

INVESTIGATION OF EXCITATION COILS CONFIGURATION  
AND PARTICLE SWARM OPTIMIZATION OF COIL'S DIAMETER  
IN MAGNETIC NANOPARTICLES IMAGING

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## ABSTRACT

Magnetic Nanoparticles Imaging (MNI) is a new imaging method which uses magnetic nanoparticles as the contrast agent. The superparamagnetism of ferro- and ferrimaterial allowed the particles to act as a temporary magnet when an external excitation is applied. The imaging is based on the reconstruction of the measured relaxation time (magnetorelaxometry) from the sample by SQUID sensors after the applied field is switched off. To date, the imaging method is still not applicable on human due to many undetermined parameters of the diagnostic configuration. The equation of the reconstruction is generally ill-posed due to the involvement of many parameters in the configuration. Hence, the optimization is required in order to eliminate the unstable parameters of this imaging technique. In this thesis, the study of excitation coils' configuration has been conducted with manipulation of the number coils, arrangement of coils, diameter of coils and the shape of coils. The results show that by increasing the number of coils will improve the correlation coefficient of the reconstruction. However, due to the limitation of the grid size, the size of the coils is another concerned criterion; hence, the total area of the coils in each grid must be smaller than the area of the grid. The correlation coefficients of the reconstruction with varying the coils diameters show an improvement with smaller coils diameter. This observation obeyed the algorithm of diameter optimization in this thesis. Besides, the examinations of the arrangement and shape of coils show that both these criteria are highly depending on the shape of the sample. Due to the size of the rectangular coils used in the simulation are basically larger than the circular coils, hence, better results are found in the circular coils. On the other hand, the examination of the possibility of applying particle swarm optimization (PSO) method on the coils diameter has been studied by constructing the algorithm of the magnetic field calculation. The results of the algorithm construction showed that the diameter element is a non-linear parameter, and it is not suitable to be used in PSO as this method only applicable for the element which poses a linear relationship between the element and the output of optimization.

## ABSTRAK

Pengimejan nanopartikel magnetic merupakan sejenis teknik pengimejan baru yang menggunakan nanopartikel magnet sebagai agen perbandingan. Sifat *superparamagnetism* bahan *ferro-* dan *ferri* membolehkan partikel-partikel berfungsi sebagai magnet sementara apabila pengujaan luaran diaplikasikan. Pengimejan ini beroperasi berdasarkan konsep pembinaan semula tempoh pengenduran (magnetorelaxometry) yang diukur dengan menggunakan penderia SQUID selepas pengujaan luaran dimatikan. Sehingga kini, teknik pengimejan ini masih tidak dapat dipraktikkan pada tubuh manusia disebabkan masih terdapat banyak parameter konfigurasi diaagnostik yang belum dapat dikenal pasti. Secara umumnya, persamaan matematik yang digunakan untuk membina semula imej masih belum terumus dengan baik disebabkan oleh penglibatan terlalu banyak parameter di dalam konfigurasi tersebut. Oleh yang demikian, proses pengoptimuman adalah sangat penting bagi menghapuskan parameter yang tidak stabil di dalam teknik pengimejan ini. Oleh yang demikian, tesis ini membentangkan satu kajian mengenai konfigurasi gegelung medan pengujaan dengan memanipulasikan bilangan, susun atur, diameter dan bentuk gegelung pengujaan. Keputusan kajian ini menunjukkan bahawa, pertambahan bilangan gegelung pengujaan akan meningkatkan pekali korelasi pembinaan semula. Namun begitu, disebabkan oleh limitasi pada saiz grid, saiz pada gegelung pengujaan menjadi kriteria yang turut perlu diteliti; oleh itu, jumlah permukaan gegelung dalam setiap grid mestilah lebih kecil daripada permukaan grid tersebut. Pekali korelasi daripada simulasi dengan pelbagai diameter gegelung menunjukkan peningkatan dengan penggunaan diameter lebih kecil. Pemerhatian ini juga turut mematuhi konsep algoritma optimasi yang diulaskan dalam tesis ini. Selain itu, kajian terhadap susun atur dan bentuk gegelung pengujaan mendapati kedua-duanya sangat bergantung kepada saiz gegelung tersebut. Disebabkan saiz gegelung segi empat yang digunakan dalam simulasi ini lebih besar berbanding saiz gegelung bulat, maka, keputusan yang lebih baik dijumpai pada gegelung bulat. Selain itu, potensi pengaplikasian kaedah *particle swarm optimization (PSO)* pada diameter gegelung juga telah dikenalpasti dengan pembinaan semula algoritma pada pengiraan medan magnet. Hasil daripada algoritma itu menunjukkan bahawa elemen diameter merupakan parameter yang tidak linear, dan ianya tidak sesuai digunakan dalam *PSO* kerana kaedah ini hanya terpakai untuk elemen yang mempunyai hubungan linear diantara elemen tersebut dan hasil optimasi.

## TABLE OF CONTENTS

CHAPTER	TITLE	PAGE
	<b>DECLARATION</b>	ii
	<b>ACKNOWLEDGEMENT</b>	iii
	<b>ABSTRACT</b>	iv
	<b>ABSTRAK</b>	v
	<b>TABLE OF CONTENTS</b>	vi
	<b>LIST OF TABLES</b>	ix
	<b>LIST OF FIGURES</b>	x
	<b>LIST OF ABBREVIATIONS</b>	xii
	<b>LIST OF SYMBOLS</b>	xiii
<b>1</b>	<b>INTRODUCTION</b>	<b>1</b>
	1.1 Background of Study	1
	1.2 Problem Statement	3
	1.3 Objective	4
	1.4 Scope	5
	1.5 Significant of Study	5
<b>2</b>	<b>LITERATURE REVIEW</b>	<b>6</b>
	2.1 Magnetic Nanoparticles	6
	2.2 Principle of Magnetism	9
	2.2.1 Superparamagnetism	9
	2.2.2 Magnetorelaxometry	13
	2.2.3 Measurement of MRX	14
	2.3 Imaging of Magnetic Nanoparticles with MRX	16

2.3.1	MRX as the Tool for Determination of Biodistribution of MNP	16
2.3.2	Source Reconstruction	17
<b>3</b>	<b>METHODOLOGY</b>	<b>19</b>
3.1	Simulation of Magnetic Nanoparticles Imaging	19
3.2	Methodology of Computational Modelling	21
3.2.1	Forward Modelling	21
3.2.2	Lead Field Matrix	24
3.3	Inverse Problem Solution	25
3.3.1	Minimum Norm Estimation	25
3.3.2	Regularization	27
3.4	Determination of the Sensitivity Distribution In Volume	28
3.5	Magnetic Field Activation	31
3.5.1	Homogeneous Field Activation	31
3.5.2	Inhomogeneous Field Activation	32
3.6	Implementation	34
3.6.1	Simulation Configuration	34
3.7	Particle Swarm Optimization	35
3.7.1	Basic Principle	35
3.7.2	Social Model	36
<b>4</b>	<b>SIMULATION</b>	<b>37</b>
4.1	Implementation Program of Magnetic Nanoparticles Imaging	37
4.2	Simulation of Coils Configuration	41
4.2.1	Effects of the Number of Coils	41
4.2.2	Effects of the Arrangement of Coils	43
4.2.3	Effects of the Diameter of Coils	54
4.2.4	Effects of the Shape of Coils	54
4.2.5	Effects of the Offset of TSVD	55
4.3	Algorithm of Particle Swarm Optimization	

	for Coils Diameter	56
<b>5</b>	<b>RESULT AND DISCUSSION</b>	<b>61</b>
5.1	Result of Simulation	61
5.1.1	Simulation with Different Number of Coils	61
5.1.2	Simulation with Different Arrangement of Coils	63
5.1.3	Simulation with Different Diameter of Coils	66
5.1.4	Simulation with Different Shape of Coils	69
5.1.5	Simulation with Different Offset of TSVD	71
5.2	Discussion	72
<b>6</b>	<b>CONCLUSION AND RECOMMENDATION</b>	<b>81</b>
6.1	Conclusion	82
6.2	Recommendation	83
	<b>REFERENCES</b>	<b>84</b>
	APPENDIX A	90

**LIST OF TABLES**

<b>TABLE NO.</b>	<b>TITLE</b>	<b>PAGE</b>
4.1	Initial configuration of simulation for magnetic nanoparticle imaging	38
4.2	Coil configuration and the schematic illustration for the simulation of the effects of coils number	42
4.3	Coils configurations and schematic illustration of different coils arrangements	44
5.1	Reconstruction results of the simulation with different number of coils	62
5.2	Reconstruction results of simulation with different coils arrangement with homogeneous activation and sequential activation	64
5.3	Results of the simulation with different coils diameters for four coils for each grid	66
5.4	Results of the simulation with different coils diameters for nine coils for each grid	68
5.5	Results of the simulation with rectangular coils	69
5.6	Correlation coefficient of the reconstructed results with different offset of TSVD	71



## LIST OF FIGURES

FIGURE NO.	TITLE	PAGE
2.1	The blocked state and superparamagnetic state of nanoparticles	11
2.2	Schematic illustration of the principle of Magnetorelaxometry	13
3.1	General procedures of magnetic nanoparticles imaging computation	20
3.2	Schematic drawing of magnetic field measurement from line segment to $i$ -th voxel	31
3.3	Schematic illustration of the simulation configuration of homogeneous field activation	32
3.4	Schematic diagram of the simulation setting for inhomogeneous field activation	33
4.1	Schematic illustration of the sensors	38
4.2	The schematic illustration of initial configuration of simulation for magnetic nanoparticle imaging	40
4.3	Shepp-Logan phantom	40
4.4	Schematic illustration of rectangular coils for one grid	55
4.5	Replacement of diameter of the circular coil to the diagonal of rectangular coil	55
4.6	Illustration of the segmented coil (8 segments) and the schematic drawing for the vector $\vec{a}$ and $\vec{b}$	57
5.1	Comparison of the arrangement of coils for 4 coils for each grid configuration	74
5.2	Comparison of the arrangement of coils for 5 coils for each grid configuration	75

5.3	Comparison of the arrangement of coils for 6 coils for each grid configuration	76
5.4	Comparison of the arrangement of coils for 7 coils for each grid configuration	77
5.5	Comparison of the arrangement of coils for 9 coils for each grid configuration	78
5.6	Schematic illustration of the position vectors of two different diameters of coils	79

## LIST OF ABBREVIATIONS

STM	-	Scanning Tunneling Microscope
AFM	-	Atomic Force Microscope
MNP	-	Magnetic nanoparticles
MPI	-	Magnetic Particle Imaging
MRI	-	Magnetic Resonance Imaging
MNI	-	Magnetic Nanoparticles Imaging
(U)SPIO	-	(Ultrasmall) Superparamagnetic Iron Oxide nanoparticles
MRX	-	Magnetorelaxometry
ACS	-	Alternating Current Susceptometry
SQUID	-	Superconducting Quantum Interference Device
<i>L</i>	-	Lead Field Matrix
TSVD	-	Truncated Singular Value Decomposition
PSO	-	Particle Swarm Optimization
GBEST	-	Global Best
LBEST	-	Local Best

## LIST OF SYMBOLS

$\tau_N$	-	Néel relaxation time
$\tau_0$	-	Time characteristic of probed material
$\Delta E$	-	Energy barrier threshold for the magnetization flip
$k_B$	-	Boltzmann constant
$T$	-	Temperature
$\tau_m$	-	Measured time
$\tau$	-	Relaxation time
$T_B$	-	Blocking temperature
$T_C$	-	Currie temperature
$K$	-	Anisotropy constant
$V_p$	-	Particles volume
$\vec{n}$	-	Particle preferred direction
$\vec{m}$	-	Particle magnetic moment vector
$\tau_B$	-	Brownian relaxation time
$\eta$	-	Viscosity of the carrier liquid
$V_{hydr}$	-	Hydrodynamic volume
$\tau_{eff}$	-	Effective time constant
$\vec{B}_{exc}$	-	External magnetic field
$t_{exc}$	-	Excitation time
$t_{del}$	-	Delay time
$t_{mag}$	-	Magnetization time
$r$	-	Distance from magnetic source
$\vec{H}$	-	Magnetic field
$\chi_v$	-	Isotropic magnetic volume susceptibility

$N_p$	-	Concentration of the nanoparticles
$\mu$	-	Magnetic moment of a single particle
$\delta\vec{m}$	-	Dipole moment
$\delta V$	-	Volume element
$\vec{r}$	-	Voxel location vector
$\vec{r}_s$	-	Sensor location vector
$\delta\vec{B}$	-	Dipole field
$d_i$	-	Unity vector
$m_i$	-	Magnitude of unity vector
$\vec{w}_j$	-	Weight of $j$ -th sensor
$\vec{d}_j$	-	Direction of $j$ -th sensor
$\vec{b}_f$	-	Forward computed field
$\vec{b}_m$	-	Measured field
$L^T$	-	Transpose of lead field matrix
$L^+$	-	Pseudo inverse of $L$
$\sigma_r$	-	Regularization parameter
$\vec{I}$	-	Current
$A_1$	-	Relation of $\vec{I}$ to $\vec{H}$
$\vec{a}$	-	Position vector of initial point of line segment
$\vec{b}$	-	Position vector of end point of line segment
$\vec{r}_0$	-	Position vector of voxel
$\vec{r}_1$	-	Vector from $\vec{a}$ to $\vec{r}_0$
$\vec{r}_2$	-	Vector from $\vec{b}$ to $\vec{r}_0$
$S$	-	Sensitivity
$A_2$	-	Relation of $\vec{H}$ to $\vec{S}$
$E_3$	-	Identity matrix
$c$	-	Physical environment constant
$\vec{p}_{Best}$	-	Local best position
$\vec{p}_{GlobalBest}$	-	Global best position
$f_{Best}$	-	Local best function
$f_{GlobalBest}$	-	Global best function
$\vec{v}$	-	Velocity vector

$\vec{p}_{Current,i}$	-	Current position
$\vec{p}_{Current,i+1}$	-	Position of next iteration
$\vec{r}_{Cognitive}$	-	Entry vector
$\vec{r}_{Social}$	-	Entry vector
$w_{Inertia}$	-	Previous iteration weighting factor
$w_{Cognitive}$	-	Next iteration weighting factor
$w_{Social}$	-	Current iteration weighting factor
$nBest(i)$	-	Neighbor best position
$\theta_s$	-	Angle between segmented lines
$d$	-	Diameter
$\vec{r}_c$	-	Position vector of coil
$\vec{r}_v$	-	$\vec{r}_c - \vec{r}_0$

## **CHAPTER 1**

### **INTRODUCTION**

#### **1.1 Background of study**

Nanotechnology or nanotech is a technology which manipulates the matter on an atomic, molecular and supramolecular scale. It expresses the billionth part of unit, which a nanometer is the  $10^{-9}$  –th part of a meter. Nanotechnology is defined by its abilities to manipulate the matter with dimension sized from 1 nm to 100 nm and comprises the development of materials within this range of sizes. The functionality in a smaller space allowed the application of this technology across other science fields, such as chemistry, biology, physics, materials science, and engineering.

The concepts of nanotechnology were first discussed by Richard Feynman, a renowned physicist in 1959. Feynman described the possibility of synthesis via direct manipulation of atoms in his talk “There’s Plenty of Room at the Bottom” [1]. This idea then inspired Eric Drexler, which independently used the term “nanotechnology” in his book “Engines of Creation: The Coming Era of Nanotechnology”. In his book he proposed that the idea of a nanoscale “assembler” which would be able to build a copy of it and of other items of arbitrary complexity with atomic control [2]. At the same time, Gerd Binnig and Heinrich Rohrer at IBM Zurich Research Laboratory

invented the Scanning Tunneling Microscope (STM), which provided unprecedented visualization of individual atoms and bonds. This technology successfully used by the researchers to manipulate individual atoms. Unfortunately, STM has some limitations such as only works for conducting materials [3]. However, these limitations were then eliminated by the invention of Atomic Force Microscope (AFM) [4]. In the early 2000s, the field garnered increased scientific, political, and commercial attention that to both controversy and progress. The definitions and potential implications of nanotechnologies were questioned in the report of Royal Society. Challenges were raised regarding the feasibility of applications envisioned by advocates of molecular nanotechnology [5].

The great achievement in nanotechnologies had led a growth in medical field. The development of a wide spectrum of nanoscale technologies is the key to change the foundation of pathologies diagnosis, treatment and prevention. National Institutes of Health (Bethesda, MD, USA) referred these technologies as nanomedicines. Nanomedicines have the ability to transform molecular discoveries arising from genomics and proteomics into widespread advantage for patients. The subject area of nanomedicine is large and includes nanoparticles, biological mimetics (e.g., functionalized carbon nanotubes), “nanomachines” (made from interchangeable DNA parts and DNA scaffolds), nanofibres and polymeric-nanoconstructs (molecular self-assembly peptides for tissue engineering) nanoscale microfabrication-based devices (silicon microchips), sensor and laboratory diagnostics. Besides, there is a huge interest of studying the capability of nanoscale technologies in cells targeting in the body for drugs, genetic materials and diagnostic agents delivery [6]. Therefore, study into the biocompatible delivery and targeting of pharmaceutical, therapeutic, and diagnostic agents through intravenous and interstitial routes of administration with nanosized particles is at the forefront of concerns in nanomedicine.

The discovery of nanoparticles provided wide possibilities of application in nanomedicine. Gold nanoparticles have been used as quenchers in fluorescence resonance energy transfer measurement studies. The unique behavior of gold



nanoparticles in the distance-dependent optical property has enabled the evaluation of binding of DNA-conjugated gold nanoparticles to a complementary RNA sequence [7]. The wide use of iron oxide cored nanocrystals with superparamagnetic properties as the contrast agents in magnetic resonance imaging (MRI) is another evidence of rising of nanotechnologies in medicines.

Magnetic Nanoparticles Imaging (MNI) is a tomographic imaging method which uses nanoparticles as the contrast agent to measure the magnetic field. This concept was proposed by Gleich and Weizenecker in 2005 as a novel imaging modality [8]. They suggested that ferromagnetic nanoparticles have the potential to provide quantitative three-dimensional real-time imaging with high sensitivity and spatial resolution, based on the non-linear magnetization and saturation behavior of ferromagnetic materials. Therefore, this method shows a high potential as an imaging modality for biodistribution of magnetic nanoparticles. However, only the setups with small sample volumes have been designed and presented up to now. A large fields will be required if it is designed for human. Additionally, scaling and realization of clinical scanners requires a vast amount of work and future developments. The single-sided of MNI device shows the results of considerable decrease image quality [9]. Similar to MRI, MNI does not allow for binding specific detection with the current technology.

## **1.2 Problem Statement**

The reconstruction results from previous finding show that there are a lot of unsure elements in either setups or configurations of the imaging methods. The results of reconstruction either by homogeneous excitation field or inhomogeneous field do not provide promising results. This imperfection has triggered the studies of simulation configurations and reconstruction methods in order to obtain an optimum result. Previous works on optimization of currents flow through the excitation coils

contributed in enhancing the reconstructed image qualities [10]. By measuring the spatial sensitivities of each voxel hence optimize the currents provided better results of reconstruction. This proved that by altering the simulation configurations, the results of reconstruction may differ as well. In other similar imaging techniques like magnetocardiography [11] and focal magnetic stimulation [12], the sensors position and the effects of coils were studied under different conditions. Thus, the studies on these parameters are very important in MNI in order to create the best results. In this thesis, the focus on the effects of coils are emphasized and studied with different configurations.

### 1.3 Objective

This thesis discusses the optimization of coil diameters in magnetic nanoparticles imaging. The application of magnetic nanoparticles is based on the magnetorelaxometry which the magnetic field is generated by the magnetic coils and highly influenced by the diameters of the coil. In order to provide the promising results, the diameter of the magnetic coil is one of the important parameters in image reconstruction. In this thesis, an optimization method based on particle swarm optimization has been introduced. The main objectives of the related works are:

- To investigate the effects of the excitation coils configuration on the reconstructed results.
- To examine the possibility of coils diameters optimization with particle swarm optimization method.

## **1.4 Scope**

The studies in this thesis are focused on the measurement of magnetorelaxometry of magnetic nanoparticles and reconstruction images of the samples. The configurations of the excitation coils are studied by varying the number of coils, diameter of coils, arrangement of coils, shape of coils and the effects of the offset value of truncated singular value decomposition. The results are then compared with the correlation coefficient of the reconstruction with the computed data. Besides, in order to examine the possibility of optimization by using particle swarm optimization technique, the algorithm development is focused on the magnetic field calculation and the position vector determination.

## **1.5 Signification of Study**

The outcomes of this study will contribute to justify the effects of varying the excitation coils' configurations in magnetic nanoparticles imaging. Other than that, the outcomes will help to create an optimum configuration to obtain the best result. The exposure of excessive of magnetic field to the human will be harmful to human. Hence, the study to obtain an optimum setup for magnetic nanoparticles imaging are very important in order to reduce the side effects of the device before applying on human.