# NUMERICAL ANALYSIS OF BOVINE TRABECULAR BONE BY USING PHYSIOLOGICAL LOADS SPECIFIC TO NORMAL WALKING LOADS AND DOWN STAIRS LOADS.

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> > JANUARY 2013

To my parents and family, thanks for patiently supports and courage during till completion of master course...

#### ACKNOWLEDGMENT

In humble to Allah, The Eternal Refuge, neither begets nor is born, Nor is there to Him any equivalent. I am as one of the creatures. Allah, Him the creator of everything allows me to complete this dissertation as fulfillment of Master Science in Mechanical Engineering by taught course.

In a deepest appreciation goes to my supervisor Dr Muhammad Noor B. Harun on the valuable encourage to this dissertation project. Followed by my cosupervisor on continuous support through project, with tight follow-up, courageousness to give and share anything important in the completion project. At the same time, I would like to thanks to my colleagues in accompanying experiences, thought, moral support and everything during project execution.

In instance to my closest friend, she lures so much support on providing journal which is related from biological matter till medical term. With time, money she spent for just to explain and makes me understand thoroughly the medical was such valuables effort. May Allah give the best return on the efforts offered.

Last but not least, my greatest appreciation to everyone who has been involved in this research even by coincidence. May Allah bless you all in return.

#### ABSTRACT

This project is containing of simulation on sectioned Bovine Trabecular Bone. The Bone was extracted from fresh bovine bone with interested section dimension for about  $2 \times 2 \times 3.5$  mm. After scanned process through µCT scanner, the bone was constructed via Mimics software. With preferred size of elements and consumed time per simulation, 774,996 elements were selected meshing number to use. Combination of 3 axes loads for both physiological movement specific to normal walking loads and downstairs loads, those presented one minute trends cycle completed both cycle as reliable applying loads in the consequent Trabecular Bone model. Simulation was conducted by fixed the model at the bottom and applying gait loads at the top, revealed most deflection of Trabecular Bone were occurred while down stairs activities. The most stress entire simulation also weighed to down stairs activities. From that, it composes young modulus for normal walking is 14.8Gpa. In the other hand, downstairs activities complies 14.9Gpa. Deviation on the experimental data of compressive test, could be translate on different of density model, besides, by doing only compressive stress could not represent on physiological loads on actual real situation.

#### ABSTRAK

Projek ini mengandungi simulasi Tulang Trabecular lembu yang telah disegmen. Tulang tersebut diekstrak dari tulang lembu segar dengan dimensi seksyen utama untuk  $2 \times 2 \times 3.5$ mm. Selepas proses imbasan melalui pengimbas  $\mu$ CT, tulang telah dibina melalui perisian Mimics. Dengan saiz pilihan elemen dan masa yang digunakan setiap simulasi, 774.996 elemen dipilih bersirat nombor untuk kegunaan. Gabungan 3 paksi beban bagi pergerakan kedua-dua fisiologi spesifik kepada beban berjalan normal dan beban menuruni tangga, yang dibentangkan satu minit trend kitaran, ia tersebut menyempurnakan kitaran kedua-dua sebagai beban aplikasi dalam model Tulang Trabecular. Simulasi telah dijalankan dengan model berada pada posisi tetap disebelah bawah dan menggunakan beban di atas, ini telah mendedahkan pesongan yang paling pada Tulang Trabecular berlaku semasa aktiviti menuruni tangga. Keseluruhan simulasi yang paling tekanan juga ditimbangi kepada aktivitiaktiviti menuruni tangga. Daripada itu, ia menghasilkan "Modulus young" untuk berjalan normal adalah 14.8Gpa. Selain itu, aktiviti-aktiviti menuruni tangga juga mematuhi 14.9Gpa. Sisihan pada data eksperimen ujian mampatan, boleh diterjemahkan pada model yang berbeza ketumpatan, selain dengan melakukan hanya kepada tegasan mampatan dan tidak boleh mewakili beban fisiologi sebagai menyamai keadaan sebenar sebenar

## TABLE OF CONTENTS

CHAPTER	TITLE	PAGE
	ACKNOWLEDGEMENT	v
	ABSTRACT	vi
	ABSTRAK	vii
	TABLE OF CONTENTS	viii
	LIST OF FIGURES	xi
	LIST OF TABLES	xiii
	LIST OF EQUATION	xiv
1		
1	INTRODUCTION	
	1.1 OBJECTIVES	16
	<b>1.2 PROBLEM STATEMENTS</b>	16
	1.3 SCOPE OF PROJECT	18
	1.4 SIGNIFICANCE OF PROJECT	19

2 LITRETURE REVIEW
--------------------

2.1 INTRODUCTION	20
------------------	----

2.2	BONE STRUCTURE	22
	2.2.1 OSTEOBLASTS AND OSTEOCLASTS	23
2.3	BONE REMODELING	24
2.4	MORPHOLOGY	25
2.5	MECHANICAL LOADING ON CANCELLOUS BONE	26
2.6	CANCELLOUS'S MECHANICAL PROPERITIES	27
2.7	SPECIMENS PREPARATION METHODS	33
2.8	<b>REPLACEMENT OF HUMAN BONE</b>	34
2.9	SUMMARY	35

### 3 METHODOLOGY

3.1	INTRODUCTION	36
3.2	METHODOLOGY FLOW CHART	37
3.3	MATERIAL PREPARATION	38
3.4	μCT SCANNER	39
	3.4.1 RECONSTRUCTING 3D MODEL	40
3.5	PROCESS OF FE PACKAGE NECESSITIES	42
3.6	MESHING	42
3.7	MATERIAL PROPERTIES	45
	<b>3.7.1 BASIC MATERIAL PROPERTIES</b>	45
	3.7.2 ELASTO – PLASTIC MATERIAL PROPERTIES	46
3.8	LOADINGS	49
	<b>3.8.1 COORDINATES SYSTEM</b>	49
	3.6.2 GAIT LOADING	50
	<b>3.8.3 POLYNOMIAL OF GAIT EQUATIONS</b>	51
	3.8.4 DOWN STAIRS LOADINGS	53
	<b>3.8.5 POLYNOMIAL DOWN STAIRS EQUATIONS</b>	54

# 4 **RESULT AND DISCUSSION**

4.1 INTRODUCTION	57
4.2 CONVERGENCE STUDY	58
4.3a DISPLACEMENT CONTOUR (Gait loading)	60
4.3b DISPLACEMENT CONTOUR (Down Stairs loadings)	63
4.4 STRESS-STRAIN CURVES	66
4.5 CRACK INITIATION	69
4.6 SUMMARY	70

### 5 CONCLUSION

5.1	CONCLUSION	71
3.1	CONCLUSION	11

### REFERENCES

Appendixes

56

72

### LIST OF FIGURES

FIGURE NO.

### TITLE

#### PAGE

1.0	(a) Cancellous Bone marrow in-Situ,	
	(b) Cancellous bone without marrow	21
2.0	Bone cross section view[13].	22
3.0	Methodology Flow Chart.	37
4.0	(a) Raw Scanned Images, (b) Stack Images	40
5.0	3D model of constructed Trabecular Bone	41
6.0	Extremely Course Meshing	43
7.0	3D model meshing elements (496904)	44
8.0	3D model meshing elements (816450)	44
9.0	Elastic – Plastic region of Plastic material properties	47
10.0	The Stress-Strain behavior of (a) Elastic perfectly plastic, (b)	
	Kinematic Hardening, (c) Isotropic Hardening (d) Isotropic &	
	Kinematic Hardening. Adapted [57].	48
11.0	Coordinate system in gait analysis by Bergman et al.,2001 [2].	49
12.0	Resultant of Hip Contact and Components, Average cycle for	
	Normal Walking. Adapted [2]	50
13.0	Plotted graph for gait cycle (Fx, Fy, Fz)	51
14.0	Down Stairs loading on femur neck.	
	Adapted from Bergman et al.,[2]	54
15.0	Plotted loading graph for Down Stairs (Fx, Fy, Fz)	54
16.0	Plotted graph of Von misses against No. of Elements	
	as convergence study.	58

17.0	Displacement contour in y-x view (gait loadings)	60
18.0	Displacement contour in z-x view (gait loadings)	61
19.0	Displacement contour in y-x view (down stairs loadings)	63
20.0	Displacement contour in z-x view (down stairs loadings)	64
21.0	Deflection data between Gait Loads and Down Stairs loads.	65
22.0	Stress-Strain curves for 3 types of bodyweight	66
23.0	Down Stairs Loadings and Gait Loadings for bodyweight 60kg.	67
24.0	Density effect of Stress Strain Curve vs. experimental data by	
	Carter and Hayes, 1977[32].	68
25.0	Total displacement by increasing number of cycles	69

# LIST OF TABLES

TABLE NO.	TITLE	PAGE
1.0	Comparison of method used in vitro experiments deta	ailing their
	advantages and limitations	30
2.0	Basic Trabecular Bone material properties	45

# LIST OF EQUATIONS

# EQUATION NO.

# PAGE

Equation 1	52
Equation 2	52
Equation 3	52
Equation 4	52
Equation 5	52
Equation 6	52
Equation 7	53
Equation 8	53
Equation 9	53
Equation 10	55
Equation 11	55
Equation 12	55

**CHAPTER 1** 

#### INTRODUCTION

This project with title Numerical analysis of Bovine Trabecular Bone by using physiological loads specific for 2 types of normal activities which are Gait loadings and Down Stairs loadings. In this first chapter, author will details the objectives, problem statements, scope of project and the significance of the project. As reflect of that, there are four objectives needs to achieve by through the concurrent problems over analysis hypothesis. However, this numerical project needs to follows scope and method constraint. Otherwise, it will be hardest to control in by taking all other environment consideration. End of this first chapter, author discussed the prolific significance of this project thorough expected findings result.

#### 1.1 **OBJECTIVES**

- To analyses the parametric behavior of the Trabecular bone respect to physiological activity (Normal walking & Down Stairs).
- To study the relationship between bodyweight and stress distribution over Trabecular bone.
- To examine and compare the pre-location of crack initiation as due to cyclic gait loadings.

#### **1.2 PROBLEM STATEMENTS**

From previous researched approaches specifically on Trabecular bone, mostly researchers constructing alike model to representing the actual Trabecular bone. Since the existence of the bio-scanner, the technology was appreciates completely in other dimension specifically in numerical analysis. The capability of scanner neither dubious nor trustworthy, the technology brings easiness on constructing similar to an actual model with even in very complex 3D models. In the absent of human bone, there is still other alternative with similar mechanical properties to replace human bone. The bovine bone is the suitable bone to used by researchers during experimental. Readily available and cheap, has a similar mechanical properties brings this project forward.

Femur neck is said the second highest stress occurred during standing activity. They are also the only connected junction between legs and others organs which are implies a fury loads during physical activity. Understanding on stress distributions and reactions is such a helpful way as continuation study on femur neck of human bone. There were several studies on the reaction contact on hips by numerous researchers [1-3]. With those findings, it shall translate the reaction of

internal stress bone behavior from basic physical movement loadings. In addition of that, pressure distribution over trabecular bone could easily analysis through stress contours. Furthermore, by using FE package features bone displacements with respect to stresses are able determines.

The intact of bodyweight and stress distribution is likely to give a linear assumption. For example, the person has weightier bodyweight is prone to have more local stresses on their hips. Simultaneously, the reactions on femur necks are equivalence to the exerted loadings. Through numerical simulation, mechanical properties will reveal the relation between bodyweight and the young modulus. Yet, it composed the suggestion risk of obese.

Normal walking and Down stairs act is of a common activities done by human. These simple activities had chaos assumption on which is contributes more stress during activity or which activity will more easily to jades for human task. In instance of that, both physiological activities have a second complete cycle. Thus, comparing between cycles is possible to make and realization. It is a different form of others activities such as slow walking, up stairs sitting down, standing on 2-1-2 legs or knee bend, all those activities had elapse more times in one completed cycles [2].

Fatigue failure is always referred to continuous cyclic loading [4]. Interestingly, human bones are always having cyclic loadings throughout any physical activities. Since the exposure of human bone against fatigue is risky. Knowing the signs of fatigue behavior under gait cycles are great achievement for future study. Practically, fatigue failure has to go through two phases of crack before failure occurred. The first is crack initiation and the second is crack growth. Location of crack initiation might sees if the crack is started. By that, the pressure contour and bone displacements could explain the situation.

#### **1.3 SCOPE OF PROJECT**

First scope of this project is to construct the Trabecular Bone structure. The model is constructed through scanning images from micro-CT scanner. The extension of the uses and advance technology brings easiness to examine any complex structure shape and design. Unlike other researcher approaches, mostly of them design their own Trabecular structure alike by composed a number of struts in definite ratio. First limitation is size, most of the FE package had a maximum numbers of elements. Thus, constructed Trabecular model will only considered in specimen dimension, shape of the specimen and meshing element size. All those consideration are important in getting an optimal finding result.

Second scope of this project is to perform static analysis by using FE package. Nowadays, numerical approaches seem to be very imperative in initial or preliminary study. That due to precision of numerical simulation brings draft taught of the simulation problem. In addition of that, stage of numerical study is far cheaper than constructing or setting apparatus for real experiment. Not repudiate on the experiment work, instance of that, hand-on experimental work is the real situation under a very minimal engineering assumption or constraint. Differently approaches on finite element simulation, the software is tends to excludes any external environment contact to the simulation models. That limitation concludes numerical simulation is just a tool to get a general problem solution near to the real situation.

Third scope of this project is to compares finding data result between physiological activities. Specific to this project, only two types of activities will be simulating thoroughly. The first is gait cycle and second is down stairs loadings. Both of them are the loads which have a direct contact between femur and tibia. By simply to understand the reaction involves in human hips during normal walking and down stairs. Data later should compares to the experimental result, even though applying physiological loads to the Trabecular Bone is novel. However, the comparison is possible by matching with uniaxial experimental data from various journals source in varies Trabecular bone samples.

#### **1.4 SIGNIFICANCE OF PROJECT**

In the first significance, exposing the actual physiological loadings on the 3D modeled Trabecular bone. The physiological loadings involved for this particular project is specific only for gait cycle and down stairs cycle loadings. Both cycles are referring to common activities for every human being. Thus, regain the understanding the mechanical properties of human bone (specify to Trabecular bone on femur neck) during involvement of physiological loadings. From that, the differentiation between physiological could be clearly stated in term of mechanical properties.

Second significance for this project is from the mechanical properties, the effect of bodyweight on the physiological activities capable to hypotheses as refer to stress-strain curve. The relation between bodyweight and physiological activities might important to obese generation and by hope finding result enable the risk of overweight body.

Prediction of bone life in fatigue study is the most preference. The prediction of fatigue life could employ in every angle of fatigue study. In order to manipulate the use of the Trabacular Bone application, estimation curve is a basic foundation of fatigue study as base on physical activities. The curve (S-N curve) is a reference to any cyclic human activity, same goes with the application of material S-N curve. As basic of the fatigue failure, crack initiation will start first before the development of crack till failure. By increasing two cycles of gait loadings, pre location of fatigue failure might appear through contour distribution on trabecular bone.

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- 74
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