### DENSITY FUNCTIONAL THEORY INVESTIGATIONS OF STRUCTURAL, ELECTRONIC AND OPTICAL PROPERTIES OF III ARSENIDES

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### DENSITY FUNCTIONAL THEORY INVESTIGATIONS OF STRUCTURAL, ELECTRONIC AND OPTICAL PROPERTIES OF III ARSENIDES

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A thesis submitted in fulfilment of the requirements for the award of the degree of Master of Science (Physics)

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A thesis submitted in fulfilment of the requirements for the award of the degree of Master of Science (Physics) I specially dedicate this thesis to my beloved parents and my siblings for their continuing support along the way. Without them none of my success would be possible

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#### ABSTRACT

III arsenide semiconductor materials have attracted considerable attention because of their unique characteristics and unfailing applications as base materials in optoelectronics and many other state of the art technologies. In this study, III arsenide investigations are presented by performing calculations using computational approach framed within the density functional theory. Exchange-correlation energy functional plays a crucial role in the efficiency of density functional theory calculations, more soundly in the calculation of fundamental electronic energy band gap. In this density functional-theory study of III arsenide, the implications of exchange-correlation energy functional and corresponding potential were investigated on the structural, electronic and optical properties of III arsenides. For gradient structural properties, local density approximation, generalized approximation and parameterized generalized gradient approximation were applied. For the calculations of electronic properties, recently developed Tran-Blaha modified Becke-Johnson potential has been implemented additionally. To execute this study, state of the art computational code WIEN2k, based on full potential linearized augmented plane-wave and local orbitals methodology, was applied. III arsenide were simulated to obtain their lattice constant, band gap, dielectric constant, reflectivity, absorption, refraction index and the energy loss values. The results point to parameterized generalized gradient approximation as a more appropriate approximation for the calculations of structural parameters. However, the electronic band structure calculations at the level of modified Becke-Johnson potential showed considerable improvements over the other exchange correlation functionals. Besides this, the reported results related to optical properties within modified Becke-Johnson potential show a good agreement with the experimental measurements in addition to other theoretically results.

#### ABSTRAK

Bahan semikonduktor III arsenida telah berjaya menarik perhatian yang meluas kerana cirinya yang unik dan kejayaan penggunaannya sebagai bahan asas dalam optoelektronik dan teknologi moden yang lain. Dalam kajian ini, penyelidikan III arsenida dijalankan dengan melakukan pengiraan menggunakan pendekatan pengkomputeran berdasarkan pendekatan teori fungsi ketumpatan. Fungsi bagi tenaga pertukaran korelasi memainkan peranan yang penting dalam ketepatan pengiraan fungsi teori ketumpatan, terutamanya dalam pengiraan asas jurang jalur tenaga elektronik. Dalam teori fungsi ketumpatan kajian III arsenida, implikasi hubungan antara fungsi bagi tenaga pertukaran korelasi dan keupayaan yang sepadan terhadap ciri struktur, elektronik dan optik dalam III arsenida telah diselidiki. Bagi sifat struktur, penghampiran kepadatan tempatan, penghampiran kecerunan teritlak dan penghampiran kecerunan teritlak berparameter telah digunakan. Bagi pengiraan sifat elektronik, keupayaan Becke-Johnson terubahsuai Tran Blaha yang dibangunkan baru-baru ini telah diguna pakai sebagai pelaksana tambahan dalam penyelidikan ini. Untuk melaksanakan kajian ini, kod pengiraan termaju WIEN2k berdasarkan keupayaan penuh dengan satah gelombang lelurus berserta kaedah orbital tempatan, telah digunakan. Simulasi ke atas kumpulan III arsenida telah dilakukan bagi mendapatkan nilai pemalar kekisi, jalur tenaga, pemalar dielektrik, pantulan, penyerapan, indeks biasan dan nilai tenaga yang hilang. Keputusan mendapati penghampiran kecerunan teritlak berparameter adalah pendekatan yang lebih sesuai untuk pengiraan parameter struktur. Walau bagaimanapun pengiraan struktur bagi tenaga elektronik di peringkat Becke-Johnson terubahsuai menunjukkan potensi kemajuan yang agak besar berbanding fungsi-fungsi korelasi pertukaran yang lain. Selain itu laporan keputusan bagi ciri optik dengan menggunakan keupayaan Becke-Johnson terubahsuai menunjukkan keputusan yang memuaskan hasil perbandingan antara nilai eksperimen dengan nilai kiraan teori yang lain.

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# LIST OF ABBREVIATIONS

DFT	Density Functional Theory
Ga	Gallium
В	Boron
In	Indium
Al	Aluminium
As	Arsenide
сс	Centered cubic
HF	Hartree-Fock
НК	Hohenberg Kohn
LDA	Local-density approximation
GGA	Generalized gradient approximation
BO	Born Oppenheimer
KS	Kohn Sham
FP-LAPW	Full Potential Linearized Augmented Plane Wave
mBJ	Modified Becke-Johnson
МТ	Muffin Tin
IR	Interstitial Region
XC	Exchange Correlation
OEP	Optimize Effective Potential

### LIST OF SYMBOLS

Ε	Energy (J)
$E_F$	Fermi Energy
Eg	Energy gap
ħ	Planck's constant
h	Dirac constant
Н	Hamiltonian
F	Force
Ψ	Eigen Value
$T_n$	Kinetic energy operator of nuclei
$T_e$	Kinetic energy operator of electron
Ven	Coulomb electron-nuclear attraction
V <sub>nn</sub>	Nuclear-nuclear repulsion
$n(\overrightarrow{r)}$	Electron density
$\nabla$	Laplacian Operator
т	Mass
е	Electron
R	Radius
Ζ	Nuclei
t	Time
V	Frequency
$E_{xc}$	Exchange correlation energy
V <sub>ext</sub>	External potential

Hartree (electron-electron interaction) energy
Density
Radius
Wave function
Potential Energy
No. of electron
Ground state density
Density functional
Single-particle wave functions
Energy
Exchange and correlation energy per particle of a uniform electron gas of density.
Electron affinity
Becke-Roussel (BR) exchange potential
Volume of unit cell
Spherical Harmonics
Vector in Brillouin zone
Reciprocal lattice vector
Solution of radial Schrodinger equation for atom
Azimuthal quantum number l
Hohenberg-Kohn functional
Muffin tin Radii
Maximun Kinetic Energy
Maximum Potential Energy

#### **CHAPTER 1**

#### **INTRODUCTION**

#### 1.1 Background

III arsenides compound semiconductors play an important role in established commercial technologies especially in electronic, microelectronics and optoelectronic devices, such as lasers, modulators, light emitting diodes, photovoltaic cells, photo detectors, filters, and also in new technological applications. All these devices, based on III arsenide semiconductors, are showing appreciable efficiency and demonstrating multi benefits in different applications. Although each compound of III-V exhibits important properties, III arsenides (a family of III-V conventional semiconductors) cover the widest range of energy gaps. These materials almost cover the whole visible spectrum from red to violet light. This feature has made III arsenide materials, a potential candidate for many advanced technologies specifically for optoelectronic systems and devices. At ambient temperature and pressure, III arsenides have been recognized to be stable in their zinc blende (ZB) structure. Reported in available experimental and theoretical studies, Boron Arsenide (BAs) and Aluminium Arsenide (AlAs) have the indirect band gap structure, whereas Gallium Arsenide (GaAs) and Indium Arsenide (InAs) are of direct nature. On account of their peculiar nature of physical properties and substantial applications in commercial technologies, in particular, electronic and optoelectronic devices, III arsenides are widely explored.

The rapid advancements in the field of information technology and device applications demands a dire need to further investigations related to this class of materials to exploit their hidden potential for future applications. Investigations of the physical properties of materials at atomic scale and their exploitation are very important and challenging. Fundamental understanding of the physical properties at atomic scale requires the application of quantum mechanics but to explore the properties of materials at atomic scale is a time taken and a complicated problem. To overcome this difficulty, first principles based computational approaches are considered to be more reliable tool because of their ability to explore the physical properties of materials with high accuracy in short time and reduced cost in comparison with experimental study.

These charming features of computer simulation motivated us to do investigation of some fundamental properties for III arsenides by using density functional theory (DFT) [1, 2] based method of calculations. It is because, among III arsenides compound family, BAs, AlAs, GaAs and InAs are the most significant due to their potential applications in semiconductor industry. Also the structural and electronic properties of these materials are of considerable importance in both fundamental and applied physics, and extensive research is going on at both levels (experimentally and theoretically) due to their potential applications in electronic/optoelectronic devices [3-34].

#### **1.2 Problem Statement**

To study the structural, electronic and optical properties of the materials, it is important to understand their features. To take insight view of these properties theoretically, a systematic solution of Schrodinger many body equation is crucial. The solution of the Schrodinger much body equation analytically is too difficult. However DFT based computational approaches provide a way out to simplify such kind of complex problem by transferring the many body equation into one particle independent Kohn-Sham equations. Though the investigations regarding structural, electronic, and optical properties of III arsenides have been discussed in a number of studies, there is still problem in doing calculation accurately comparable to the experimental value specifically electronic properties within standard DFT. To address this crucial problem of DFT, different exchange correlation (XC) functionals have been implemented in this study to investigate III arsenides structural, electronic and optical properties. The calculations of lattice parameters, bulk moduli, electronic band structure, energy band gap along with optical parameters is presented comprehensively.

In this research, LDA, PBE-GGA, and WC-GGA exchange-correlation functional are employed within DFT to deal with structural parameters. For the electronic properties, modified Becke-Johnson (mBJ) exchange potential incorporated into standard LDA and GGA is additionally applied. Furthermore, the obtained results in this research work with different approximations are compared with the previously reported experimental and theoretical works.

#### 1.3 Objectives

The main interest of this research is to understand and apply state of the art of full potential linearized augmented plane-wave plus local orbitals FP-L(APW+lo) approach to perform a study on the structural, electronic and optical properties of III arsenides (BAs, AlAs, GaAs and InAs).

The objectives of this study are as follows:

 To investigate the structural, electronic and optical properties of III arsenides (BAs, AlAs, GaAs and InAs) in their zinc blende (ZB) phase.

- 2. To study the impact of different approximations on the structural, electronic and optical properties and to find out which approximation provides better choice for reliable results in comparison to experimental values.
- To investigate the effectiveness of FP-LAPW approach using WIEN2k code on the properties of III arsenides.

### 1.4 Scope of Study

A right knowledge of the physical properties of III arsenides compounds is crucial for their prospect applications. This study may be a good addition in the body of knowledge concerning different properties of III arsenides materials and their suitability in present and future applications as well performed within different exchange correlation functional. In this research work, the ZB structures of III arsenides were simulated using experimental values of lattice parameters. For the investigations of physical properties of these materials, DFT based FP-L(APW+lo) methodology is employed. To realize these properties, computations are carried out taking into account relativistic effect within scalar relativistic approximation. To determine structural properties, the exchange–correlation energy of electrons as depicted in LDA, PBE-GGA and WC-GGA is used. For band structure calculations, in addition to LDA and GGA, the modified Becke-Johnson (mBJ) exchange potential is also used that allows the reproduction of band gaps values with accuracy similar to very expensive GW calculations. Furthermore in this study, for optical properties, we use mBJ+LDA and mBJ+GGA. From here we can see the suitability of each approach in calculating the properties of III arsenides. In short;

- 1. III arsenides are studied in their zinc blende phase structures
- Lattice constants, bulk modulus and its pressure derivative, and total energy for each compound of III arsenides are studied for the structural properties.

- 3. Band structure and band gap energy are studied for the electronic properties.
- 4. The dielectric function, absorption, reflectivity, refractive index and energy loss are studied for their optical properties.
- 5. Density functional theory is used to calculate and simulate the structural, electronic and optical properties of III arsenides.

#### 1.5 Significance of Study

The efficiency of a device not only depends on the quality of its engineering, it also requires clear knowledge about the physical properties of the base material, and the understanding of fundamental science behind their characteristics. It is therefore very important to know the different properties of the III arsenides to expose their further potential. The findings of this study related to the structural, electronic and optical properties of III arsenides compounds using different approaches of exchange correlation functional will also be useful to design new materials as well as to investigate the properties of known materials for academicians and industrial researchers. Also our findings related to III arsenides lattice parameters, band gap values, band structure, bulk moduli and optical parameters will play important role to widen further spectrum of the III arsenides applications and to determine the effective usage of these materials in the semiconductor devices. By calculating these properties, we can obtain the informations of these materials. The study of these properties also may be helpful in the specifications needed for its quality control for the material's production in different applications. Besides that, this computational calculation enables the system to be investigated where experiments are very expensive which is difficult or even impossible to perform.

#### 1.6 Previous Studies

III-V semiconductors are essential for their unfailing applications as base materials for device fabrications in current and future electronic, microelectronic and optoelectronic industries. Among these, III arsenides are of particular interest for their unique physical properties like wide band gaps, low density, high thermal conductivities, and dielectric constants [30]. At ambient temperature and pressure, III arsenides have been recognized in zinc blende (ZB) stable structure. Their fundamental band gap both experimentally and theoretically is reported indirect for BAs and AlAs and direct for GaAs and InAs. Also III arsenides almost covers whole visible spectrum from red to violet light. These properties have made this class of materials potential candidate for light emitting diodes, lasers, photo detectors, integrated circuits, modulators, filters, and many more other advanced technologies. On account of their peculiar nature of physical properties, and substantial applications in commercial technologies specifically in electronic and optoelectronic devices, III arsenides are widely explored [3-34]

Each member of this group demonstrates unique electronic structure and corresponding physical properties. BAs exhibit strong covalent nature [27], and have analogous electronic nature to silicon that led it unique among the other III compounds [28]. Being a wide band gap semiconductor BAs is considered a suitable partner for alloying with GaAs and AlAs [29]. However because of difficult synthesis of BAs its properties are under debate [36]. Similarly GaAs, owing to direct wide band gap and having small effective mass of electrons, besides many other applications, is exploited as ultra fast transistors especially where reliability is the main point. Likewise, InAs and AlAs play fundamental role as a part of many optoelectronic heterojunction devices require a fully understanding of the properties of materials, and the fundamental science behind these properties on its material engineering and also at practical level. Because of technological importance, clear understanding about physical properties and their science is very essential. Therefore experimental and theoretical investigations are of fundamental interest.

Theoretically, most of the studies are performed using first principles approaches: Chimot et al. [98] have studied structural and electronic properties of BAs, GaAs, InAs and there alloys within the DFT framework of virtual crystal approximation. They have recommended III arsenides materials and their alloys as an alternative to the InP substrate, for the epitaxial growth of nanostructures to fabricate field effect transistors, lasers and storable absorbers in the field of optoelectronics. Zaoui et al. [37] and A. Boudjemline et al. [38] have reported the electronic and optical properties of BAs using LDA and GGA within DFT. Using a FP-LAPW method Arabi et al. [25] have studied structural and electronic structure of GaAs in four different phases. Ahmed et al. [4] have also investigated structural and electronic properties of III arsenides using LDA, GGA and GGA proposed by Engel-Vosko (EV). Amrani et al. [39] have studied the structural parameters, electronic and optical properties and variation in it under higher pressure using FP-LAPW method using LDA as an XC potential. Ground state and high pressure structural parameters were also investigated by Wang et al. [40] using full potential linearized muffin-tin orbital (FP-LMTO) scheme at the level of GGA within the frame work of DFT. Similarly Hart et al. [29] have investigated ground state as well as electronic properties of BAs, AlAs, InAs and GaAs within DFT using LDA approximation. Most recently Guemou et al. [41] have studied the structural and electronic properties and optical properties of BAs, GaAs and their alloys using LDA and GGA. Although a sizeable number of theoretically investigations have been reported in literature previously using different forms of exchange correlation functional, mostly reproduce underestimated values of fundamental band gap values especially in case of semiconductors and insulators and corresponding optical properties.

Right knowledge of fundamental and optical band gap is important in the study of physical properties of materials as it play decisive role for their applications as a base material in electronics and optoelectronics devices, to exploit their potential for further applications. Though DFT based on computer simulation have made it possible nowadays to investigate electronic band structure at atomic scale and the corresponding fundamental properties of materials in amazingly short time with low cost, and have predicted the properties of materials that yet not synthesized, reproduction of accurate electronic band gap within conventional DFT is not straightforward. It is because DFT is basically designed to cope up ground state properties, however to overcome this difficulty a proper choice of XC potential functional is crucial to reproduce electronic band gap and optical properties comparable to experimental measurements. One of them is the Tran- Blaha (TB) modified Becke Johnson (mBJ) XC potential, which has been reported in several studies of semiconductors and insulators to calculate energy gap with high accuracy or near to the experimental value. The highly accurate results at effectively low cost have proclaimed mBJ as superior on other approaches.

Motivated by fascinating features of DFT computer simulations, the important applications of III arsenides in cutting edge technologies and balance role of mBJ+LDA exchange and correlation potential to reproduce band gap for semiconductors and insulators, we investigate some of fundamental properties of III arsenides using FP-L(APW+lo) framed within DFT [2,42]. However to investigate the response of XC-potential to band gap calculation we employ mBJ+LDA in addition to LDA, PBE-GGA and WC-GGA. Calculations are also performed related to optical properties.

#### 1.7 III-V Semiconductors

III-V semiconductors are formed by chemical elements from group III and V with every atom group of III is bound to four atoms of group V atoms and every group of V atom is bound to four atoms of group III atoms in the crystal structure of III semiconductors. These III semiconductors are able to build binary, ternary, quaternary and also higher-order compound to provide extensive potential for engineering of the semiconductor band gap and the related emission or absorption wavelength which are vital properties for optoelectronic and microelectronic applications.

#### 1.8 Modeling and Simulation

A set of mathematical equations or physical model is used in modeling technique in order to clarify it as a real system. By changing its variables, according to their behavior and performance of the system, prediction can be made. Computer simulation helps to see how the system works on the models and therefore a study on the models can be made. Computational science has become a vital tool in modeling and simulation. Modeling and simulation are usually achieved by the aid of computational science and therefore they are always referred to computer modeling and computer simulation. Computational science could be defined as an interdisciplinary approach that uses concepts and skills from the science, computer science and mathematics disciplines to solve complex problems in the study of various phenomena which can be illustrated by Fig. 1.1.



**Figure 1.1:** Computational science is defined as the intersection of the three disciplines, i.e. computer science, mathematics and applied science.

#### REFERENCES

- W. Kohn, L. J. Sham, Self-Consistent Equations Including Exchange and Correlation Effects, Phys. Rev. 140, A1133 (1965).
- Blaha P, Schwarz K, Madsen G K H, Kvasnicka D, Luitz J WIEN2K, an augmented planewave + local orbitals program for calculating crystal properties, Techn. Universitat, Vienna, Austria, 2001.
- T. P. Pearsall, in: R.K. Willardson, A.C. Beer (Eds.), Strained-Layer Super-Lattices: Materials Science and Technology, Semiconductors and Semimetals, vol. 33, Academic Press, Boston, 1991.
- R. Ahmed, S. J. Hashmifar, H. Akbarzadeh, M. Ahmed, F. Aleem, Ab initio study of structural and electronic properties of III-arsenide binary compounds. Comput. Mater. Sci., **39** (2007) 580.
- E. Kasper, F. Schaffler, in: R.K. Willardson, A.C. Beer (Eds.), Strained-Layer Super-Lattices: Materials Science and Technology, Semiconductors and Semimetals, vol. 33, Academic Press, Boston, (1991) 223.
- G. Grosso, C. Piermarocchi, Tight-binding model and interaction scaling laws for silicon and germanium, Phys. Rev. B 51 (1995) 16772.
- 7. R.W.G. Wyckoff, Crystal Structures, second ed., Krieger, Malabar, 1986.
- B. Fillipi, D.J. Singh, C.J. Umrigar, All-electron local-density and generalizedgradient calculations of the structural properties of semiconductors Phys. Rev. B 50 (1994) 14947.
- 9. S. Q. Wang, H.Q. Ye, A plane-wave pseudopotential study on III zinc-blende and wurtzite semiconductors under pressure, J. Phys.: Condens. Matter 14 (2002) 9579.

- P. Philip, Rushton, Stewart J. Clark, David J. Tozer, Density-functional calculations of semiconductor properties using a semiempirical exchange-correlation functional, Phys. Rev. B 63 (2001) 115206.
- B. I. Min, S. Massidda, A.J. Freeman, Structural and Electronic Properties of Bulk GaAs, AlAs, and the (GaAs)<sub>1</sub>(AlAs)<sub>1</sub> Superlattice, Phys. Rev. B 38 (1988) 970.
- B. K. Agrawal, P.S. Yadav, Sudhir Kumar, S. Agrawal, First principle calculation of Ga-based System, Phys. Rev. B 52 (1995) 4896.
- 13. S. Huai, A. Zunger, First-principles calculation of band offsets, optical bowings, and defects in CdS, CdSe, CdTe, and their alloys, Phys. Rev. B **60** (1999) 5404.
- 14. N. Viktor, Staroverov, E. Gustavo Scuseria, Jianmin Tao, John P. Perdew, Climbing the Density Functional Ladder: Non-Empirical Meta-Generalized Gradient Approximation Designed for Molecules and Solids, Phys. Rev. B 69 (2004) 075102.
- S. Kalvoda, B. Paulus, P. Fulde, H. Stoll, Influence of Electron Correlations on Ground-State Properties of III Semiconductors, Phys. Rev. B 55 (1997) 4027.
- M. Causa, R. Dovesi, C. Roetti, Pseudopotential Hartree-Fock study of seventeen III and IV-IV semiconductors, Phys. Rev. B 43 (1991) 11937.
- 17. A. Mokhatari, H. Akbarzadeh, Electronic and Structural Properties of β-Be3N2, Phyisca B 324 (2002) 305.
- C. Fillipi, D. J. Singh, C.J. Umrigar, All-electron local density and generalized gradient calculations of structural properties of semiconductors, Phys. Rev. B 50 (1994) 14947.
- 19. K. H. Hellwege, O. Madelung, L. Bornstein *New Series Group III*, vol. 17a, Springer, 1982.
- 20. S. Adachi, Material parameters of In<sub>1-x</sub>Ga<sub>x</sub>As<sub>y</sub>P<sub>1-y</sub> and related binaries J. Appl. Phys.
  53 (1982) 8775.

- 21. P. Hohenberg, and W. Kohn, Inhomogeneous electron gas, Phys. Rev. B 136 (1964) 864.
- 22. G. G. Mahan, and K. R. Subbaswamy, *Local density theory of polarizability*, 1990 New York, Plenum Press. S. Cotteiner, Density functional Theory and the Family of (L)APW-methods: a step by step introduction (2004)
- 23. M. Born, and R. Oppenheimer, On the quantum theory of molecules, *Annalen der Physik* 84 (1927) 457.
- D. R. Hatree, 1928. Mathematical Proceeding of the Cambridge Philosophical Society, 24, 89-110.
- H. Arabi, A. Pourghazi, F. Ahmadian, and Z. Nour-bakhsh, First-principles study of structural and electronic properties of different phases of GaAs Phys. B 373 (2006) 16.
- 26. R. M. Wentzcovitch, M. L. Cohen and P. K. Lam Theoretical study of BN, BP, and BAs at high pressures, Phys. Rev. B 36 (1987) 6058.
- 27. A Zaoui, E. H. Hassan Full Potential linearized augmented plane wave calculations of structural and electronic properties of BN,BP, BAs and BSb , J. Phys. Condens. Matter 13 (2001) 253.
- M. Ferhat, B. Bouhafs, A. Zaoui, H. Aourag, First-principles study of structural and electronic properties of BSb, J. Phys.: Condens.Matter 10 (1998) 7995; M. Ferhat, B. Bouhafs, A. Zaoui, H. Aourag, J. Phys.: Condens. Matter 51 (1998) 285.
- 29. G. L.W. Hart, A. Zunger, BAs and Boride III–V alloys, Phys. Rev. B 62 (2000) 13522
- 30. Y. Al Douri A.H Reshak, U. Hashim, *Optoelectronic of GaAs and AlAs under temperature effects*, Optik 124 (2013) 2128-2130.
- Y. Al Douri, H. Auurag The effect of pressure on the iconicity of In-V compounds Phy. Rev. B 324 (2012) 173:178.

- 32. Y. Al Douri, Confirmation of bulk modulus of III-V compounds under pressure effect using tight binding method. Optik vol 123 (11), 2012, pages 989-992
- 33. Y. Al-Douri, Ali Husain Reshak Calculated optical properties of GaX (X=P, As, Sb) under hydrosatatic pressure, Applied Physics A: Materials Science & Processing 104 (2011) 1159-1167.
- M. Rabah, Y. Al-Douri, M. Sehill D Rached. Pressure effect on electronic band structure of III-V compounds, *Materials Chemistry and Physics* vol 80 (2003) 34-38.
- 35. M. A. Ghebouli, H. Choutri, N. Bouarissa, B. Ghebouli Journal of Solid State Chemistry 192 (2012) 161. E. A. Chagarov and A. C. Kummel, Density Functional Theory Simulations of High-k Oxides on III Semiconductors.
- 36. A. Mujica, A. Rubio, A. Munoz, R.J. Needs, High pressure phases of group IVa, IIIa-Va, and IIb-VIa compounds, Rev. Mod. Phys 75 (3) (2003) 863.
- A. Zaoui, S. Kacimi, A. Yakoubi, B. Abbar, B. Bouhafs Optical properties of BP, BAs and BSb compounds under hydrostatic pressure, Phys. B 367 (2005) 195.
- 38. A. Boudjemline, M. M. Islam L. Louail, B. Diawara, Electronic and optical properties of BAs under pressure, Phys. B 406 (2011) 4272.
- B. Amrani, Superlattices and Microstructures, First Principles Investigation of Alas at High. Pressure," *Superlattices and Microstructures*, No. 2, 40 (2006) 65.
- H. Y. Wang, X. S. Li, C. Y. Li, K. F. Wang, First-principles study of phase transition and structural properties of AlAs, Materials Chemistry and Physics 117 (2009) 373– 376.
- 41. M. Guemou, B. Bouhafs, A. Abdiche, R. Khenata, Y.A. Douri, S. B. Omran, Firstprinciples calculations of the structural, electronic and optical properties of cubic B<sub>x</sub>Ga<sub>1-x</sub>As alloys, Physica B 407 (2012) 1292.

- 42. H. Meradji, S. Drablia, S. Ghemid, H. Belkhir, B. Bouhafs, A. Tadjer, Firstprinciples elastic constants and electronic structure of BP, BAs, and BSb, Phys. Status Solidi B 241 (2004) 2881.
- 43. Attila Szabo and Neil S.Ostlund. *Modern Quantum Chemistry: Introduction to Advance Electronic Structure Theory*. Revised Edition. US: McGraw-Hill. 2003.
- 44. M. Levy, Universal variational functionals of electron densities, first-order density matrices, and natural spin-orbitals and solution of the v-representability problem, *Proc. Natl. Acad. Sci. USA* **76**, 6062 (1979); M. Levy, Electron densities in search of Hamiltonians, *Phys. Rev. A* **26**, (1982) 1200. N.M Harrison, An Introduction to Density Functional Theory, Imperial College of Science and Technology.
- 45. L. H. Thomas. The calculation of atomic fields. Proc. *Cambrigde Philos. Soc.* 23,542(1927).
- 46. E. Fermi. Application of statistical gas methods to electronic systems. *Atti. Accad. Naz. Lincei, Cl. Sci. Fis. Mat. Nat. Rend.*. 6,602 (1927).
- 47. A. D. Becke, Density-functional exchange-energy approximation with correct asymptotic behaviour, Phys. Rev. A 38, 3098 (1988).
- 48. Y. Yang, J. P. Perdew, J. A. Cevary, L. D. Macdonald and S. H. Vosko, Exchange Potentials in Density. Functional Theory, *Phys. Rev.* A **41**, 78 (1990)
- J. P. Perdew and Y. Wang, Accurate and simple density functional for the electronic exchange energy: Generalized gradient approximation. *Phys. Rev. B* 33, 8800, (1986); Ibid. E 34, 7406, (1986). A. Foster (2000), Theoretical Modelling of Non-contact Atomic Force on Insulators. Doctor Philosophy, University College London.
- 50. J. P. Perdew, in *Electronic Structure of Solids 91*, Ed. P. Ziesche and H. Eschrig, Akademie Verlay, Berlin, (1991).
- 51. D. C. Langreth and J. P. Perdew, Theory of Non-Uniform Electronic Systems: I. Analysis of the Gradient Approximation and a Generalization that Works, Phys. Rev. B 21, 5469 (1980).
- 52. D. C. Langreth and M. J. Mehl, Beyond the Local-Density Approximation in Calculations of Ground-State Electronic Properties, Phys. Rev. B 28, 1809 (1983).

- 53. J. P. Perdew, Density-functional approximation for the correlation energy of the inhomogeneous electron gas, Phys. Rev. B **33**, 8822 (1986).
- 54. J. P. Perdew, A. Ruzsinszky, J. Tao, V. N. Staroverov, G. E. Scuseria, and G. I. Csonka, Prescription for the design and selection of density functional approximations: More constraint satisfaction with fewer fits, J. Chem. Phys. **123**, 062201 (2005)
- A. D. Becke and E. R. Johnson, A simple effective potential for exchange, J. Chem. Phys. 124, 221101 (2006)
- 56. Tran, Blaha, Schwarz, Band gap calculations with Becke–Johnson exchange potential, J. Phys. CM. 19, 196208 (2007)
- 57. A. D. Becke and M. R. Roussel, Exchange holes in inhomogeneous systems: A coordinate-space model, Phys. Rev. A **39**, 3761 (1989)
- 58. R. T. Sharp and G. K. Horton, A Variational Approach to the Unipotential Many-Electron Problem, Phys. Rev. **90**, 317 (1953).
- 59. J. D. Talman and W. F. Shadwick, Optimized effective atomic central potential, Phys. Rev. A 14, 36 (1976)
- 60. F. Tran and P. Blaha, Accurate Band Gaps of Semiconductors and Insulators with a Semilocal Exchange-Correlation Potential, Phys. Rev. Lett. **102**, 226401 (2009); D. Koller, F. Tran, and P. Blaha, Improving the modified Becke-Johnson exchange potential, Phys. Rev. B **85**, 155109 (2012).
- 61. D. Koller, F. Tran, and P. Blaha, Merits and limits of the modified Becke-Johnson exchange potential, Phys. Rev. B **83**, 195134 (2011)
- 62. M. A. L. Marques, J. Vidal, M. J. T. Oliveira, L. Reining, and S. Botti, Density-based mixing parameter for hybrid functional, Phys. Rev. B **83**, 035119 (2011)
- 63. W. Al-Sawai, H. Lin, R. S. Markiewicz, L. A. Wray, Y. Xia, S.-Y. Xu, M. Z. Hasan, and A. Bansil, Topological electronic structure in half-Heusler topological insulators, Phys. Rev. B 82, 125208 (2010).

- 64. D. J. Singh, Electronic structure calculations with the Tran-Blaha modified Becke-Johnson density functional, Phys Rev. B **82**, 155145 (2010).
- 65. D. J. Singh, Electronic structure calculations with the Tran-Blaha modified Becke-Johnson density functional, Phys. Rev. B **82**, 205102 (2010).
- 66. Y.-S. Kim, M. Marsman, G. Kresse, F. Tran, and P. Blaha. Toward Efficient Band Structure and Effective Mass Calculations for III Direct Band Gap Semiconductors, Phys. Rev. B 82, 205212 (2010).
- 67. V. Smith, M. Hermanowicz, G. A. Shah, and M. W. Radny, Spin–orbit and modified Becke–Johnson potential effects on the electronic properties of bulk Ge: A density functional theory study, Comput. Mater. Sci. 54, 37 (2012).
- H. Dixit, N. Tandon, S. Cottenier, R. Saniz, D. Lamoen, B. Partoens, V. Van Speybroeck, and M. Waroquier, Electronic structure and band gap of zinc spinel oxides beyond LDA: ZnAl2O4, ZnGa2O4 and ZnIn2O4, New J. Phys. 13, 063002 (2011).
- 69. M. C'esar, Y. Ke, W. Ji, H. Guo, and Z. Mi, Band gap of In<sub>x</sub>Ga<sub>1-x</sub>N: A first principles analysis, Appl. Phys. Lett. **98**, 202107 (2011).
- 70. R.M.Wentzcovitch, K.J. Chang, M.L. Cohen, Electronic and structural properties of BN and BP, Phys. Rev. B 34 (1986) 1071
- 71. K. Schwarz, P. Blaha, G.K.H. Madsen, Electronic structure calculations of solids using the WIEN2k package for material sciences, Comput. Phys. Commun.147 (2002) 71–76
- 72. J.C. Slater , Wave functions in a periodic potential, Phys. Rev. 51 (1937) 151–156.
  R. Terki, G. Bertrand and H. Aourag, Full Potential investigations of structural and electronic properties of *ZrSiO*<sub>4</sub>, Microelectronic Engineering 81 (2005), 514-523.
- 73. O.K. Andersen, Linear Methods in Band Theory, Phys. Rev. B 12 (1975) 3060– 3083.
- 74. D. R. Hamann, SemiconductorCharge Densities with Hard-Core and Soft-Core Pseudopotentials, E. Wimmer, H. Krakauer, M. Weinert, and A. J. Freeman, Full-

potential selfconsistent linearized-augmented-plane-wave method for calculating the electronic structure of molecules and surfaces: O<sub>2</sub> molecule, Phys. Rev. B 24, (1981) 864, Phys. Rev. Lett. 42, (1979) 662.

- 75. P. Blaha, K. Schwarz, G.K.H. Madsen, D. Kvasnicka, J. Luitz, An augmented plane wave plus local orbitals program for calculating crystal properties, Vienna University of Technology, Austria (2001) ISBN 3-9501031-1-2.
- 76. G. H. K. Madsen, P. Blaha, K. Schwarz, E. Sjo<sup>--</sup> stedt, L. Nordstrom, Efficient linearization of the augmented plane-wave method, Phys. Rev. B 64 (2001) 195134-1-9. S. Blugel and G. Bihlmayer, Full-potential Linearized Augmented Planewave Method, John von Neumann Institute for Computing, vol 31, (2006) 85-129.
- 77. K. Schwarz, P. Blaha, G.K.H. Madsen, Electronic structure calculations of solids using the WIEN2k package for material sciences, Comput. Phys. Commun. 147 (2002) 71–76.
- Z. Wu, R. E. Cohen, More accurate generalized gradient approximation for solids, Phys. Rev. B. 73 (2006) 235116.
- 79. J. P. Perdew, K. Burke, and M. Ernzerhof. Generalized Gradient Approximation Made Simple, Phys. Rev. Lett., **77**, (1996) 3865.
- J. P. Perdew, Y. Wang, Local Spin Density Approximation, Phys. Rev. B 45 (1992) 13244.
- W.E. Pickett, Pseudopotential methods in condensed matter applications, Comput. Phys. Rep. 9 (1989) 117.
- S. Adachi, Properties of Group-IV, III–V and II–VI Semiconductors, John Wiley & Sons, England, 2005
- I. Vurgaftman, J.R. Meyer, L.R. Ram-Mohan, Band parameters for III–V compound semiconductors and their alloys, J. Appl. Phys. 89 (2001) 5815
- M. Vukcevich, On the Elasticity of Ionic Compounds Under Hydrostatic Pressure, Phys. Status Solidi B 54 (1972) 219.

- 85. P.E. Van Camp, V.E. Doren, J.T. Devreese, Pressure Dependence of the Electronic Properties of Cubic III in Compounds, Phys. Rev. B 41 (1990)1598.
- H. Bross, R. Bader, Calculation of the Ground State Properties of Diamond and Cubic Boron Nitride, Phys. Status Solidi B 191, (1995) 369.
- 87. W. Martiensses, H. Warlimont, Springer Handbook of Condensed Matter and Materials Data, Springer, Berlin Heidelberg, Germany, (2005).
- R. M. Wentzcovitch, M. L. Cohen, Theory of structural and electronic properties of BAs, J. Phys. C: Solid State Phys. 19 (1986) 6791.
- A. Stroppa, M. Peressi, Composition and strain dependence of band offsets at metamorphic In<sub>(x)</sub>Ga<sub>(1-x)</sub>As/In<sub>(y)</sub>Al<sub>(1-y)</sub>As heterostructures, Phys. Rev. B 71 (2005) 205-303.
- 90. P. Dufek, P. Blaha, K. Schwarz, Applications of Engel and Vosko's generalized gradient approximation in solids, Phys. Rev. B 50 (1994) 7279.
- 91. S. Zh. Karazhanov, L.C. Lew Yan Voon, Ab initio studies of the band parameters of III–V and II–VI zinc-blende semiconductors, Fizika i Tekhnika Poluprovodnikov 39 (2) (2005) 177.
- F. D. Murnaghan, The Compressibility of Media Under Extreme Pressures, Proc. Natl., Acad. Sci. USA 30 (1947) 244.
- L. Pavesi, M. Guzzi, Photoluminescence of Al<sub>x</sub>Ga<sub>1-x</sub>As alloys, J. Appl. Phys. **75** (1994) 4779.
- S. K. Jain, P. Srivastava, Electronic and optical properties of ultrathin single walled boron nanotubes–An ab initio study, Computational Materials Science 50 (2011) 3038.
- 95. R. Chowdhury S. Adhikari, P. Rees, Optical properties of Silicon doped ZnO, Phys. B 405 (2010) 4763.

- O. Madelung, M. Schulz, H. Weiss (Eds.), Landolt- Bornstein Numerical Data and Functional Relationships in Science and Technology, vol. 17, Springer, Berlin, Heidelberg, New York, (1982).
- W. J. Moore, R. T. Holm, Infrared dielectric constant of gallium arsenide, J.Appl. Phys. 80 (1996) 6939.
- N. Chimot, J. Even, H. Folliot, S. Loualiche, Structural and electronic properties of BAs and B<sub>x</sub>Ga<sub>1-x</sub>As, B<sub>x</sub>In<sub>1-x</sub>As alloys, Physica B 364 (2005) 263.
- 99. Y. Yan,Q. Wang, W. Shu, Z. Jia, X. Ren,Xia Zhang,Y. Huang, The electronic and optical properties of quaternary B<sub>x</sub>Ga<sub>1-x</sub>As1-<sub>y</sub>Sb<sub>y</sub> alloys with low boron concentration: A first principle study, Phys. B 407, (2012) 4570
- 100.P. Blaha, K. Schwarz, P. Sorantin, and S. B. Trickey, Full-potential, linearized augmented plane wave programs for crystalline systems, Comput. Phys. Commun. 59, (1990) 399
- K. Schwarz, P. Blaha, Solid state calculations using WIEN2k, Computational Materials Science 28 (2003) 259–273.
- 102.J.Kohanoff and N.I Gidopoulos, Density Functional theory: Basic New Trends and Applications. In: Stephen Wilson. Handbook of Molecular Physics and Quantum Chemistry. Chichester: John Wiley &Sons. Volume 2, Part 5, Chapter 26,(2006) 532-568.
- 103.H. A. Kramers, "Some remarks on the theory of absorption and refraction of X-rays", Nature 117 (1926) 775.
- 104.R. de L. Kronig, "On the theory of dispersion of X-rays", J. Opt. Soc. Am. 12 (1926) 547.
- 105.Wang S, Swingle S F, Ye H, Fan F R F, Cowley A H, Bard A J 2012 Synthesis and Characterization of a p-type Boron Arsenide Photoelectrode Journal of the American Chemical Society 134 11056-9