

THE COMPARISON OF IMAGE MANIFOLD METHOD  
AND VOLUME ESTIMATION METHOD  
IN CONSTRUCTING 3D BRAIN TUMOR IMAGE

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*To my beloved family and the person who loves me,*

*Thanks for your love and support...*

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## **ABSTRACT**

Three dimensional (3D) image visualization is one of the important processes that extract information from the given two dimensional (2D) images. This study deals with the 3D object visualization via 2D images that included difference surfaces. The main objective of this work is to combine the contour of the brain tumor in 2D Magnetic Resonance Imaging (MRI) slices and reconstruct the 3D object. The fundamental research is based on the Alternating Operating Splitting and Geodesic Active Contour methods where these methods are used to detect the contour on a brain tumor MRI image. To combine these contours, we will apply Image Manifold method by using 3D Slicer Software and to calculate the volume of the 3D image, we will apply Volume Estimation method by using MATLAB. The objective of this study is to investigate the performance evaluation of some numerical methods for constructing 3D image and estimating the volume of the image. The obtained results indicate a good resolution of the reconstruction 3D image visualization process.

## ABSTRAK

Visualisasi tiga dimensi (3D) imej adalah salah satu proses penting bagi mendapatkan maklumat daripada dua dimensi (2D) imej. Tujuan penyelidikan ini adalah untuk menghasilkan objek 3D melalui imej 2D yang terdiri daripada pelbagai permukaan yang berbeza. Objektif utama kajian ini adalah untuk menggabungkan kontur tumor otak dalam bentuk 2D Pengimejan Resonans Magnet (MRI) dan membina objek 3D. Penyelidikan asas adalah berdasarkan kaedah Pemisahan Pembekal Semi-implisit dan Kontur Aktif Geodesic di mana kaedah ini digunakan untuk mengesan kontur pada imej MRI tumor otak. Untuk menggabungkan kontur ini, kami akan mengaplikasi gabungan imej dengan menggunakan Perisian 3D Slicer dan untuk mengira jumlah isipadu imej 3D, kami akan mangaplikasi kaedah penganggaran isipadu dengan menggunakan MATLAB. Objektif projek ini adalah untuk membandingkan prestasi beberapa kaedah berangka bagi membina imej 3D dan menganggarkan jumlah isipadu imej. Keputusan yang diperolehi dapat menunjukkan resolusi yang baik dalam proses pembinaan imej 3D.

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## **LIST OF ABBREVIATIONS**

2D	-	Two dimensional
3D	-	Three dimensional
ACM	-	Active Contour Method
AOS	-	Additive Operator Splitting
IBVP	-	Initial Boundary Value Problem
IM	-	Image Manifold
GAC	-	Geodesic Active Contour
LSE	-	Linear System of Equation
VE	-	Volume Estimation

## LIST OF SYMBOLS

$\beta$	Weighted of energy
$\nabla$	Gradient operator
$\Omega$	Image domain
$\rho$	Acceleration parameter
$g$	Stopping function
$\nu$	Positive constant
$\tau$	Time
$k$	Number of iterations
$D$	The distance function
$\alpha$	The initial scaling factor
$\Delta s$	The smoothing parameter
$\phi(x, y, z)$	Distance function
$V_g$	Volume of manifold
$I_\sigma$	Initial image
$g(x, y, z)$	Edge indicator
$K_\phi$	Curvature operator

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## CHAPTER 1

### INTRODUCTION

#### 1.1 Introduction

A brain tumor is a growth of abnormal cells and normal cells in an inappropriate place in the brain. Clinically, magnetic resonance imaging (MRI) is widely used for brain tumor detection. MRI is a medical imaging technique and used in radiology to investigate the anatomy and function of the body in both health and disease. MRI scanners use a strong magnetic fields and radio waves to form images of the body in two dimensional images (2D).

Based on the segmentation of 2D brain tumor images, early *diagnosis* and *treatment of brain tumor* become *inaccurate prediction*. *It is because 2D images do not present the overall natural tumor images in 3D visualization*. *In this project, we will prove that the 2D MRI images can be used to construct 3D image by using two different methods*. Visualisation of 3D image will gives significant information of the tumour growth, feature and property. The function of image visualization is very important for diagnosis and treatments process. The significant potential of 3D visualization remains undiscovered and undeveloped completely. Thus, 3D



visualisation becomes an important area of researcher to provide a new tool, devices, procedures, propose an accurate diagnosis and recommends a treatments strategy.

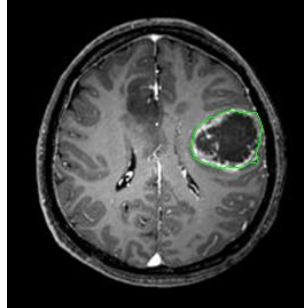
This project will propose two different numerical methods of 3D image construction. The methods are Image Manifold (IM) and Volume Estimation (VE). IM method describes an approach of 3D model reconstruction from 2D MRI image. The construction will be from three points of view; front view, side view and top view of 2D MRI images. All of these can be done using 3D Slicer software. VE method is an automatic procedure of calculation region of brain tumor in 2D MRI images and this method was proposed by K. Krechetova *et al*, 2008. In this project, we will use the VE method to construct 3D images by using a few 2D MRI images which is from the various size of brain tumor images visualization. IM and VE methods will provide the practical improvements to the reliability of medical diagnosis process by constructing the 3D visualization of brain tumor.

## **1.2 Background of the Problem**

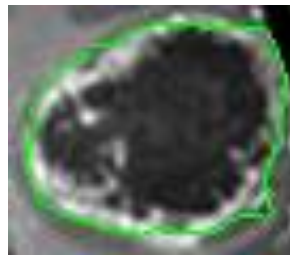
One of the problems in constructing 3D image is we need to join the contour of 2D MRI images. In order to get the contour of 2D images, we need to apply the result from previous study in Active Contour Model.

From the previous study, Rosdiana Shahril, 2010, has introduced GAC model based on Additive Operator Splitting (AOS). AOS scheme is used to detect the edges of brain tumor on 2D MRI images. Gauss Seidel method is used as a numerical solution of the matrix system and the numerical result obtained were in terms of time execution, number of iterations, root mean square error, accuracy, rate of convergence, and computational cost.

The result obtained was the edge detection on brain tumor 2D MRI images. The figures below show the result of edge detection from the previous study.



**Figure 1.1 :** 2D MRI brain image with edge detection



**Figure 1.2 :** Enlargement of the edge detection from Figure 1.1

Figure 1.1 shows 2D MRI brain image with edge detection and Figure 1.2 shows the selected area of brain tumor image obtained by the previous study. In this work, we will extend this result from 2D MRI brain tumor images to 3D visualization by implementing IM and VE methods.

### **1.3 Statement of the Problem**

This study is to investigate the enhancement of 2D brain tumor image (MRI) based on GAC and AOS methodology. The enhancement process from 2D to 3D image visualization will be obtained by implementing IM and VE methods. The study will focus on the performance comparison between IM and VE methods to visual 3D brain tumor images in terms of volume calculation and the quality of 3D visualization quality.

### **1.4 Objective of the Research**

The objectives of this study are:

- i. To apply the edge detection method of 2D MRI brain tumor image based on AOS technique in constructing 3D image.
- ii. To construct high resolution of the 3D images using IM and VE methods based on (i).
- iii. To implement (ii) using 3D Slicer Software and MATLAB version R2011.
- iv. To analyse the numerical performance in (iii) using the comparison of volume calculation between IM and VE methods.

## **1.5 Scope of the Research**

The scope of research will focus on constructing 3D brain tumor image and calculating the volume of the brain tumor by using IM and VE methods. The solution for IM method can be done by using 3D Slicer software while VE method can be done in MATLAB version R2011a. The application of AOS modelling in detecting the contour of 2D MRI image for both IM and VE methods will be considered. This experiment will be applied to real MRI brain tumor images of a patient from Hospital Kubang Kerian, Kelantan.

### **1.5.1 The Chart of the Research Scope**

The Figure 1.3 shows the flow chart of research scope. The research scope is based on the rounded rectangles with the yellow colour. This project will be started on detecting the edges of brain tumor by integrating GAC model and AOS scheme. This experiment will be applied to brain tumor on the real 2D MRI images of a patient from Hospital Kubang Kerian, Kelantan. The digital results of edge detection in 2D images will be used to construct the 3D brain tumor images by using IM and VE methods. The algorithm will be run on MatlabR2011a and 3D Slicer software. Finally, the performance comparison between IM and VE methods will provide the alternative method to visualize high resolution of 3D brain tumor images. The performance evaluation will be focused on the expected volume size and visualization quality.

## **1.6 Significance of Study**

This project expecting a successful application of GAC and AOS strategies to obtain the edge detection of 2D images. The selected contour line of 2D MRI brain tumor images will be used to construct the 3D image by applying the IM and VE methods. Based on the comparison of numerical performance of IM and VE methods, the significance of the project will assume that IM is better than VE in terms of visualization. Finally, the result of this project is significance to enhance the medical images to *3D visualization of medical imaging* since the methods have an interesting application in reconstructing a high resolution of 3D medical images.

## **1.7 Thesis Organization**

This thesis consists of six chapters. Chapter 1 describes the introduction of AOS model. In this chapter, we presented the result from previous study, introducing IM and VE methods under consideration, objectives, scope, and significance of the research.

Chapter 2 focuses on the literature review of previous studies related to constructing 3D images and also IM and VE methods. We also describe the use and application of GAC method and AOS scheme in constructing 3D image.

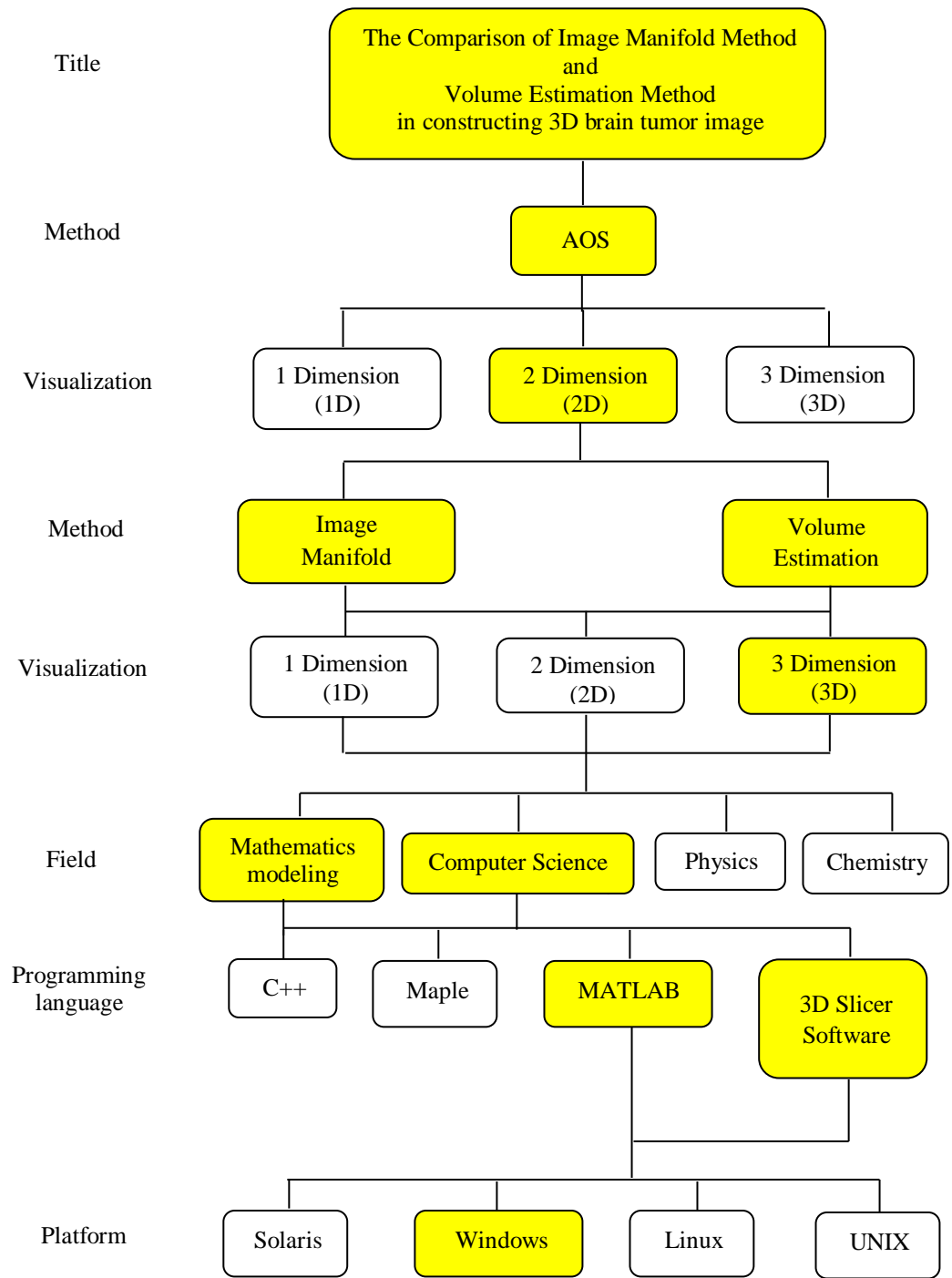
In Chapter 3, we will discuss the methodology for GAC-AOS scheme and also IM and VE method.

In Chapter 4, we will describe the implementation of IM method in constructing 3D image based on the edge detection of 2D brain tumor MRI images. We will perform this method by using 3D Slicer software.

In Chapter 5, we will describe the implementation of VE method to join the 2D images and calculate the volume of the 3D image. We will perform this method in Matlab programming.

In Chapter 6, we will analyse the results based on the expected volume calculation obtained by both methods. We will also make a comparison of the performance between the two methods. In this chapter, we also state the conclusions of this research based on the results that are shown in Chapter 4 and Chapter 5 and relate them with our objectives in Chapter 1.

In Chapter 7, we summarize the whole work and provide some suggestions and recommendations for the future researchers.



**Figure 1.3:** The chart of research scope in constructing 3D brain tumor image.

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