

WAVELET BASED SIGNAL PROCESSING TECHNIQUES FOR MEDICAL
IMAGE FUSION

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To our Prophet Rasullu allah S.A.A.W.S First teacher

To my parents for always believing in me

To my brothers support and Encouragement

To my beloved Wife,

To my fruits daughters, and son

and

To My Ustaz Al-Shaheed Ismail and his Son Sinan

...

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Saif Saaduldeen

ABSTRACT

Recently signal and image processing have been central to researchers and scholars through present various applications and solve many problems in different fields in our life. This thesis presents signal processing algorithm for multi-modal medical images by fusion technique. Medical image fusion has been used to derive texture from multi-modal medical image data. The idea is to improve the image content by fusing images like computer tomography (CT) and magnetic resonance imaging (MRI) images. This derived texture can be assisted by medical examiner for various purposes such as, diagnosing diseases, detecting the tumor, surgery treatment, and clinical treatment planning system. Our object to get more as possible better image fused high quality and clearer. Previous fusion based on the spatial domain and another depends on the frequency domain, both these strategies have disadvantages like contrast reduction, weak quality, artifact, and ringing. Therefore researchers in medical fusion field attempt to solve these problems by many algorithms are presented and are competed to improve previous results. Hence, this work present an algorithm based on Discrete Wavelet Transform (DWT) to obtain the scale and detail coefficients of the various images. Different fusion methods are also used comparing ; Non-linear fusion rule (NLFR), average mean value (AMV), maximum absolute rule (MAR), and Weighted Condition Value (WCV) to correlate the coefficients each method is used separately then produce the last result by Inverse Discrete Wavelet Transform (IDWT) which based on single level transform. The novelty in this thesis are using two strategies, first one, deal with match measures are calculated as a whole to select the wavelet coefficients coming from different wavelet transform filters banking ,Second once using NLFR method, output results to compare with the chosen method so as to determine which is better. The medical fusion system implemented by MATLAB software, and analyzed the results done by Petrovic Fusion Algorithm (PFA). The method yields high scores the conventional methods. Overall this method has high potential for a better application of fusion in the medical imaging field.

ABSTRAK

Baru-baru ini isyarat dan pemrosesan imej merupakan pusat penyelidikan dan ulama melalui masa ini pelbagai aplikasi dan menyelesaikan banyak masalah dalam bidang yang berbeza dalam kehidupan kita. Tesis ini membentangkan isyarat algoritma pemrosesan imej perubatan multi-modal dengan teknik fusion. Idea ini adalah untuk meningkatkan kandungan imej dengan menggabungkan imej seperti komputer tomografi (CT) dan pengimejan resonans magnetik (MRI) imej. Gabungan sebelumnya berdasarkan domain ruang dan satu lagi bergantung kepada domain frekuensi, kedua-dua strategi ini mempunyai kelemahan seperti pengurangan. Sebaliknya, kualiti lemah, artifak, dan nada. Oleh itu penyelidik dalam gabungan perubatan bidang usaha untuk menyelesaikan masalah-masalah ini oleh banyak algoritma dibentangkan dan bersaing untuk meningkatkan hasil sebelumnya. Oleh itu, kerja ini membentangkan satu algoritma berdasarkan diskret ubahan wavelet (DWT) untuk mendapatkan skala dan terperinci pekali pelbagai imej. Kaedah gabungan yang berbeza juga digunakan membandingkan; Peraturan gabungan bukan linear (NLFR), nilai purata min (AMV), pemerintahan mutlak maksimum (MAR), dan wajaran Keadaan Nilai (WCV) untuk mengaitkan pekali setiap kaedah yang digunakan secara berasingan kemudiannya mengeluarkan hasil terakhir oleh songsang diskret ubahan wavelet (IDWT) yang berdasarkan tahap tunggal mengubah. Sesuatu yang baru di dalam tesis ini menggunakan dua strategi, pertama, menangani Perlawanan langkah dikira secara keseluruhan untuk memilih pekali ombak kecil datang dari ombak kecil yang berbeza mengubah perbankan penapis, sekali menggunakan kaedah NLFR Kedua, keputusan output untuk membandingkan dengan kaedah yang dipilih jadi untuk menentukan yang lebih baik. Sistem gabungan perubatan dilaksanakan oleh perisian MATLAB, dan menganalisa keputusan dilakukan oleh Petrovic Fusion Algoritma (PFA). Kaedah ini menghasilkan markah yang tinggi kaedah konvensional. Keseluruhan kaedah ini mempunyai potensi tinggi untuk kegunaan yang lebih baik daripada gabungan dalam bidang pengimejan perubatan.

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LIST OF ABBREVIATIONS

CT	-	Computed Tomography
MRI	-	Magnetic Resonance Imaging
PET	-	Positron Emission Tomography
SPECT	-	Single photon Emission Computed Tomography
PSNR	-	Peak to noise Signal Ratio
MSE	-	Mean Square Error
NIR	-	Night Image Resolution
BT	-	Brovey Transform
IHS	-	Intensity Hue Saturation
PCA	-	Principle Component Analysis
SVR	-	Synthetic Variable Ratio
IF	-	Image Fusion
MIF	-	Medical Image Fusion
MRA	-	Multi-resolution Analysis
LPT	-	Laplacian Pyramid Transform
WT	-	Wavelet Transform
DWT	-	Discreet Wavelet Transform
CWT	-	Continues Wavelet Transform

FIR	-	Finite Impulse Response
1 D	-	One Dimension
2 D	-	Two Dimensions
LPF	-	Low Pass Filter
HPF	-	High Pass Filter
LL1	-	Low Frequency coefficient (approximation) in one Level
HL1	-	High Frequency coefficient (Horizontal) in one Level
LH1	-	High Frequency coefficient (Vertical) in one Level
HH1	-	High Frequency coefficient (Diagonal) in one Level
Db2	-	Daubechies 2
Db4	-	Daubechies 4
FB	-	Filter Banking
AMV	-	Average Mean Value
MAR	-	Maximum Absolute Rule
WCV	-	Weighted Condition Value
NLFR	-	Non Liner Fusion Rule
HVS	-	Human System System
PFA	-	Petrovic Fusion Algorithm

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CHAPTER 1

PROJECT OVERVIEW

1.1 Introduction

Many modern medical scenes need fusion techniques in order to produce images capable of improving clinical diagnosis. The medical image can be classified into high resolution and low resolution, or classified according to sensor device and physical process which is used to generate the images (multi-modality image).

Take for example, the CT and MRI images of the brain; each one has high resolution but different multi-modality, the CT provides better analysis in hard tissue while the MRI is more useful in soft tissue. Positron emission tomography (PET) low resolution image contains functional information, while Single Photon Emission Computed Tomography (SPECT) image provides information about visceral metabolism and blood circulation [1]. Fusion process is applied on these images to get a new image containing all texture of the original images as will be proved and discussed in the subsequent parts to come.

Therefore this research uses image fusion technology, and applies it on the brain images, by using two samples from images; one from sample magnetic resonance imaging (MRI) and second from sample computed tomography (CT) scan, and then these images are integrated using Wavelet Transform Methods This is illustrated in Figure 1.1.

The research tries to work on getting acceptable results through applying wavelet transform methods in the remote sensing field of medical imaging.

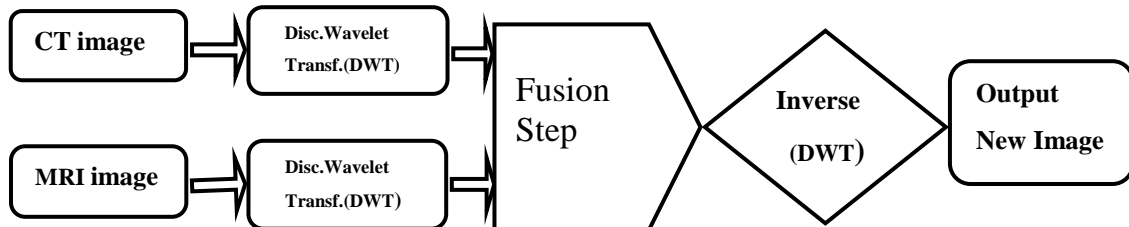


Figure 1.1 Block diagram medical image fusion process

This research will also evaluate the performance of the organization of fusion technology suitable for medical images after getting results by modern methods of evaluation, and then ultimately determined by the user in general as shown in Figure 1.2. There are many methods to check and evaluate the results after fusion process is finished such as peak signal to noise ratio (PSNR), Petrovic Algorithm which is used in this project.

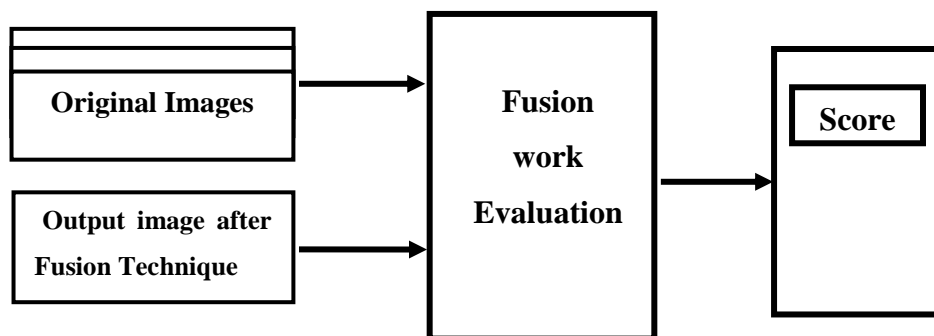


Figure 1.2 Block diagram evolution of a fusion work

1.2 Problem Statement

Fused medical image is required to get better contrast and quality is important for medical images. Previous studies that used wavelet transform technique to fuse medical image did not cover many wavelet banking filters and as such did not obtained optimum results. Earlier algorithms are based on traditional methods, hence less accurate fusion result were obtained. Most previous works fusion evaluation methods are based on PSNR, mean square error (MSE) and Entropy that caters for only one image at a time.

1.3 Motivations for the Research

There is need to provide the technique of image fusion more effectively through analytical study of medical images using wavelet transforms technique. A new tool for medical diagnosis is obtained in an effective manner, dependent on the integration of two or more images, from the same scene or the same section, and then incorporating good features of each image and injecting it into a new image to form a more accurate picture and clearer input images. This process is called image fusion. Image fusion technique within short time is able to overcome many obstacles that face the subject of image enhancement compared to traditional techniques used in various fields like remote sensing, military surveillance, and medical field [2]. Therefore, more research is needed in this field to develop medical technology and so this is what this study is going to try to do by combining most of the images features in one image using image fusion technique. This technique has an important role in providing information required by medical doctors in providing better medical diagnostics services.

1.4 Objectives of Project

The basic objectives to be carried out for this research are:

- i. To use spectral domain techniques of multi-resolution transform based on various banking wavelet transform filters to obtain an optimum fused image.
- ii. To develop an enhanced fusion algorithm that uses correlation coefficient based on the Non-Linear Fusion Rule compared with traditional methods.
- iii. To evaluate Performance using the Petrovic Algorithm. This method caters for multiple images at a time unlike other evaluation methods.

1.5 Project Scope

This project is covers the CT and MRI medical images. These images have different medical diagnosis specification but have same dimensional and quality for the same scene from a human body which is obtained from the official medical fusion website. The medical image fusion system is implemented by MATLAB software, which related on the wavelet toolbox through using most of the wavelet filters banking in single level transform. The project will be focusing on result quality evaluated by Human Visual System and Petrovic Fusion Algorithm.

1.6 Thesis Layout

Chapter 1 Project Overview, Problem Statement, Objectives of project, Motivation for the Research, project scope and limitation. Last part of this chapter will present the report layout.

Chapter 2 Two-dimensional medical signal, Example of image fusion, Properties of the CT and MRI Medical images, Computed Tomography and Magnetic resonance imaging specification, Fusion Technique Role to Medical Images, Previous Works on Image Fusion and Medical Image Fusion

Chapter 3 Continues and Discrete Wavelet transform in one, and Two Dimension, Discrete wavelet transform and filters banking, Types of Filter Banking in 2D-DWT.

Chapter 4 focuses in project design methodology including algorithm and methods implementation steps.

Chapter 5 presents the results and discussion that can be obtained from various scenarios of experiment. These results are evaluated by Human Visual System and Special statistical algorithm.

Chapter 6 summarizes the conclusions from this research. The last part of this chapter discusses recommendation for future works and project contribution.

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