

# ULTIMATE STRENGTH ANALYSIS OF SHIPS PLATE DUE TO CORROSION

ZULFAQIH BIN LAZIM

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To my beloved mother, *Kamariah* and father, *Lazim*, my sisters, *Nuha*, and *Madihah* who are never fail to give me a full of supports in the journey of my study.

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## ABSTRACT

Today in maritime industry, it is a mandatory task to compute the ultimate strength of structural components and their system for structural design and strength assessment based on ultimate limit states. Increasing the number of ship failure because of structural incapable to support the load have gain the motivation and interest to study the ultimate strength of the ship's structure. One of the reason of ship structural failure mainly because of ship's plate corrosion. Through this thesis, the study have found out that decreasing thickness of the plate due to ship's plate corrosion will decrease the critical load of the ship's plate itself. The study concern about compressive uni-axial loading on the ship's plate which resulting linear and nonlinear buckling effect. The critical load of the ship's plate structure is study using method eigenvalue linear buckling analysis by ABAQUS Finite Element Software packaged. The result show that more lower the critical load by the structure, more tendency the structure will fail and reach the un-stability mode of deflection. The ultimate compressive strength on the other hand showing the strength of the ship plate under condition of nonlinear buckling analysis. The condition which ship plate located at the bottom and middle section of bulkhead experienced more compressive stress compare to other part in ship. This is according to maximum moment according to shear force-moment diagram of any ship that gives the maximum moment stress at the middle of the ship. Finding ultimate strength of the ship's plate gives the understanding about the concept of allowable limit load the ship structure can withstand under ship service loading. The parameter of plate slenderness ratio is important for linear and nonlinear ship's plate buckling analysis and the ultimate strength is calculated based on formula by Faulkner.

## ABSTRAK

Hari ini dalam industri maritim, ia merupakan satu tugas yang wajib untuk mengira kekuatan muktamad komponen struktur dan sistem mereka untuk reka bentuk struktur dan penilaian kekuatan berdasarkan keadaan had muktamad. Meningkatnya bilangan kegagalan kapal kerana tidak mampu untuk menyokong beban struktur telah membawa motivasi dan minat untuk mengkaji kekuatan muktamad struktur kapal. Salah satu sebab kegagalan struktur kapal terutamanya kerana pengaratan pada plat kapal. Melalui tesis ini, kajian telah dipelajari bahawa pengurangan ketebalan plat kerana pengaratan pada plat kapal akan mengurangkan beban kritikal plat kapal sendiri. Kajian mengambilkira tentang mampatan beban uni-paksi pada plat kapal yang menyebabkan kesan lengkok linear dan tak linear. Beban kritikal struktur plat kapal adalah kajian menggunakan kaedah lengkok linear '*eigenvalue*' analisis menggunakan '*ABAQUS Finite Element Software packaged*'. Keputusan kajian menunjukkan hasil yang lebih rendah beban kritikal pada struktur, lebih kecenderungan struktur akan gagal dan mencapai mod ketidakstabilan pesongan. Kekuatan mampatan muktamad sebaliknya menunjukkan kekuatan plat kapal dalam keadaan analisis lengkokan tak linear. Keadaan plat kapal yang terletak di bahagian bawah dan bahagian tengah 'bulkhead' kapal mengalami lebih mampatan berbanding dengan bahagian lain dalam kapal. Ini adalah berpandukan momen maksimum mengikut gambarajah ricih-momen mana-mana kapal yang memberikan tekanan momen maksimum di tengah-tengah kapal. Mencari kekuatan muktamad plat kapal memberikan pemahaman tentang konsep beban had yang dibenarkan struktur kapal yang boleh ditahan dalam beban semasa penggunaan kapal. Parameter '*plate slenderness ratio*' adalah penting bagi analisis plat kapal lengkokan linear dan tak linear dan kekuatan muktamad dikira berdasarkan formula oleh Faulkner.

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**LIST OF SYMBOLS**

$\beta$	-	The plate slenderness ratio
b	-	Longitudinal stiffener's plate spacing
a	-	Transverse stiffener's plate spacing
$\sigma_y$	-	Yield's Strength
E	-	Modulus of Elasticity
$\nu$	-	Poisson's Ratio
$\sigma_c$	-	Buckling Stress
$\phi_b$	-	Ratio between buckling stress and yield stress
$R_{xu}$	-	Ultimate strength reduction factor for axial compression loads
$\sigma_{xu}$	-	Ultimate compressive strength for a plate with pit corrosion
$\sigma_{xu0}$	-	Ultimate compressive strength for an intact plate
$A_o$	-	Original cross-sectional area
$A_r$	-	Minimum cross-sectional area with pitting corrosion

**LIST OF ABBREVIATION**

<b>IMO</b>	-	International Maritime Organization
<b>ISSC</b>	-	International Ship and Offshore Congress
<b>ISO</b>	-	International Organization for Standardization
<b>IACS</b>	-	International Association of Classification Societies
<b>FEA</b>	-	Finite Element Analysis
<b>FEM</b>	-	Finite Element Method
<b>ULS</b>	-	Ultimate limit states
<b>CSR</b>	-	Common structural rules
<b>DNV</b>	-	Det Norske Veritas

## CHAPTER 1

### INTRODUCTION

#### 1.1 Introduction

Today in maritime industry, it is a mandatory task to compute the ultimate strength of structural components and their system for structural design and strength assessment based on ultimate limit states (ISO, 2006, 2007; IMO, 2006; IACS, 2006a, b). This is because it is not possible to determine the true margin of structural safety as long as the ultimate strength remains unknown Paik et al, (2008).

Although the ANSYS nonlinear FEA may be the most refined method among the candidate methods, and believed to give the most accurate solutions, it is important to realize that the modelling technique applied must be adequate enough in terms of representing actual structural behaviour associated with geometrical nonlinearity, material nonlinearity, type and magnitude of initial imperfections, boundary condition, loading condition, mesh size, and so on. Otherwise, the resulting computations may be totally wrong. For the present benchmark study purpose, the elastic-perfectly plastic material model is applied for all the candidate methods by neglecting strain-hardening effect of the material.

Buckling strength analysis of plates and stiffened plates was the subject of many researches. (Liu et al, 2008) have used energy method to study elastic stability

of simply supported rectangular plates under any combination of in-plane loads. Maiorana et al. (2008) have analysed elastic buckling of un-stiffened plates under interacting patch loading and bending moment. Steen et al, (2008) have studied elastic buckling and post-buckling of bi-axially compressed plates. Bringhenti, (2005) have investigated buckling failure of plates with cracks.

The project is about method of solving the marine structure problem using FEM software. The selected structure is plate on ship structure, the problem was the safety of the ship by determining the ultimate strength of plate that having pit defect because of aging. This result in the project are compare with result by other researcher having similar size and loading condition of ship plate structure. This considered as influencing variable contributing to the safety factor of the investigated structure. The safety's factor of the structure or safety margin determine from the value of design demand, the value of design demand by the structure is the minima require value for the plate ship structure to be able to deliver its function for overall ship structure.

In world maritime industry, substantial efforts have been directed by various stakeholders such as IMO, ISO, and IACS, toward the application of advanced methodologies such as:

- a) Goal-based design using first-principles-based direct methods;
- b) Limit states-based methods;
- c) Risk-based methods.

The present study is concerned with ultimate limit states (ULS) which are the common aspect of the three technologies noted above. It has been well recognized that the ULS approach is a better basis for design and strength assessment than the traditional allowable working stress approach, the latter being primarily based on linear elastic method solutions alone. This is because it is not possible to determine the true margin of structural safety as long as the ULS remains unknown. While the margin of safety can be determined by a comparison with the ultimate strength and the design



working stress, it is essential to accurately predict the ultimate strength within the design framework.

Some benchmark studies on the methods of ultimate strength computations for plate elements, stiffened panels and ship's hull girders Paik et al, (2008) were previously investigated. In the present study, some useful insights on the application of non-linear finite element (FE) methods are developed in terms of structural modelling. As an illustrative example of the structure, the present study adopts steel stiffened-plate structures which are the most important structural parts in outer bottom of ships and ship-shaped offshore installations. The object structure is considered to be subject of bi-axial compression.

## **1.2 Problem Statement**

Most of ship plate or ship stiffener and ship hull around the world are made of steel. Steel material tend to corrode due to certain environment condition. The ferum oxide  $\text{Fe}(\text{OH})_3$  layer called corrosion form in different rate depending on the situation. In case of chemical ship's carrier, certain chemical rise the rate of corrosion. Although the ship structure made of steel is coating to prevent the corrosion but the coating also wear out due to service life of the vessel and several other reason. Many researcher found out that one of the reason the failure of structure integrity on global ship's structure or local ship's structure because of corrosion. Every year or every agreed period, on the matter of ship structure safety, the port state require to check the ship plate thickness to ensure the safety of the ship. The safety is important in term of ship's business and in aspect of human lives.

The ultimate strength limit state approach is a better basis for design and strength assessment of various types of structures than the traditional allowable working stress approach because it is not possible to determine the true margin of

structural safety as long as the limit states remain unknown. In recent years, substantial efforts by stakeholders such as International Organization for Standardization (ISO), International Maritime Organization (IMO), and classification societies have been directed to the developments of limit state based standards. (Paik et al, 2008)

### **1.3 Objective of the Research**

The objective of the research is finding the ultimate strength of the ship's plate due to corrosion. The corrosion being investigated is general corrosion which is the thickness is decrease uniformly by ship's plate thickness. The project first study about the critical loading on ship's plate and then study the ultimate strength on the ship's plate. The modelling of the ship by parameter of geometry and material properties is referring to previous other publish work.

### **1.4 Scope of the Research**

The scope of the research throughout the master project on the study about ship's plate linear and nonlinear buckling analysis are listed below:

1. The deflection occur only at plates, not at the stiffeners. The geometry of the ship plate fixed.
2. The temperature have no effect, low temperature makes the structure material properties becomes brittle. The effect of the residual stress from the welding are also neglected.
3. There are no effect of welding (residual stress) from assembly between plate and stiffener.
4. Assume the corrosion only uniform corrosion on plate, not other kind of corrosion such as pit corrosion. The corrosion causing uniform thickness

reduction also recognized as general corrosion from the others publish work. (pitting corrosion)

5. Assume the material only use is general material use for plate construction for ship which is mild steel. The material properties of ship's plate based on oil tanker double hull ship plate based on CSR 2006 by IACS of double hull tanker.
6. The study is based only on longitudinal stress uniaxial compression loading on the model.

## **1.5 Significant of the Research**

The significant of the research is being able to find the ultimate strength and critical load of the ship's plate. The ship's plate is fundamental structure of ship's plate which is the first failure happen at the ship plate because the ship plate govern most part of the ship structure. Ship's plate location for example at the side of the ship which is hull, at the deck floor of the ship and at the bottom of the ship. The knowledge of finding ultimate strength by famous researcher which investigated only the ship structure such as Jeom Kee Paik, Faulkner, Shengming Zhang and several other with engage to DNV and IMO classification bodies with the ISSC conference also put the focus of the significant of the project in the higher level.

## REFERENCES

- Thomas Telford 2015 *Modern Structural Analysis: Modelling Process and Guidance*  
Technology & Engineering
- Mohammad Reza Khedmati, Ahmad Reza Rashedi, *Nonlinear finite element modelling and progressive collapse analysis of a product carrier under longitudinal bending*, Applied Ocean Research, Volume 48, October 2014, Pages 80-102, ISSN 0141-1187
- Lars Brubak, Ha'kon Andersen, Jostein Hellesland, *Ultimate strength prediction by semi-analytical analysis of stiffened plates with various boundary conditions*. Thin-Walled Structures 62(2013)28–36
- Stipica Novoselac, Todor, Pavo (2012). *Linear and Nonlinear Buckling and Post Buckling Analysis of a Bar with the Influence of Imperfections*
- J.K. Paik, S.J. Kim, D.H. Kim & D.C. Kim (2011) *Benchmark study on use of ALPS/ULSAP method to determine plate and stiffened panel ultimate strength* ISBN 978-0-415-67771-4
- Mohammad Reza Khedmati, Mohammad Mahdi Roshanali, Zorareh Hadj Mohammad  
Esmail Nouri, *Strength of steel plates with both-sides randomly distributed with corrosion wastage under uniaxial compression*, Thin-Walled Structures, Volume 49, Issue 2, February 2011, Pages 325-342, ISSN 0263-8231,
- Hughes, O.F. and Paik, J.K. 2010. *Ship structural analysis and design*, The Society of Naval Architects and Marine Engineers, New Jersey, USA
- Shengming Zhang, Imtaz Khan, *Buckling and ultimate capability of plates and stiffened panels in axial compression*, Marine Structures, Volume 22, Issue 4, October 2009, Pages 791-808, ISSN 0951-8339,  
<http://dx.doi.org/10.1016/j.marstruc.2009.09.001>.

- Liu YG, Pavlovic MN. *A generalized analytical approach to the buckling of simply-supported rectangular plates under arbitrary loads*. Eng Struct 2008;30(5):1346–59.
- Maiorana E, Pellegrino C, Modena C. *Linear buckling analysis of unstiffened plates subjected to both patch load and bending moment*. Eng Struct 2008;30(12):3731–8.
- Steen E, Byklum E, Hellesland J. *Elastic postbuckling stiffness of biaxially compressed rectangular plates*. Eng Struct 2008;30(10):2631–43.
- Jeom Kee Paik, Bong Ju Kim, Jung Kwan Seo, *Methods for ultimate limit state assessment of ships and ship-shaped offshore structures: Part I—Unstiffened plates*, Ocean Engineering, Volume 35, Issue 2, February 2008, Pages 261-270, ISSN 0029-8018
- Paik JK, Kim BJ, Seo JK. *Methods for ultimate limit state assessment of ships and ship-shaped offshore structures, Part II: stiffened panels*. Ocean Eng 2008; 35:271–80.
- Paik JK, Kim BJ, Seo JK. *Methods for ultimate limit state assessment of ships and ship-shaped offshore structures, Part III: hull girders*. Ocean Eng 2008; 35:281–6.
- ISO 18072-1. *Ships and marine technology-ship structures-Part 1: general requirements for their limit state assessment*. Geneva: International Organization for Standardization; October 2007.
- Paik JK, Thayamballi AK. *Ship-shaped off shore installations: design, building, and operation*. Cambridge, UK: Cambridge University Press; 2007.
- George J. Simitses, Dewey H. Hodges, *Fundamentals of Structural Stability*. Butterworth-Heinemann, 2006 – Science-389 pages
- IACS (2006) *Common structural rules for double hull oil tankers and bulk carriers*, IACS Limited, Permanent Secretariat, 6th Floor, 36 Broadway, London UK.

- IMO. *Goal-based standards*. London: International Maritime Organization; November 2006.
- ISO/CD 18072-2. *Ships and marine technology-ship structures-Part 2: requirements for their ultimate limit state assessment*. Geneva: International Organization for Standardization; November 2006.
- Bringhenti R. *Numerical buckling analysis of compressed or tensioned cracked thin plates*.  
Eng Struct 2005;27(2):265–76.
- Amlashi HKK, Moan T. *On the strength assessment of pitted stiffened plates under biaxial compression loading*. In: Proceedings of 24th international conference on offshore mechanics and arctic engineering, Halkidiki, Greece, paper number OMAE2005-67232; 2005.
- D.A. Danielson, A. Wilmer. 2004. *Buckling of stiffened plates with bulb flat flanges*. International Journal of Solids and Structures 41 (2004) 6407–6427
- Paik JK, Thayamballi AK. *Ultimate limit state design of steel-plated structures*. Chichester, UK: Wiley; 2003.
- Marian Kmiecik, *Usefulness of the yield line theory in design of ship plating*, Marine Structures, Volume 8, Issue 1, 1995, Pages 67-79, ISSN 0951-8339
- C. Guedes Soares, M. Kmiecik, *Simulation of the Ultimate Compressive Strength of Unstiffened Rectangular Plates*, Marine Structures 0951-8339/93/\$06.00 © 1993 Elsevier Science Publishers Ltd, England.
- Guedes Soares, C., *Design equation for the compressive strength of unstiffened plate elements with initial imperfections*. J. Constructional Steel Research, 9 (1988) 287-310.
- Itoh, Y. & Fukumoto, Y., *Stochastic evaluation of compressive strength of unstiffened plate components*. Paper presented at 4th Int Colloquium on Stability of Plate and Shell Structures, Belgium, April 1987.
- C. Guedes Soares and T.H. Soreide, *Behaviour and design of stiffened plates under*

- predominantly compressive loads*, Int. Shipbuild. Prog., 30 (1983) 13-27.
- Guedes Soares, C., *Uncertainty modelling in plate buckling*. Structural Safety, 5 (1988) 17-34.
- Guedes Soares, C. & Faulkner, D., *Probabilistic modelling of the effect of initial imperfections on the compressive strength of rectangular plates*. In Proc. 3rd Int. Symp. on Practical Design of Ships and Mobile Units, Trondheim, 2 (1987) 783-95.
- C. Guedes Soares, *Survey of methods of prediction of the compressive strength of stiffened plates*, Report No. MK/R57, Division of Marine Structures, Norwegian Institute of Technology, Trondheim, Norway, August, 1981.
- L.D. Ivanov and S.G. Rousev, *Statistical estimation of reduction coefficient of ship's hull plates with initial deflections*, Nav. Archit., (4) (1979) 158-160.
- Y. Ueda and T. Yao, *Ultimate strength of a rectangular plate under thrust with consideration of the effects of initial imperfections due to welding*, Trans. J. Weld. Res. Inst. of Osaka University, 8 (2) (1979) 97-104.
- Frieze, P. A., Dowling, P. J. & Hobbs, R. H., *Ultimate load behaviour of plates in compression*. In *Steel Plated Structures*, ed. P. J. Dowling et al. Crosby Lockwood Staples, London, 1977, pp. 24-50.
- Harding, J. E., Hobbs, R. H. & Neal, B. G., *The elasto-plastic analysis of imperfect square plates under in-plane loading*. Proc. Inst. Civil Engineers, 63(2) (1977) 137-58.
- Faulkner DA. *Review of effective plating for the analysis of stiffened plating in bending and compression*. Journal of Ship Research 1975;19(1):1-17.
- Kmieciak, M., *Behaviour of axially loaded simply supported long rectangular plates having initial deformations*. Report No. 84, Ship Research Institute, Trondheim, 1971.

Ueda, Y. & Tall, L., *Inelastic buckling of plates with residual stresses*. Publications Int. Assoc.

for Bridge and Structural Engineering (1967).

Frankland JM. *The strength of ship plating under edge compression*. US EMM report 469

(1940).

von Karman. *Die Millragenc Bricite*, Springer, Berlin (1924).

Box TA. *Practical treatises on the strength of materials*. London: Spon; 1883.