# AN IMPROVED RING METHOD FOR CALIBRATION OF HYDROMETERS

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### AN IMPROVED RING METHOD FOR CALIBRATION OF HYDROMETERS

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A thesis submitted in fulfilment of the requirements for the award of the degree of Master of Science (Physics)

> Faculty of Science Universiti Teknologi Malaysia

> > AUGUST 2014

To my beloved parent

Mohd Nor bin Jaafar Fatimah bte Ithnin

To my beloved wife and children who always there for me

Noor Zarina bte Sulaiman Ahmad Farhan bin Mohd FazrulHisyam Ahmad Farihin bin Mohd FazrulHisyam Khairun Naajihah bte Mohd FazrulHisyam



You are always in my mind...

#### ACKNOWLEDGEMENT

I wish to express my sincere gratitude to my supervisor, Dr. Abd Khamim bin Ismail for his encouragement, guidance, criticism and friendship. My special thanks to Dr. Mark Clarkson, Dr. Kunihiko Toda and Mr.Futoshi Inoue for their technical support.

My greatest appreciation goes to Mrs Hafidzah Othman for her supports in this project. My fellow colleagues should also be recognized for their support and assistance in various occasions. Their views and opinions are indeed useful.

I am also indebted to the Ministry of Science, Technology and Innovation of Malaysia and SIRIM for their financial support.

And last but not least, special thanks go to all my family members who have given me strength and moral support in completing this thesis.

#### ABSTRACT

This study describes an improved hydrometer calibration method using a ring type sinker as a reference standard mass. Ring method offers simple yet effective hydrometer calibration method with comparable performance to other hydrometer calibration methods. This work also reports a ring method experimental setup for calibrating hydrometers. The theoretical calculation was developed and tested with experimental data. This calibration method can be used for any surface tension and reference temperature design of hydrometer. A suitable dimension of standard ring was used to sink hydrometers into distilled water. The distilled water was used as standard liquid, traceable to a standard solid density determined by hydrostatic weighing method. A tensiometer consisting of balance and Wilhelmy plate was used to measure the surface tension of the distilled water. The calibration results showed an improvement in the calibration range between 0.600 g mL<sup>-1</sup> and 1.000 g mL<sup>-1</sup> with an uncertainty of  $0.0002 \text{ g mL}^{-1}$  for hydrometers with scale graduations of 0.0005 g mL<sup>-1</sup>. The differences in measured scale corrections of this method compared to the comparison method and hydrostatic weighing method indicate a bias smaller than half of the hydrometer graduation. In comparison, this method offers simpler, cheaper calibration with accuracy comparable to other existing hydrometer calibration methods. Furthermore, no harmful chemicals were used as standard liquid especially mixtures of volatile hydrocarbons or aqueous solutions of acids.

#### ABSTRAK

Kajian ini menerangkan penambahbaikan tentukuran hidrometer dengan menggunakan cincin pemberat sebagai standard rujukan. Kaedah cincin ini menawarkan tentukuran hidrometer yang berkesan dan setanding dengan kaedah tentukuran hidrometer yang lain. Selain daripada itu, kajian ini juga melaporkan persediaan eksperimen untuk menentukur hidrometer dengan menggunakan kaedah cincin. Pengiraan teori telah dibangunkan dan diuji dengan data eksperimen. Kaedah penentukuran ini boleh digunakan untuk semua jenis ketegangan permukaan hidrometer dan suhu rujukan hidrometer. Cincin standard yang sesuai telah digunakan untuk menenggelamkan hidrometer ke dalam air suling. Air suling digunakan sebagai standard cecair yang bolehkesan kepada standard pepejal melalui kaedah hidrostatik. Tensiometer yang terdiri daripada alat penimbang dan plat Wilhelmy telah digunakan untuk mengukur ketegangan permukaan air suling. Keputusan tentukuran menunjukkan penambahbaikan dalam penentukuran antara 0.600 g mL<sup>-1</sup> dan 1.000 g mL<sup>-1</sup> dengan ketidakpastian sebanyak 0.0002 g mL<sup>-1</sup> untuk hidrometer dengan sub-skala 0.0005 g m $L^{-1}$ . Perbezaan dalam pembetulan skala digunakan bagi membandingkan kaedah cincin dengan kaedah perbandingan dan kaedah hidrostatik. Perbezaan dalam pembetulan skala menunjukkan perbezaannya sangat kecil. Sebagai perbandingan, kaedah ini menawarkan cara yang lebih mudah, penentukuran lebih murah dengan ketepatan setanding dengan lain-lain kaedah penentukuran hidrometer yang sedia ada. Seterusnya, tiada sebarang bahan kimia berbahaya digunakan sebagai standard cecair terutama campuran hidrokarbon yang mudah meruap atau asid.

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## LIST OF SYMBOLS

$ ho_c$	-	Calculated Density
$ ho_{a1,3}$	-	Air density when weighing the standard weight, S1
$ ho_a$	-	Air density
ρ	-	Hydrometer reading
$ ho_{at}$	-	Density of air at the time of the measurement at
		temperature t
$ ho_{st}$	-	Density of the sinker at temperature <i>t</i>
$ ho_{wt}$	-	Density of distilled water at temperature t
γ	-	Surface tension of the distilled water
$\sigma$	-	Surface Tension liquid
$\beta_{cry}$	-	Thermal expansion coefficient of crystal sphere
$\Delta s$	-	Balance sensitivity
$A_o$	-	Contact angle
$A_f$	-	Contact angle of the liquid at the hydrometer stem
$C_T$	-	Temperature Corrections
$C_{ST}$	-	Surface Tension Corrections
$C_M$	-	Meniscus Corrections
$C_{CAL}$	-	Hydrometer Calibration Corrections
d	-	Stem diameter hydrometer
D	-	Diameter of hydrometer stem
$F_M$	-	Mass Force
$F_{ST}$	-	Surface Tension Force
$F_i$	-	Water Force
$F_a$	-	Air Force
F	-	Force
$Fg_{sinker}$	-	Standard sinker gravitational force
$Fg_{hyd}$	-	Hydrometer gravitational force

$F_{ST}$	-	Surface tension force
Fa <sub>hyd</sub>	-	Hydrometer buoyancy force in air
Fi <sub>hyd</sub>	-	Hydrometer buoyancy force in liquid
Fisinker	-	Sinker buoyancy force
g	-	Gravity
$g_{RS}$	-	Gravity ratios
$g_l$	-	Local gravity
i	-	Nominal scale range
L	-	Length
m	-	Mass
$M_{S1}$	-	True masses of the standard weight S1
$M_{S2}$	-	True masses of the standard weight S2
M <sub>cry</sub>	-	True mass of the crystal sphere
М	-	Mass of the hydrometer
$m_s$	-	Mass of sinker(s) on the hydrometer
$M_{wet}$	-	Mass of the Wilhelmy plate wetted
$M_{dry}$	-	Mass of the Wilhelmy plate dry
$m_H$	-	Mass of the hydrometer
Р	-	Ambient pressure
R	-	Hydrometer reading
S	-	Scale length
$S_{f}$	-	Surface tension of the liquid
S	-	Surface Tension Liquid
$S_o$	-	Surface tension
So	-	Design Surface Tension of hydrometer
Т	-	Ambient temperature
t	-	Liquid temperature
$t_S$	-	Reference temperature of hydrometer
<i>t</i> <sub>plate</sub>	-	Thickness of the Wilhelmy plate
V	-	Volume
$V_{SI}$	-	Volume of standard weight S1

$V_{S2}$	-	Volume of standard weight S2
$V^{20}_{cry}$	-	Volume of crystal sphere
$V_i$	-	Immersed volume of hydrometer
$V_t$	-	Volume of the hydrometer at temperature $t$
W	-	Width of the Wilhelmy plate

## LIST OF ABBREVIATIONS

API	-	American Petroleum Institute
BS	-	British Standard
DCWU	-	Department of Chemistry, Wayne University
KRISS	-	Korea Research Institute of Standard and Science
MSL-NZ	-	Measurement Standard Laboratory, New Zealand
NMI	-	National Metrology Institute
NML-SIRIM	-	National Metrology Laboratory, SIRIM Berhad
NMIJ	-	National Metrology Institute of Japan
SI	-	International System
UUT	-	Unit Under Test

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### **CHAPTER 1**

#### **INTRODUCTION**

#### 1.1 Background of Problem

The earliest hydrometer ever invented was by Hypatia [1, 2]. She lived in Alexandria, Egypt and was born around 370AD. There were also inventors other than Hypatia including Leonardo Da Vinci [3], Antoine Baume [4], William Nicholson [5] and James Watt [6]

Hydrometer is an instrument used to measure a wide range of density of various liquid [7]. It will freely float with the stem partially immersed in liquid to an extent depending on the density of the liquid. The lower the density of the liquid the deeper the stem sink. There are many types of hydrometers namely: Density hydrometer, Specific Gravity hydrometer, Percentage hydrometer and Arbitrary scale hydrometer [8].

Hydrometers have found many practical applications particularly for measuring liquid density in many research areas and industries such as food and beverage, chemical, petroleum and gases [9, 10].

Before hydrometers can be used for measurement, they must go through calibration process. Calibration is a relationship between known value of a measurement and measuring instrument. The device with the known value is the standard. The second device or the measuring instrument is the unit under test or device being calibrated. The calibration objectives are to ensure readings from an instrument are consistent with other measurements and to determine the accuracy of the instrument readings.

Hydrometer calibration methods such as hydrostatic weighing method, comparison method, and ring method are the most popular methods commonly used by many national standards laboratories around the world [11-14]. There are many National Metrology Institutes such as Korea, New Zealand, Japan, Australia, Italy, Brazil and China using hydrostatic weighing method to calibrate the hydrometer [15-18]. They are using hydrostatic weighing method because of high accuracy compared with other method but high costly to develop. So there are many secondary laboratories using comparison method. National Metrology Institute, India is using ring method to calibrate the hydrometer [7, 12]. Ring method is more accurate compared to comparison method [19].

In the hydrostatic weighing method, the hydrometer is suspended from a weighing balance in order to determine the hydrometer mass in air and in standard liquid [20]. Both density of liquid and solid can be determined by using this method [21, 22]. It offers a high degree of accuracy but a high cost to develop. On the other hand, a comparison method offers simpler step where a hydrometer is compared to a standard hydrometer in chemical solution [13]. However it is time consuming since the chemical temperatures need to be stabilized before reading can be taken. The chemicals used as medium such as methanol, petroleum ether, sulphuric acid, mercury II iodide and potassium iodide are harmful and this is also a costly method to develop. The third method was so-called a ring method because a suitable dimension of metallic ring is used to sink the hydrometer into the liquid when inserted into its stem [12]. Harmful petroleum liquid such as diethyl ether and petroleum ether will be used as a standard medium. An expensive and fragile standard hydrometer was used to measure the density of the standard petroleum liquid. However, the calibration range of this method is very limited

compared to other methods, which is only between 0.600g/ml to 0.650g/ml. Expanded range of calibration is very important and is currently on demands since typical hydrometer samples from industries are in the range between 0.600g/ml to 1.000g/ml.

#### **1.2 Problem Statement**

The most commonly used hydrometer calibration methods previously discussed have several advantages but also have some major limitations and drawbacks such as the used of harmful chemicals as standard solution, complicated calibration steps, limited range of calibration in the order of 0.600g/ml – 0.650g/ml, time consuming and expensive. This research project proposed a modified ring method which could solve some of those limitations.

### 1.3 Objectives

The objectives of this study are;

- i. to design and construct a hydrometer calibration procedure based on ring method,
- ii. to calibrate various samples of hydrometer using the proposed ring method and
- iii. to verify and compare the performance of the proposed ring method with the existing hydrometer calibration method commonly used in Density Laboratory, National Metrology Laboratory, SIRIM Berhad (NML-SIRIM) and other National Metrology Institutes from other countries.

#### 1.4 Research Significance

This work proposed an improved ring method for hydrometer calibration by using a ring type sinker as a traceable reference mass and later called as standard sinker. This standard sinker was added into the hydrometer stem and both were immersed into standard distilled water. The density of the standard distilled water will be measured using crystal sphere or solid artifact. This is much cheaper compared to an expensive and fragile standard hydrometer commonly used in hydrometer calibration. This method is predicted to be more accurate for up to five decimal places compared to the most popular methods mentioned above. The hydrometer calibration range could be further improved from 0.600 g/ml to 1.00 g/ml.

Furthermore, time spent for hydrometer calibration and monthly labor cost could be reduced since it offers much simpler calibration steps. The used of expensive and fragile standard hydrometer and standard harmful chemicals solution also can be avoided.

#### 1.5 Scope

To meet the objectives, the following studies must be carried out:

- i. Preparation and construction of the experimental setup for the ring hydrometer calibration method.
- ii. Characterization and optimization of the parameters involved for verification purpose between the proposed method and the existing hydrometer calibration method.
- iii. Construction of a computerized data acquisition system for the ring hydrometer calibration method.

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