	-	Source Term/Sink of Mass Conservation Equation
S_i	-	Source Term/Sink of Ionic Conservation Equation
S_l	-	Source Term/Sink of Liquid Water
S_m	-	Source Term/Sink of Momentum Conservation Equation
S_{phase}	-	Source Term/Sink of Water in Corresponding Phase
S_T	-	Source Term/Sink of Energy Conservation Equation
S	-	Source Term/Sink of Dissolved Water
T	-	Temperature

V	-	Velocity
V_{cell}	-	Cell Potential
w	-	Mass Fraction

Greek letters

Γ	-	Symmetry Factor
β	-	Transfer Coefficient
α	-	Porosity
κ	-	Electrical Conductivity
η	-	Overpotential
ν	-	Stoichiometric Ratio
ϕ	-	Ionic Potential
ψ	-	Electrical Potential
λ	-	Membrane Water Content

Subscripts

act	-	Activation
a	-	Anode
c	-	Cathode
$conc.$	-	Concentration
$resist$	-	Resistance
g	-	Gas Phase
i	-	Specie
$cell$	-	Fuel Cell

Superscripts

ref	-	Reference
eff	-	Effective

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CHAPTER 1

INTRODUCTION

1.1 Introduction

Fuel cells are future technology as a major energy conversion and there are many electrochemical advantages conversion processes in compared with thermal combustion processes (Scherer and Gürsel, 2008). Fuel cells share the electrochemical nature of the power generation process same to batteries but unlike batteries fuel cells work continuously consuming a fuel of different type. A fuel cell defined as an device that changes over compound vitality into electric vitality electrochemically continuously until fuel and oxidant are supplied (Hoogers, 2002).

Fuel cells are clean devices because of its by-products (for example, water when fuel cell fuel is pure hydrogen) and they also operate quietly because they do not have any moving parts. Moreover, they have high power density and effectiveness, commonly more than 40% efficiency in electric power production, which is better than sets of traditional combustion (Gou *et al.*, 2009).

The most common fuel for fuel cells is hydrogen, which may be supplied as almost pure hydrogen or as a major component (50 to 70%) of a reformed fuel stream. Alternatively, a hydrogen-containing component may be used, such as methanol in a direct methanol fuel cell (Li, H. *et al.*, 2010).

Three distinct fuel cell technologies currently exist. Two types are well proven for providing electrolytic alkaline and PEM fuel cell. In general, the PEM fuel cell offers several advantages compared with alkaline fuel cell much higher current densities; smaller mass and volume characteristics; high degree of purity; increased level of safety (no circulation of caustic electrolyte); possibility of combining a fuel cell with electrolyzer modes. A third type usually termed as solid-oxide fuel cell (SOFC), is currently under development and may be viable in the longer term. Practical SOFC operates at high temperature (800 C). They are properly designed to operate in combination with nuclear plants or other technologies where there is an extra amount of heat at a low cost. In safety-critical applications, PEM fuel cell reliability has been extremely high, with units achieving 100,000 h operation without failure (Siracusano *et al.*, 2012).

PEM fuel cell/electrolyzer used in a photovoltaic array to save green energy (Figure 1.1). A photovoltaic array drives a PEM (Proton-Exchange Membrane) fuel cell, producing on-demand electricity to power a load. The only required input is energy to drive the electrolyzer-the water and gases cycle in a closed loop (Shapiro *et al.*, 2005).

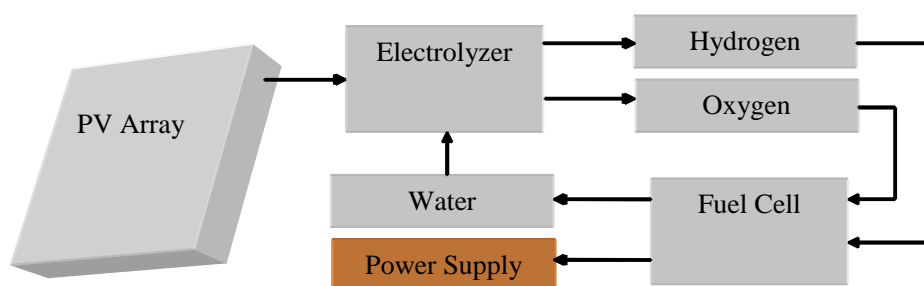
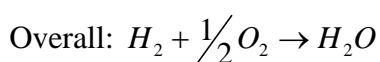
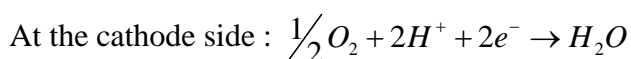
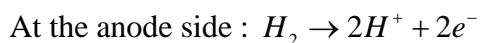


Figure 1.1 Photovoltaic electrolyzer/fuel cell system

The PEM fuel cell schematic is presented in figure 1.2. The PEM fuel cell consists of the solid membrane with gas diffusion layers and the anode and cathode electrodes. An anode and cathode electrode consists of catalyst layer particles, and is fixed to the gas diffusion layer or solid membrane. porous and electrically conductive substance have been used to made the gas diffusion layer , such as carbon cloth, to permeate the fuel feed to diffuse into and out of the PEM, and to collect the resulting

current by providing electric contact between the electrode and the outside bipolar plate. Moreover, it allows the formed water at the cathode electrode to exit to the cathode gas channels. The bipolar plates, also called flow field plates, distribute the reactant gas over the surface of the electrodes through flow channels on their surfaces. (Gou *et al.*, 2009). The electrochemical reactions that happen on both sides of membrane in fuel cell– the anode and cathode electrodes are (Kakaç *et al.*, 2008):



In a PEM fuel cell, both the anodic hydrogen (or liquid fuel) oxidation reaction (HOR) and the cathodic oxygen reduction reaction (ORR) take place within the respective catalyst layers. Electrocatalysts and their corresponding catalyst layers, thus play critical roles in fuel cell performance. In our present state of technology, the most practical catalysts in PEM fuel cells are highly dispersed Pt-based nanoparticles (Zhang, Jiujun, 2008). The heart of the PEM fuel cell is the proton exchange membrane, which transports protons from the anode to the cathode. The membrane also serves to separate the fuel and oxidant gas phases and electronically insulates the cathode from the anode. The most typical membrane is a sulfonated perfluorinated polymer. The Nafion[®] family of membranes made by DuPont is representative of this class, and is based on a sulfonated tetrafluoroethylene based fluoropolymer-copolymer (Li, H. *et al.*, 2010).

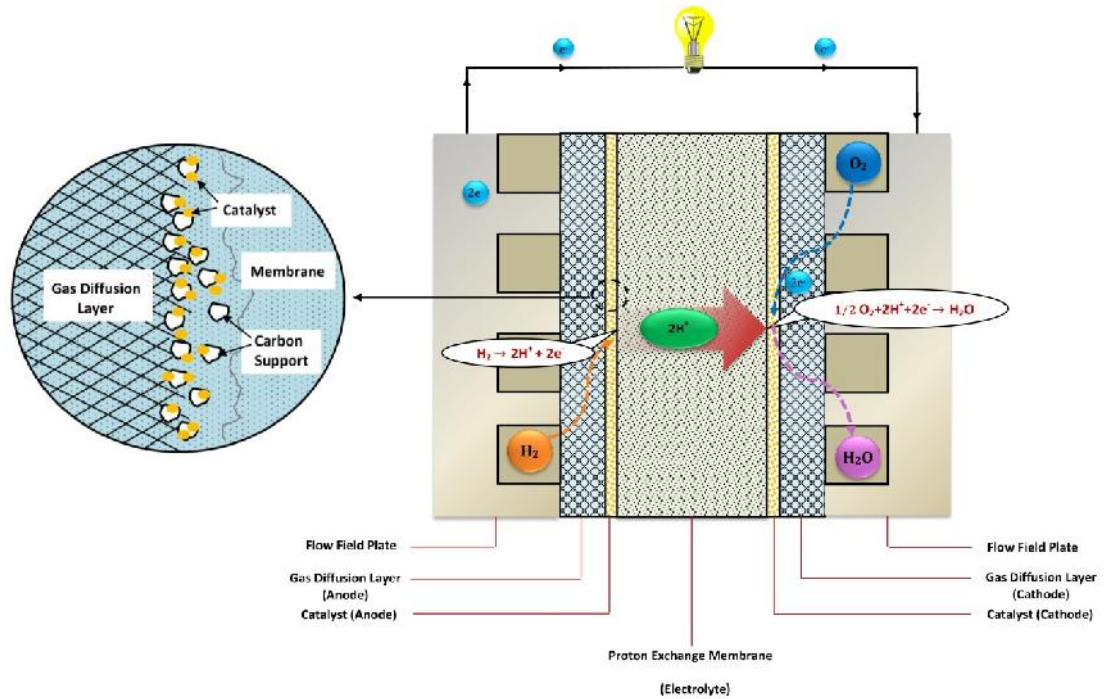


Figure 1.2 PEM fuel cell schematic

1.2 Problem Statements

Increasing the efficiency is the basic reason that modeling and design optimization of PEM fuel cell need to be performed. Several researches by different method and tools have been done to improve the PEM fuel cell but there are still some gap that needed more study. Although many studies available in the literature but simple types of modeling did not have the ability to consider all aspect of cells and stacks development in one single framework (Selamet *et al.*, 2011). The comprehensive model is also very complex. CFD is an emerging technique to investigate the PEMFCs systems. In this situation CFD modeling is close to the real condition and make helpful and easy for scaling-up. According to this literature review, following aspects of CFD modeling of PEM fuel cell problem need to be considered and solved:

Most of modeling domain, such as analytical and semi-empirical do not have the ability to analyze the geometry of the cell. On the other hand, there is no updated framework for mechanistic modeling.

- i. CFD modeling has a potential to be used to investigate the cell geometry since CFD is a powerful tool to model the geometry analysis with high accuracy but there is an doubt on geometry analysis in CFD modelling.
- ii. Flooding is one of the most important phenomena that has a bad effect on PEM fuel cell performance and durability. However, analytical modelling does not have the ability to investigate this phenomenon. CFD modelling has a potential to evaluate the flooding phenomena on the anisotropic gas diffusion layer properties.
- iii. One of the disadvantages of CFD is the calculation time because of solving a set of differential conservation equations in each of the computational zones. Finding the new axillary relations may improve this limitation. The modification of a new approximation to approximate some of the PEMFCs parameters such as electrochemistry properties has a potential in resolving the limitation of the CFD.

1.3 Objective of the Study

The main objective of this study is to develop a systematic computational fluid dynamic modeling framework of PEM fuel cell for electricity generation. These specific objectives were constructed in order to achieve the main objective:

- i. To increase the geometry analysis accuracy of the PEM fuel cell system through grid independence test.
- ii. To evaluate the anisotropic property effects over flooding phenomenon in the PEM fuel cell system.
- iii. To improve the prediction of electrochemistry property relation in a fuel cell system.

1.4 Scope of the Work

In order to achieve the above mentioned objectives, the following scope of work was proposed:

The PEM fuel cell CFD modelling could be conducted in the channel, serpentine (a U type channel), cell or stack system, but in this research it was only conducted for the serpentine system of a cell. Investigations in the serpentine system where the fundamental investigation of PEM FC research. A great potential extended investigations for a cell or a stack system will be easier if these fundamental investigations can successfully be achieved.

- i. An investigation of the geometry analysis accuracy was only applied to the grid independence test. Grid independence test is important because the fuel cell has a simple geometry and focusing on the other aspect of geometry such as mesh adapting will be not necessary.

- ii. The anisotropic properties effect on the flooding phenomenon has been investigated only in a gas diffusion layer of the cathode. This investigation is important because, the flooding only happened on the cathode side of the cell and catalyst layer anisotropic properties effect are negligible due to this layer is very thin in thickness.
- iii. The activation overpotential is the electrochemistry property that this research focused to improve the approximation to predict it. Simple approximation can reduce the numerical calculation time in CFD modelling of PEM fuel cell.

1.5 Organization of Thesis

The thesis consists of 7 chapters, chapter 1 outline a brief introduction of PEM fuel cell and background of the research. Then, it is followed by the problem statements, which identify the research direction. Based on the problem statements defined, the objectives and scopes of the elaborate study in details. General overview of different modeling of a PEM fuel cell is presented in chapter 2. The review of thesis objectives also has been presented in chapter two. Chapter 3 describes the computational fluid dynamics methodology for PEM fuel cell modeling. In this chapter the theory behind the electrochemistry modeling, current and mass conservation, liquid water formation and transport phenomena are presented. The results of PEM fuel cell validation have been achieved through the CFD modeling also is presented in chapter 3. Other results according to research objectives are presented in chapter 4 to 6, respectively. Finally, the general conclusion is drawn from this research and some recommendations for the future research are provided in chapter 7.

REFERENCES

- Al-Baghdadi, M., and Sadiq, A. R. (2005). Modelling of proton exchange membrane fuel cell performance based on semi-empirical equations. *Renewable Energy*, 30(10), 1587-1599.
- Al-Baghdadi, M., Sadiq, A. R., Al-Janabi, H., and Shahad, A. K. (2007). Modeling optimizes PEM fuel cell performance using three-dimensional multi-phase computational fluid dynamics model. *Energy Conversion and Management*, 48(12), 3102-3119.
- Allen, J.A., Tulloch, J., Wibberley, L., and Donne, S. W. (2014). Kinetic Analysis of the Anodic Carbon Oxidation Mechanism in a Molten Carbonate Medium. *Electrochimica Acta*, 129, 389-395.
- Almohammadi, K. M., Ingham, D. B., Ma, L., and Pourkashan, M. (2013). Computational fluid dynamics (CFD) mesh independency techniques for a straight blade vertical axis wind turbine. *Energy*, 58, 483-493.
- Anderson, R., Blanco, M., Bi, X., and Wilkinson, D. P. (2012). Anode water removal and cathode gas diffusion layer flooding in a proton exchange membrane fuel cell. *International Journal of Hydrogen Energy*, 37(21), 16093-16103.
- Andersson, M., Paradis, H., Yuan, J., and Sundén, B. (2013). Three dimensional modeling of an solid oxide fuel cell coupling charge transfer phenomena with transport processes and heat generation. *Electrochimica Acta*, 109, 881-893.
- Andreas, H. A., Black, J. M., and Oickle, A. A. Self-discharge in Manganese Oxide Electrochemical Capacitor Electrodes in Aqueous Electrolytes with Comparisons to Faradaic and Charge Redistribution Models. *Electrochimica Acta*, 140, 116-124.
- Apostol, T. M. (2007). *Calculus, volume I*. New Delhi: John Wiley & Sons.
- Artin, E. (1964). *The gamma function*. New York: International Thomson Publishing.

- Arvay, A. (2011). *Proton exchange membrane fuel cell modeling and simulation using Ansys Fluent*. Arizona State University.
- Audichon, T., Mayousse, E., Napporn, T. W., Morais, C., Comminges, C., and Kokoh, K. B. (2014). Elaboration and characterization of ruthenium nano-oxides for the oxygen evolution reaction in a Proton Exchange Membrane Water Electrolyzer supplied by a solar profile. *Electrochimica Acta*, 132, 284-291.
- Baharlou-Houreh, N., and Afshari, E. (2014). Three-dimensional CFD modeling of a planar membrane humidifier for PEM fuel cell systems. *International Journal of Hydrogen Energy*, 39(27), 14969-14979.
- Bao, C., and Zhang, X. (2014). A Nonlinear Relationship between Area-specific and Volume-specific Exchange Current Densities. *Electrochimica Acta*, 130, 785-790.
- Barelli, L., Bidini, G., Gallorini, F., and Ottaviano, A. (2011). Analysis of the operating conditions influence on PEM fuel cell performances by means of a novel semi-empirical model. *International Journal of Hydrogen Energy*, 36(16), 10434-10442.
- Baschuk, J. J., and Li, X. (2000). Modelling of polymer electrolyte membrane fuel cells with variable degrees of water flooding. *Journal of Power Sources*, 86(1), 181-196.
- Batchelor-McAuley, C., Laborda, E., Henstridge, M. C., Nissim, R., and Compton, R. G. (2013). Reply to comments contained in “Are the reactions of quinones on graphite adiabatic?”, by N.B. Luque, W. Schmickler [Electrochim. Acta xx (2012) yyy]. *Electrochimica Acta*, 88, 895-898.
- Bernardi, D. M., and Verbrugge, M. W. (1991). Mathematical model of a gas diffusion electrode bonded to a polymer electrolyte. *AIChE journal*, 37(8), 1151-1163.
- Berning, T., Lu, D. M., and Djilali, N. (2002). Three-dimensional computational analysis of transport phenomena in a PEM fuel cell. *Journal of Power Sources*, 106(1), 284-294.
- Bhat, M. A., and Ingole, P. P. (2012). Evidence for formation of ion pair stabilized diiodomethane radical anion in 1-butyl-3-methylimidazolium tetrafluoroborate room temperature ionic liquid. *Electrochimica Acta*, 72, 18-22.

- Boscaino, V., Miceli, R., Capponi, G., and Ricco-Galluzzo, G. (2014). A review of fuel cell based hybrid power supply architectures and algorithms for household appliances. *International Journal of Hydrogen Energy*, 39(3), 1195-1209.
- Bove, R., and Ubertini, S. (2008). *Modeling solid oxide fuel cells*. Netherlands: Springer.
- Caston, Terry B., Murphy, Andrew R., & Harris, Tequila A. L. (2011). Effect of weave tightness and structure on the in-plane and through-plane air permeability of woven carbon fibers for gas diffusion layers. *Journal of Power Sources*, 196(2), 709-716.
- Çelik, M., Özı ık, G., Genç, G., and Yapıcı, H. (2014). The Effect of Microporous Layer in Phosphoric Acid Doped Polybenzimidazole Polymer Electrolyte Membrane Fuel Cell. *Journal of Applied Mechanical Engineering*. 3(1), 33-38.
- Chae, J. E., Annaka, K., Hong, K., Lee, S., Munakata, H., Kim, S., and Kanamura, K. (2014). Electrochemical Characterization of Phosphorous-doped Soft Carbon using Single Particle for Lithium Battery Anode. *Electrochimica Acta*, 130, 60-65.
- Chang, C. H., Zhang, M., Lim, J., Choa, Y., Park, S., and Myung, N. V. (2014). Synthesis of PbTe and PbTe/Te Nanostructures by Galvanic Displacement of Cobalt Thin Films. *Electrochimica Acta*, 138, 334-340.
- Cheddie, D., and Munroe, N. (2005). Review and comparison of approaches to proton exchange membrane fuel cell modeling. *Journal of Power Sources*, 147(1), 72-84.
- Cheddie, D., and Munroe, N. (2006). Mathematical model of a PEMFC using a PBI membrane. *Energy Conversion and Management*, 47(11), 1490-1504.
- Chen, F. C., Gao, Z., Loutfy, R. O., and Hecht, M. (2003). Analysis of Optimal Heat Transfer in a PEM Fuel Cell Cooling Plate. *Fuel Cells*, 3(4), 181-188.
- Das, P. K., Li, X., and Liu, Z. (2007). Analytical approach to polymer electrolyte membrane fuel cell performance and optimization. *Journal of Electroanalytical Chemistry*, 604(2), 72-90.
- Debenjak, A., Gašperin, M., Pregelj, B., Atanasijevi -Kunc, M., Petrovi , J., and Jovan, V. (2013). Detection of flooding and drying inside a PEM fuel cell stack. *Strojniski Vestnik/Journal of Mechanical Engineering*, 59(1), 56-64.

- del Real, A. J., Arce, A., and Bordons, C. (2007). Development and experimental validation of a PEM fuel cell dynamic model. *Journal of Power Sources*, 173(1), 310-324.
- Djilali, N. (2007). Computational modelling of polymer electrolyte membrane (PEM) fuel cells: Challenges and opportunities. *Energy*, 32(4), 269-280.
- Engstrom, A. M., Lim, E., Reimer, J. A., and Cairns, E. J. (2014). Anodic Oxidation of COads Derived from Methanol on Pt Electrocatalysts Linked to the Bonding Type and Adsorption Site. *Electrochimica Acta*, 135, 249-254.
- Ferng, Y. M., Tzang, Y. C., Pei, B. S., Sun, C. C., and Su, A. (2004). Analytical and experimental investigations of a proton exchange membrane fuel cell. *International Journal of Hydrogen Energy*, 29(4), 381-391.
- Ferng, Y. M., and Su, A. (2007). A three-dimensional full-cell CFD model used to investigate the effects of different flow channel designs on PEMFC performance. *International Journal of Hydrogen Energy*, 32(17), 4466-4476.
- Fukuyama, Y., Shiomi, T., Kotaka, T., and Tabuchi, Y. (2014). The Impact of Platinum Reduction on Oxygen Transport in Proton Exchange Membrane Fuel Cells. *Electrochimica Acta*, 117, 367-378.
- Ge, S., and Yi, B. (2003). A mathematical model for PEMFC in different flow modes. *Journal of Power Sources*, 124(1), 1-11.
- Ghaznavi, M., and Chen, P. (2014). Analysis of a Mathematical Model of Lithium-Sulfur Cells Part III: Electrochemical Reaction Kinetics, Transport Properties and Charging. *Electrochimica Acta*, 137, 575-585.
- Giurgea, S., Tirmovan, R., Hissel, D., and Outbib, R. (2013). An analysis of fluidic voltage statistical correlation for a diagnosis of PEM fuel cell flooding. *International Journal of Hydrogen Energy*, 38(11), 4689-4696.
- Gou, B., Na, W., and Diong, B. (2009). *Fuel cells: modeling, control, and applications*: CRC press.
- Gurau, V., Barbir, F., and Liu, H. (2000). An Analytical Solution of a Half-Cell Model for PEM Fuel Cells. *Journal of The Electrochemical Society*, 147(7), 2468-2477.
- Gurau, V., Liu, H., and Kakaç, S. (1998). Two-dimensional model for proton exchange membrane fuel cells. *AIChE Journal*, 44(11), 2410-2422.

- Guvelioglu, G. H., and Stenger, H. G. (2005). Computational fluid dynamics modeling of polymer electrolyte membrane fuel cells. *Journal of Power Sources*, 147(1), 95-106.
- Haji, S. (2011). Analytical modeling of PEM fuel cell i–V curve. *Renewable Energy*, 36(2), 451-458.
- Hamour, M., Garnier, J. P., Grandidier, J.C., Ouibrahim, A., and Martemianov, S. (2011). Thermal-Conductivity Characterization of Gas Diffusion Layer in Proton Exchange Membrane Fuel Cells and Electrolyzers Under Mechanical Loading. *International Journal of Thermophysics*, 32(5), 1025-1037.
- Han, S. H., Choi, N. H., and Choi, Y. D. (2012). Study on the flooding phenomena and performance enhancement of PEM fuel cell applying a Concus-Finn condition. *Renewable Energy*, 44, 88-98.
- Haraldsson, K., and Wipke, K. (2004). Evaluating PEM fuel cell system models. *Journal of Power Sources*, 126(1), 88-97.
- He, G., Yamazaki, Y., and Abudula, A. (2010). A three-dimensional analysis of the effect of anisotropic gas diffusion layer(GDL) thermal conductivity on the heat transfer and two-phase behavior in a proton exchange membrane fuel cell(PEMFC). *Journal of Power Sources*, 195(6), 1551-1560.
- He, Z., Liu, J., Han, H., Chen, Y., Zhou, Z., Zheng, S., and He, Z. (2013). Effects of organic additives containing NH₂ and SO₃H on electrochemical properties of vanadium redox flow battery. *Electrochimica Acta*, 106, 556-562.
- Henstridge, M. C., Wang, Y., Limon-Petersen, J. G., Laborda, E., and Compton, R. G. (2011). An experimental comparison of the Marcus–Hush and Butler–Volmer descriptions of electrode kinetics applied to cyclic voltammetry. The one electron reductions of europium (III) and 2-methyl-2-nitropropane studied at a mercury microhemisphere electrode. *Chemical Physics Letters*, 517(1), 29-35.
- Henstridge, M. C., Laborda, E., Rees, N. V., and Compton, R. G. (2012). Marcus–Hush–Chidsey theory of electron transfer applied to voltammetry: A review. *Electrochimica Acta*, 84, 12-20.
- Henstridge, M. C., Ward, K. R., and Compton, R. G. (2014). The Marcus-Hush model of electrode kinetics at a single nanoparticle. *Journal of Electroanalytical Chemistry*, 712, 14-18.
- Hoogers, G. (2002). *Fuel cell technology handbook*: CRC press.

- Hou, Y., Yang, Z., and Wan, G. (2010). An improved dynamic voltage model of PEM fuel cell stack. *International Journal of Hydrogen Energy*, 35(20), 11154-11160.
- Hou, Y., Zhuang, M., and Wan, G. (2007). A transient semi-empirical voltage model of a fuel cell stack. *International Journal of Hydrogen Energy*, 32(7), 857-862.
- Huang, J., Zhang, J., Li, Z., Song, S., and Wu, N. (2014). Exploring Differences between Charge and Discharge of LiMn₂O₄/Li Half-cell with Dynamic Electrochemical Impedance Spectroscopy. *Electrochimica Acta*, 131, 228-235.
- Huisseune, H., Willockx, A., and De-Paepe, M. (2008). Semi-empirical along-the-channel model for a proton exchange membrane fuel cell. *International Journal of Hydrogen Energy*, 33(21), 6270-6280.
- Huth, A., Schaar, B., and Oekermann, T. (2009). A “proton pump” concept for the investigation of proton transport and anode kinetics in proton exchange membrane fuel cells. *Electrochimica Acta*, 54(10), 2774-2780.
- Hutzenlaub, T., Thiele, S., Paust, N., Spotnitz, R., Zengerle, R., and Walchshofer, C. (2014). Three-dimensional electrochemical Li-ion battery modelling featuring a focused ion-beam/scanning electron microscopy based three-phase reconstruction of a LiCoO₂ cathode. *Electrochimica Acta*, 115, 131-139.
- Iranzo, A., Muñoz, M., Rosa, F., and Pino, J. (2010). Numerical model for the performance prediction of a PEM fuel cell. Model results and experimental validation. *International Journal of Hydrogen Energy*, 35(20), 11533-11550.
- Ismail, M. S., Damjanovic, T., Ingham, D. B., Pourkashanian, M., and Westwood, A. (2010). Effect of polytetrafluoroethylene-treatment and microporous layer-coating on the electrical conductivity of gas diffusion layers used in proton exchange membrane fuel cells. *Journal of Power Sources*, 195(9), 2700-2708.
- Ismail, M. S., Hughes, K. J., Ingham, D. B., Ma, L., and Pourkashanian, M. (2012). Effects of anisotropic permeability and electrical conductivity of gas diffusion layers on the performance of proton exchange membrane fuel cells. *Applied Energy*, 95, 50-63.
- Ismail, M. S., Hughes, K. J., Ingham, D. B., Ma, L., and Pourkashanian, M. (2012). Effects of anisotropic permeability and electrical conductivity of gas

- diffusion layers on the performance of proton exchange membrane fuel cells. *Applied Energy*, 95, 50-63.
- Jamekhorshid, A., Karimi, G., and Noshadi, I. (2011). Current distribution and cathode flooding prediction in a PEM fuel cell. *Journal of the Taiwan Institute of Chemical Engineers*, 42(4), 622-631.
- Jang, J., Yan, W., Li, H., and Tsai, W. (2008). Three-dimensional numerical study on cell performance and transport phenomena of PEM fuel cells with conventional flow fields. *International Journal of Hydrogen Energy*, 33(1), 156-164.
- Jiao, K., Zhou, B., and Quan, P. (2006). Liquid water transport in parallel serpentine channels with manifolds on cathode side of a PEM fuel cell stack. *Journal of Power Sources*, 154(1), 124-137.
- Ju, H., Meng, H., and Wang, C. (2005). A single-phase, non-isothermal model for PEM fuel cells. *International Journal of Heat and Mass Transfer*, 48(7), 1303-1315.
- Kakaç, S., Pramuanjaroenkij, A., and Vasil ev, L. L. (2008). *Mini-Micro Fuel Cells: Fundamentals and Applications*: Springer.
- Kamarajugadda, S., and Mazumder, S. (2008). On the implementation of membrane models in computational fluid dynamics calculations of polymer electrolyte membrane fuel cells. *Computers & Chemical Engineering*, 32(7), 1650-1660.
- Kang, S., Zhou, B., Cheng, C., Shiu, H., and Lee, C. (2011). Liquid water flooding in a proton exchange membrane fuel cell cathode with an interdigitated design. *International Journal of Energy Research*, 35(15), 1292-1311.
- Khan, M. A., Sundén, B., and Yuan, J. (2011). Analysis of multi-phase transport phenomena with catalyst reactions in polymer electrolyte membrane fuel cells—a review. *Journal of Power Sources*, 196(19), 7899-7916.
- Klein, R. I. (1999). Star formation with 3-D adaptive mesh refinement: the collapse and fragmentation of molecular clouds. *Journal of Computational and Applied Mathematics*, 109(1), 123-152.
- Kostevšek, N., Rožman, K. Ž., Pe ko, D., Pihlar, B., and Kobe, S. (2014). A comparative study of the electrochemical deposition kinetics of iron-palladium alloys on a flat electrode and in a porous alumina template. *Electrochimica Acta*, 125, 320-329.

- Kulikovsky, A. A., Wüster, T., Egmen, A., and Stolten, D. (2005). Analytical and numerical analysis of PEM fuel cell performance curves. *Journal of the Electrochemical Society*, 152(6), A1290-A1300.
- Laborda, E., Suwatchara, D., Rees, N. V., Henstridge, M. C., Molina, A., and Compton, R. G. (2013). Variable temperature study of electro-reduction of 3-nitrophenolate via cyclic and square wave voltammetry: Molecular insights into electron transfer processes based on the asymmetric Marcus–Hush model. *Electrochimica Acta*, 110, 772-779.
- Larbi, B., Alimi, W., Chouikh, R., and Guizani, A. (2013). Effect of porosity and pressure on the PEM fuel cell performance. *International Journal of Hydrogen Energy*, 38(20), 8542-8549.
- Le, A. D., and Zhou, B. (2010). A numerical investigation on multi-phase transport phenomena in a proton exchange membrane fuel cell stack. *Journal of Power Sources*, 195(16), 5278-5291.
- Li, H., Knights, S., Shi, Z., Van-Zee, J. W., and Zhang, J. (2010). *Proton exchange membrane fuel cells: contamination and mitigation strategies*: CRC Press.
- Li, P., Yuan, S., Tang, Q., and He, B. (2014). Robust conducting gel electrolytes for efficient quasi-solid-state dye-sensitized solar cells. *Electrochimica Acta*, 137, 57-64.
- Litster, S., and Djilali, N. (2007). Mathematical modelling of ambient air-breathing fuel cells for portable devices. *Electrochimica Acta*, 52(11), 3849-3862.
- Liu, Y., and Mustain, W. E. (2014). Stability limitations for Pt/Sn–In₂O₃ and Pt/In–SnO₂ in acidic electrochemical systems. *Electrochimica Acta*, 115, 116-125.
- Lu, L., Ouyang, M., Huang, H., Pei, P., and Yang, F. (2007). A semi-empirical voltage degradation model for a low-pressure proton exchange membrane fuel cell stack under bus city driving cycles. *Journal of Power Sources*, 164(1), 306-314.
- Maggio, G., Recupero, V., and Pino, L. (2001). Modeling polymer electrolyte fuel cells: an innovative approach. *Journal of Power Sources*, 101(2), 275-286.
- Maharudrayya, S., Jayanti, S., and Deshpande, A. P. (2004). Pressure losses in laminar flow through serpentine channels in fuel cell stacks. *Journal of Power Sources*, 138(1), 1-13.

- Malavé, V., Berger, J. R., Zhu, H., and Kee, R. J. (2014). A Computational Model of the Mechanical Behavior within Reconstructed Li_xCoO_2 Li-ion Battery Cathode Particles. *Electrochimica Acta*, 130, 707-717.
- Mazumder, S. (2005). A Generalized Phenomenological Model and Database for the Transport of Water and Current in Polymer Electrolyte Membranes. *Journal of The Electrochemical Society*, 152(8), A1633-A1644.
- McNaughton, J., Afgan, I., Apsley, D. D., Rolfo, S., Stallard, T., and Stansby, P. K. (2014). A simple sliding-mesh interface procedure and its application to the CFD simulation of a tidal-stream turbine. *International Journal for Numerical Methods in Fluids*, 74(4), 250-269.
- Meiler, M., Schmid, O., Schudy, M., and Hofer, E. P. (2008). Dynamic fuel cell stack model for real-time simulation based on system identification. *Journal of Power Sources*, 176(2), 523-528.
- Mendoza-Hernandez, O. S., Ishikawa, H., Nishikawa, Y., Maruyama, Y., Sone, Y., and Umeda, M. (2014). State of Charge Dependency of Graphitized-Carbon-Based Reactions in a Lithium-ion Secondary Cell Studied by Electrochemical Impedance Spectroscopy. *Electrochimica Acta*, 131, 168-173.
- Meng, H. (2006a). A simplified method for solving anisotropic transport phenomena in PEM fuel cells. *Journal of Power Sources*, 161(1), 466-469.
- Meng, H. (2006b). A three-dimensional PEM fuel cell model with consistent treatment of water transport in MEA. *Journal of Power Sources*, 162(1), 426-435.
- Meng, H. (2007). A two-phase non-isothermal mixed-domain PEM fuel cell model and its application to two-dimensional simulations. *Journal of Power Sources*, 168(1), 218-228.
- Meng, H., and Wang, C. (2004). Large-scale simulation of polymer electrolyte fuel cells by parallel computing. *Chemical Engineering Science*, 59(16), 3331-3343.
- Miansari, M., Sedighi, K., Amidpour, M., Alizadeh, E., and Miansari, M. (2009). Experimental and thermodynamic approach on proton exchange membrane fuel cell performance. *Journal of Power Sources*, 190(2), 356-361.
- Moreira, M. V., and Da-Silva, G. E. (2009). A practical model for evaluating the performance of proton exchange membrane fuel cells. *Renewable Energy*, 34(7), 1734-1741.

- Mosiątek, M., Nowak, P., Dudek, M., and Mordarski, G. (2014). Oxygen reduction at the Ag|Gd_{0.2}Ce_{0.8}O_{1.9} interface studied by electrochemical impedance spectroscopy and cyclic voltammetry at the silver point electrode. *Electrochimica Acta*, 120, 248-257.
- Najjari, M., Khemili, F., and Ben-Nasrallah, S. (2013). The effects of the gravity on transient responses and cathode flooding in a proton exchange membrane fuel cell. *International Journal of Hydrogen Energy*, 38(8), 3330-3337.
- Naterer, G. F., Tokarz, C. D., and Avsec, J. (2006). Fuel cell entropy production with ohmic heating and diffusive polarization. *International Journal of Heat and Mass Transfer*, 49(15), 2673-2683.
- Nguyen, P. T., Berning, T., and Djilali, N. (2004). Computational model of a PEM fuel cell with serpentine gas flow channels. *Journal of Power Sources*, 130(1), 149-157.
- Ni, M., Leung, M. K., and Leung, D. Y. C. (2007). Parametric study of solid oxide fuel cell performance. *Energy Conversion and Management*, 48(5), 1525-1535.
- Nikooee, E., Karimi, G., and Li, X. (2011). Determination of the effective thermal conductivity of gas diffusion layers in polymer electrolyte membrane fuel cells: a comprehensive fractal approach. *International Journal of Energy Research*, 35(15), 1351-1359.
- Noren, D., and Hoffman, M. (2005). Clarifying the Butler–Volmer equation and related approximations for calculating activation losses in solid oxide fuel cell models. *Journal of Power Sources*, 152, 175-181.
- Oberkampf, W. L., and Trucano, T. G. (2002). Verification and validation in computational fluid dynamics. *Progress in Aerospace Sciences*, 38(3), 209-272.
- Orvananos, B., Malik, R., Yu, H., Abdellahi, A., Grey, C. P., Ceder, G., and Thornton, K. (2014). Architecture Dependence on the Dynamics of Nano-LiFePO₄ Electrodes. *Electrochimica Acta*, 137, 245-257.
- Pasaogullari, U., Mukherjee, P. P., Wang, C., and Chen, K. S. (2007). Anisotropic heat and water transport in a PEFC cathode gas diffusion layer. *Journal of the Electrochemical Society*, 154(8), B823-B834.
- Patankar, S. (1980). *Numerical heat transfer and fluid flow*: CRC Press.

- Pisani, L., Murgia, G., Valentini, M., and D'-Aguanno, B. (2002). A new semi-empirical approach to performance curves of polymer electrolyte fuel cells. *Journal of Power Sources*, 108(1), 192-203.
- Pisani, L., Valentini, M., and Murgia, G. (2003). Analytical Pore Scale Modeling of the Reactive Regions of Polymer Electrolyte Fuel Cells. *Journal of The Electrochemical Society*, 150(12), A1549-A1559.
- Rodchanarowan, A., Sarswat, P. K., Bhide, R., and Free, M. L. (2014). Production of copper from minerals through controlled and sustainable electrochemistry. *Electrochimica Acta*. 140, 447-456.
- Rosalina, K. M., Kumari, K. N., and Kumar, N. P. (2013). Modeling of Fuel Cell Electrical Supply Management System for Onboard Marine Application. *International Journal of Advanced Research in Computer Engineering & Technology (IJARCET)*, 2(4), 1574-1578.
- Rowe, A., and Li, X. (2001). Mathematical modeling of proton exchange membrane fuel cells. *Journal of Power Sources*, 102(1), 82-96.
- Sadeghi, E., Djilali, N., and Bahrami, M. (2010). Effective thermal conductivity and thermal contact resistance of gas diffusion layers in proton exchange membrane fuel cells. Part 2: Hysteresis effect under cyclic compressive load. *Journal of Power Sources*, 195(24), 8104-8109.
- Sadeghi, E., Djilali, N., and Bahrami, M. (2011a). Effective thermal conductivity and thermal contact resistance of gas diffusion layers in proton exchange membrane fuel cells. Part 1: Effect of compressive load. *Journal of Power Sources*, 196(1), 246-254.
- Sadeghi, E., Djilali, N., and Bahrami, M. (2011b). A novel approach to determine the in-plane thermal conductivity of gas diffusion layers in proton exchange membrane fuel cells. *Journal of Power Sources*, 196(7), 3565-3571.
- Sadeghifar, H., Bahrami, M., and Djilali, N. (2013). A statistically-based thermal conductivity model for fuel cell Gas Diffusion Layers. *Journal of Power Sources*, 233, 369-379.
- Scherer, G. G., and Gürsel, S. A. (2008). *Fuel cells I*: Springer.
- Scott, Keith, & Mamlouk, M. (2009). A cell voltage equation for an intermediate temperature proton exchange membrane fuel cell. *International Journal of Hydrogen Energy*, 34(22), 9195-9202.

- Scrivano, G., Piacentino, A., and Cardona, F. (2009). Experimental characterization of PEM fuel cells by micro-models for the prediction of on-site performance. *Renewable Energy*, 34(3), 634-639.
- Selamet, Ö. F., Becerikli, F., Mat, M. D., and Kaplan, Y. (2011). Development and testing of a highly efficient proton exchange membrane (PEM) electrolyzer stack. *International Journal of Hydrogen Energy*, 36(17), 11480-11487.
- Senarathna, K. G. C., Mantilaka, M. M. M. G. P. G., Peiris, T. A. N., Pitawala, H. M. T. G. A., Karunaratne, D. G. G. P., and Rajapakse, R. M. G. (2014). Convenient routes to synthesize uncommon vaterite nanoparticles and the nanocomposites of alkyd resin/polyaniline/vaterite: The latter possessing superior anticorrosive performance on mild steel surfaces. *Electrochimica Acta*, 117, 460-469.
- Shapiro, D., Duffy, J., Kimble, M., and Pien, M. (2005). Solar-powered regenerative PEM electrolyzer/fuel cell system. *Solar Energy*, 79(5), 544-550.
- Sharma, M., Bajracharya, S., Gildemyn, S., Patil, S. A., Alvarez-Gallego, Y., Pant, D., Dominguez-Benetton, X. (2014). A critical revisit of the key parameters used to describe microbial electrochemical systems. *Electrochimica Acta*. 140, 191-208.
- Shou, D., Tang, Y., Ye, L., Fan, J., and Ding, F. (2013). Effective permeability of gas diffusion layer in proton exchange membrane fuel cells. *International Journal of Hydrogen Energy*, 38(25), 10519-10526.
- Siegel, C. (2008). Review of computational heat and mass transfer modeling in polymer-electrolyte-membrane (PEM) fuel cells. *Energy*, 33(9), 1331-1352.
- Siegel, N. P., Ellis, M. W., Nelson, D. J., and Von-Spakovsky, M. R. (2004). A two-dimensional computational model of a PEMFC with liquid water transport. *Journal of Power Sources*, 128(2), 173-184.
- Singhal, S. (2003). *High-temperature Solid Oxide Fuel Cells: Fundamentals, Design and Applications: Fundamentals, Design and Applications*: Elsevier.
- Siracusano, S., Baglio, V., Briguglio, N., Brunaccini, G., Di-Blasi, A., Stassi, A., and Aricò, A. S. (2012). An electrochemical study of a PEM stack for water electrolysis. *International Journal of Hydrogen Energy*, 37(2), 1939-1946.
- Sivertsen, B. R., and Djilali, N. (2005). CFD-based modelling of proton exchange membrane fuel cells. *Journal of Power Sources*, 141(1), 65-78.

- Song, C., Tang, Y., Zhang, J. L., Zhang, J., Wang, H., Shen, J., and Kozak, P. (2007). PEM fuel cell reaction kinetics in the temperature range of 23–120 C. *Electrochimica Acta*, 52(7), 2552-2561.
- Sørensen, B. (2012). *Hydrogen and fuel cells: Emerging technologies and applications*: Academic Press.
- Spiegel, C. (2011). *PEM fuel cell modeling and simulation using MATLAB*: Academic Press.
- Springer, T. E., Zawodzinski, T.A., and Gottesfeld, S. (1991). Polymer electrolyte fuel cell model. *Journal of the Electrochemical Society*, 138(8), 2334-2342.
- Standaert, F., Hemmes, K., and Woudstra, N. (1996). Analytical fuel cell modeling. *Journal of Power Sources*, 63(2), 221-234.
- Standaert, F., Hemmes, K., and Woudstra, N. (1998). Analytical fuel cell modeling; non-isothermal fuel cells. *Journal of Power Sources*, 70(2), 181-199.
- Stempien, J. P., Sun, Q., and Chan, S. H. (2014). Theoretical consideration of Solid Oxide Electrolyzer Cell with zirconia-based electrolyte operated under extreme polarization or with low supply of feedstock chemicals. *Electrochimica Acta*, 130, 718-727.
- Sui, P. C., Kumar, S., and Djilali, N. (2008). 3-D modelling of a proton exchange membrane fuel cell with anisotropic material properties. *2008 AIChE Annual Meeting*. New York, USA.
- Tang, H., and Pesic, B. (2014). Electrochemistry of ErCl₃ and morphology of erbium electrodeposits produced on Mo substrate in early stages of electrocrystallization from LiCl–KCl molten salts. *Electrochimica Acta*, 133, 224-232.
- Tant, S., Rosini, S., Thivel, P. X., Druart, F., Rakotondrainibe, A., Geneston, T., and Bultel, Y. (2014). An algorithm for diagnosis of proton exchange membrane fuel cells by electrochemical impedance spectroscopy. *Electrochimica Acta*, 135, 368-379.
- Tatsukawa, E., and Tamura, K. (2014). Activity correction on electrochemical reaction and diffusion in lithium intercalation electrodes for discharge/charge simulation by single particle model. *Electrochimica Acta*, 115, 75-85.
- Tchekwagep, P. M. S., Nansu-Njiki, C. P., Ngameni, E., Arnebrant, T., and Ruzgas, T. (2014). Quantification of BSA concentration by using Ag electrochemistry

- in chloride solution: extension of the linear range. *Electrochimica Acta*, 135, 351-355.
- Ticianelli, E.A., Derouin, C.R., Redondo, A., and Srinivasan, S. (1988). Methods to advance technology of proton exchange membrane fuel cells. *Journal of the Electrochemical Society*, 135(9), 2209-2214.
- Um, S., Wang, C., and Chen, K. S. (2000). Computational fluid dynamics modeling of proton exchange membrane fuel cells. *Journal of the Electrochemical society*, 147(12), 4485-4493.
- Vynnycky, M. (2007). On the modelling of two-phase flow in the cathode gas diffusion layer of a polymer electrolyte fuel cell. *Applied Mathematics and Computation*, 189(2), 1560-1575.
- Wang, C. (2004). Fundamental models for fuel cell engineering. *Chemical Reviews*, 104(10), 4727-4766.
- Wang, L., Husar, A., Zhou, T., and Liu, H. (2003). A parametric study of PEM fuel cell performances. *International Journal of Hydrogen Energy*, 28(11), 1263-1272.
- Wang, Q., Song, D., Navessin, T., Holdcroft, S., and Liu, Z. (2004). A mathematical model and optimization of the cathode catalyst layer structure in PEM fuel cells. *Electrochimica Acta*, 50(2), 725-730.
- Wang, X., and Zhou, B. (2011). Liquid water flooding process in proton exchange membrane fuel cell cathode with straight parallel channels and porous layer. *Journal of Power Sources*, 196(4), 1776-1794.
- Wang, Z., Shi, G., Xia, J., Xia, Y., Zhang, F., Xia, L., and Brito, M. E. (2014). Facile preparation of a Pt/Prussian blue/graphene composite and its application as an enhanced catalyst for methanol oxidation. *Electrochimica Acta*, 121, 245-252.
- Weber, A. Z., and Newman, J. (2004). Modeling transport in polymer-electrolyte fuel cells. *Chemical Reviews*, 104(10), 4679-4726.
- Wei, S. S., Wang, T. H., and Wu, J. S. (2014). Numerical modeling of interconnect flow channel design and thermal stress analysis of a planar anode-supported solid oxide fuel cell stack. *Energy*, 69, 553-561.
- Wishart, J., Dong, Z., and Secanell, M. (2006). Optimization of a PEM fuel cell system based on empirical data and a generalized electrochemical semi-empirical model. *Journal of Power Sources*, 161(2), 1041-1055.

- Wöhr, M., Bolwin, K., Schnurnberger, W., Fischer, M., Neubrand, W., and Eigenberger, G. (1998). Dynamic modelling and simulation of a polymer membrane fuel cell including mass transport limitation. *International Journal of Hydrogen Energy*, 23(3), 213-218.
- Yan, W., Chen, F., Wu, H., Soong, C., and Chu, H. (2004). Analysis of thermal and water management with temperature-dependent diffusion effects in membrane of proton exchange membrane fuel cells. *Journal of Power Sources*, 129(2), 127-137.
- Yang, X., Ye, Q., and Cheng, P. (2014). Oxygen starvation induced cell potential decline and corresponding operating state transitions of a direct methanol fuel cell in galvanostatic regime. *Electrochimica Acta*, 117, 179-191.
- Yu, Y., Zuo, Y., Zuo, C., Liu, X., and Liu, Z. (2014). A Hierarchical Multiscale Model for Microfluidic Fuel Cells with Porous Electrodes. *Electrochimica Acta*, 116, 237-243.
- Zhang, J., Li, H., and Shi, Z. (2010). Effects of hardware design and operation conditions on PEM fuel cell water flooding. *International Journal of Green Energy*, 7(5), 461-474.
- hang, J., Shi, Y., and Cai, N. (2014). An approximate analytical model of reduction of carbon dioxide in solid oxide electrolysis cell by regular and singular perturbation methods. *Electrochimica Acta*, 139, 190-200.
- Zhang, J. (2008). *PEM fuel cell electrocatalysts and catalyst layers: fundamentals and applications*: Springer.
- Zhang, X., Ostadi, H., Jiang, K., and Chen, R. (2014). Reliability of the spherical agglomerate models for catalyst layer in polymer electrolyte membrane fuel cells. *Electrochimica Acta*, 133, 475-483.
- Zhang, Z., Huang, X., Jiang, J., and Wu, B. (2006). An improved dynamic model considering effects of temperature and equivalent internal resistance for PEM fuel cell power modules. *Journal of Power Sources*, 161(2), 1062-1068.
- Zhao, Y., Deng, F., Hu, L., Liu, Y., and Pan, G. (2014). Electrochemical deposition of copper on single-crystal gallium nitride(0001) electrode: nucleation and growth mechanism. *Electrochimica Acta*, 130, 537-542.
- Zhu, F. (2013). Fractal geometry model for through-plane liquid water permeability of fibrous porous carbon cloth gas diffusion layers. *Journal of Power Sources*, 243, 887-890.

- Zhu, H., and Kee, R. J. (2003). A general mathematical model for analyzing the performance of fuel-cell membrane-electrode assemblies. *Journal of Power Sources*, 117(1), 61-74.
- Zhu, X., Sui, P. C., and Djilali, N. (2008). Three-dimensional numerical simulations of water droplet dynamics in a PEMFC gas channel. *Journal of Power Sources*, 181(1), 101-115.