

# Fuzzy Control System Review

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**Abstract**— Overall intelligent control system which runs on fuzzy, genetic and neural algorithm is a promising engine for large –scale development of control systems . Its development relies on creating environments where anthropomorphic tasks can be performed autonomously or proactively with a human operator. Certainly, the ability to control processes with a degree of autonomy is depended on the quality of an intelligent control system envisioned. In this paper, a summary of published techniques for intelligent fuzzy control system is presented to enable a design engineer choose architecture for his particular purpose. Published concepts are grouped according to their functionality. Their respective performances are compared. The various fuzzy techniques are analyzed in terms of their complexity, efficiency, flexibility, start-up behavior and utilization of the controller with reference to an optimum control system condition.

**Index Terms**— Fuzzy, Intelligent Control System

## 1 INTRODUCTION RESERCH BACKGROUND

An intelligent system has the ability to act logically in an uncertain environment to achieve certain behavioral sub goals which support the system's ultimate goal. Control systems are a key enabling technology for the increase in functionality and safety of many critical applications such as transportation systems, manufacturing systems, medical devices, and networked embedded systems . Modern power systems are non-linear and behave in a highly complex manner with continuous extensive variations in their operating conditions. Design of this type of systems requires knowledge in many multi-disciplines. The most popular technique is to use Fuzzy controller in which expert knowledge can be incorporated into the design. Most of Fuzzy controllers which are used in industry have the same structure as incremental PD or PID controllers. Controller design using Genetic Algorithm and neural network has been combined with Fuzzy controller to form an intelligent control scheme. The first feedback device on record was the water clock invented by the Greek Ktesibios in Alexandria Egypt around the 3rd century B.C . [2] . This was certainly a successful device as water clocks of similar design were still being made in Baghdad when the Mongols captured that city in 1258 A.D. The first mathematical model to describe plant behavior for control purposes is attributed to J.C. Maxwell who in 1868 used differential equations to explain instability problems encountered with James Watt's flyball governor; the governor was introduced in 1769 to regulate the speed of steam engine vehicles.[1] . When J.C. Maxwell used mathematical modeling and methods to explain instability problems encountered with James Watt's flyball governor, it demonstrated the importance and usefulness of mathematical models and methods in understanding complex phenomena and signaled the beginning of mathematical system and control theory. It also signaled the end of the era of intuitive inventions. Control theory made significant strides in

the past 120 years, with the use of frequency domain methods and Laplace transforms in the 1930s and 1940s and the development of optimal control methods and state space analysis in the 1950s and 1960s. Ideas such as optimal control (in the 1950s and 1960s) and stochastic, robust, adaptive and nonlinear control methods (in the 1960s till today), have made it possible to control complex dynamical systems more accurately than the original flyball governor.

### A. Scope of this review

Owing to recent rising interest in intelligent control systems , it has been necessary to collect and classify these control systems and explain how their control techniques were developed. Despite the increase in the number of papers describing intelligent control techniques, understanding of the application of these techniques among the community of practice is somewhat sketchy. This is because those papers specifically deal only with research works which are aimed at achieving overall intelligent control using the techniques of fuzzy logic. This paper will attempt at classifying intelligent fuzzy control systems according to the control techniques used. There will be a discussion on how their intelligent control can be improved.

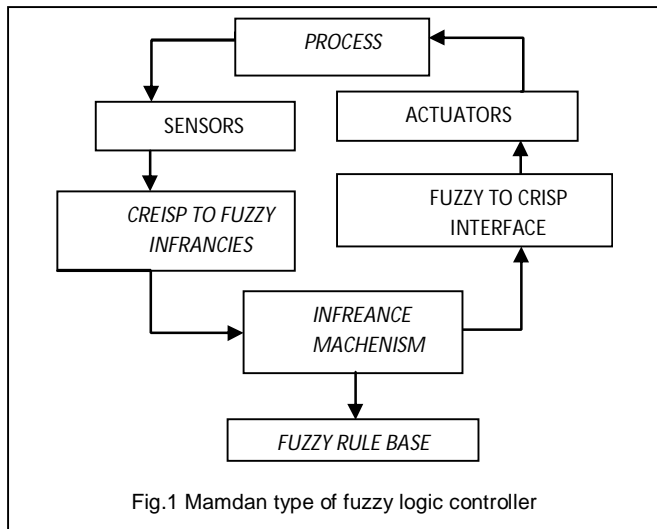
## 2 FUZZY LOGIC CONTROLLERS

There are two main types of fuzzy logic based controller [5-12]. The first is the madman type fuzzy logic controller which is adaptive and where the system to be controlled is not explicitly identified. The second is the Takagi-surgeon type fuzzy logic controller (FLC) which is indirectly adaptive and where the system to be controlled is identified using T-S fuzzy model . The controller is designed based on the identified model.

Rule base approach provides a useful framework for the definition of different methods of logic control [13-15]. Controller design using the rule based approach would assemble three component implementation phases. These are the knowledge acquisition phase, the model development phase and the model testing phase Examples of rule base

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structure can be found in Fuzzy PI/PD/PID controllers, Fuzzy Lyapunov controllers and Self organizing rule controllers.



Fuzzy rule base is normally run from statements containing fuzzy IF-THEN rules to derive the linguistic values for the intermediate and output linguistic variables

Let us denote the error and change of error as  $e$  and  $\dot{e}$  and control input as  $u$  respectively. Looking at the output response curve the following rules can be formed: PD, PID

- I. IF  $e$  is LE and  $\dot{e}$  is SE/ME. THEN  $u$  is LARGE
- II. IF  $e$  is ME and  $\dot{e}$  is ME. THEN  $u$  is MEDIUM
- III. IF  $e$  is SE and  $\dot{e}$  is LE. THEN  $u$  is NEGATIVE SMALL

Fuzzy PI/ PID controllers provide the rules base that gives the change in controller output, i.e.  $u(t+1) = u(t) + \Delta u$  where  $\Delta u$  can be found from the fuzzy rule base, and Fuzzy PD controller is the control input  $u$  is directly computed from the rule base. Fuzzy PI/PD/PID controller rule base is illustrated as follows:

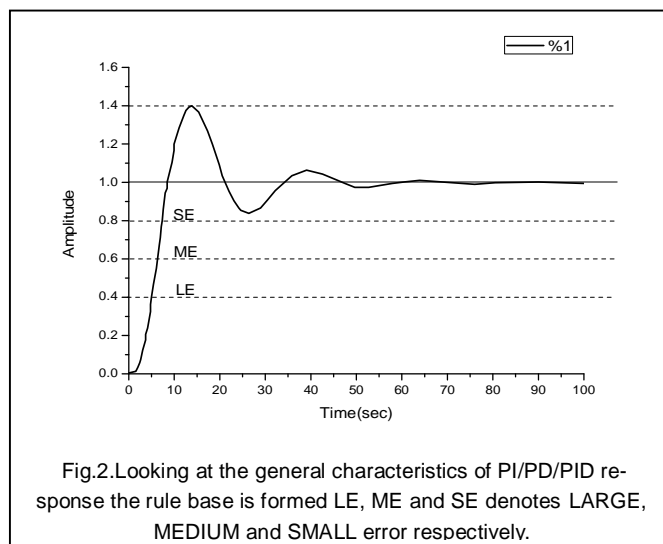
### 2. 1 Fuzzy PD/ PID/PI controller

In a general FLC the control objective is to design a fuzzy controller using information based on some physical intuition event if the exact system dynamic is not known but the main problem is constructing the rule base for the controller. In a typical mamdani type FLC, the rule base is obtained using the notion of classical PD, PI, or PID controller in Fuzzy Lyapunov control environment. The rule base is formed using the notion of Lyapunov Stability Theory for which  $V(x)$  represents a general single input single output nonlinear system. The value  $\dot{x} = f(x, u)$  is considered Lyapunov stable around the operating point  $x = 0$ .

There exists a continuously differentiable function  $V(x)$ , known as Lyapunov function where  $V(x)$  is positive definite

in the neighborhood of 0 and  $\dot{V}(x)$  is negative definite in the neighborhood of 0. Fuzzy Lyapunov controller, assumes prior knowledge of the system model. Under normal circumstances, only some partial knowledge about the system is known. Hence, it will be necessary to treat FLC as a classical case where a Lyapunove function candidate  $V$  is considered. The derivative of  $V$  (which is  $\dot{V}$ ) is then calculated and used to obtain the fuzzy rule base for the control input  $u$  as long as  $\dot{V}$  is negative definite. According to the rule base, a fuzzy controller  $u$  is obtained using general inference mechanism and defuzzification method. FLC structure. That is with the rule base it will be possible to formulate the resulting conditions in the form of rules in one of two possible representations. That is

- 1: IF  $x_1$  is  $A_1$  and /or  $x_2$  is  $A_2$  ...and/or  $x_n$  is  $A_n$  THEN  $u$  is  $B$ , where  $A_i$  and  $B$  are linguistic variables (e.g. large, small). Representation
- 2: IF  $x_1$  is  $A_1$  and /or  $x_2$  is  $A_2$  ...and/or  $x_n$  is  $A_n$  THEN  $u$  is  $f(x_1, x_2, \dots, x_n)$  where  $f(i)$  is a linear function.



### 2. 2 Fuzzy Lyapunov Controller

To understand the use of FLC, it is useful to see how it is used on a Single Linked Manipulator (SLM): which is normally considered as a dynamic model described by the equation

$$ml^2\ddot{\theta} + mgl\sin\theta = \tau$$

Where  $m = 1kg$ ,  $g = \frac{9.81kg}{meter^2}$ ,  $x_1 = \theta, x_2 = \dot{\theta}$  {afferent

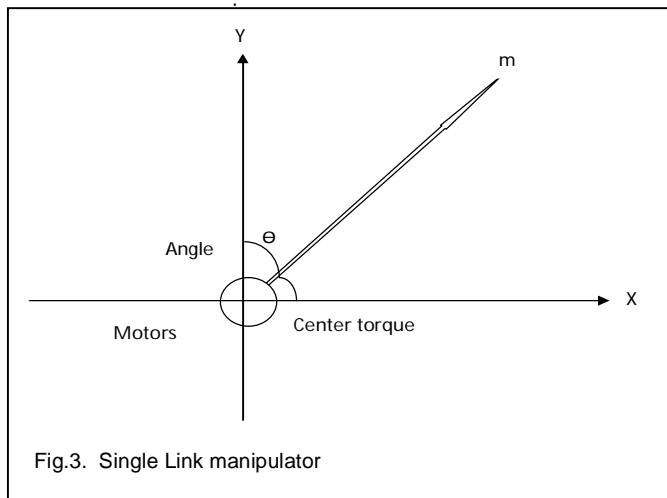
knowledge}  $\tau\alpha\ddot{\theta}, \tau\alpha\dot{\theta}$ .

Fuzzy Lyapunov controller:

SLM Without knowing the complete dynamics of the system, the following statements can be made: S-1 the relevant state variables are  $x_1 = \theta$  and  $x_2 = \dot{\theta}$ , S-2,  $\dot{x}$  is proportional to  $\tau$

Let us take a Lyapunov function candidate

$$V = 1/2(x_1^2 + x_2^2)$$



The time derivative of  $V$  is:  $\dot{V} = (x_1\dot{x}_1 + x_2\dot{x}_2)$

Where  $\dot{x}_1 = x_2, \dot{x}_2 = \tau$ , Using S-1 and S-2.  $\dot{V} = (x_1x_2 + x_2\tau)$

Find FLC rule such that  $\dot{V}$  qualitatively negative definite,

$\dot{V} = (x_1x_2 + x_2\tau)$ , Can make negative definite if the rule base is formed as follows:

IF  $x_1$  is negative AND  $x_2$  is negative, THEN  $\tau$  is positive big

IF  $x_1$  is positive AND  $x_2$  is positive, THEN  $\tau$  is negative big

IF  $x_1$  is negative AND  $x_2$  is positive, THEN  $\tau$  is zero

IF  $x_1$  is positive AND  $x_2$  is negative, THEN  $\tau$  is zero

### 2. 3 Takuge \_Sugeno Type Fuzzy logic controller

In general (FLC using TS fuzzy model) Takuge-sugeno type fuzzy logic controller is an example of indirect adaptive control. The main steps are identifying the nonlinear system in terms of T-S fuzzy model and designing the controller based on the identified T-S fuzzy model. There are three different control structures using T-S fuzzy model. The first controller is designed with common input matrix, the second linear controller is designed using robust control approach and the third controller is designed using LMI techniques.

Many important research work in this field have been carried out by several researchers. T. Takage and M. Sugeno approached Fuzzy identification from the condition of system when applied to modeling and control [17]. P.I. Kar, Prnam Karmer and L. Bahera performed identification and stabilization of nonlinear plants using Fuzzy neural networks [18]. They also suggested a workable variable gain controllers for nonlinear systems using T-S Fuzzy model [20]. S.H. Zak proposed stabilizing fuzzy system models using linear controllers [19]. K. Tanaka proposed a novel fuzzy-neural-linear control systems with desirable stability and stabilizability [7]. H. K. Lam, F.H.F. Leung and Peter K.S. Tam proposed a line-

ar matrix inequality approach for the control of Uncertain Fuzzy systems [21].

Type-1 and Type-2 FLSs (fuzzy logic system) have received increasing attention recently [22]. Type-2 (T2) FLSs have been applied in many engineering areas, demonstrating their ability to outperform Type-1 (T1) FLSs mainly in the presence of dynamic uncertainties [23]-[24]. The major difference between T1 and T2 FLSs is in the model of individual Fuzzy Sets (FSs) which use membership degrees that are themselves FSs. The most commonly used kind of T2 FLS is the Interval T2 (IT2) FLS, which uses interval membership degrees. Many researchers argue in favor of IT2 FLSs because of their potential to model and minimize the effects of dynamic uncertainties [25]. Typically, the performance of IT2 FLSs in various applications is compared to their T1 counterparts demonstrating improvements when noise and uncertainty are introduced into the system. Many researchers associate the geometrical properties of the interval centered with the uncertainty about the system's output [26,27]. whereas, a method for incorporating the experimentally measured input uncertainty into the design of the IT2 FLS was proposed [28]. Interval type-2 fuzzy logic controllers (IT2 FLCs) have been attracting great interests recently. Many reported results have shown that IT2 FLCs are better able to handle uncertainties than their type-1 (T1) counterparts [29], [30], [32], [33]. Wu and Tan [31], [32], [33] showed through both simulations and experiments that IT2 FLCs are better able to cope with modeling uncertainties, and hence IT2 FLCs optimized from simulations are more likely to perform well on the actual plant than T1 FLCs. Dongrui Wu, [34] explains that the two fundamental differences between IT2 and T1 FLCs are: 1) Addictiveness, meaning that the embedded T1 fuzzy sets used to compute the bounds of the type-reduced interval change as input changes; and, 2) Novelty, meaning that the upper and lower membership functions of the same IT2 fuzzy set may be used simultaneously in computing each bound of the type reduced interval. T1 FLCs do not have these properties; thus, a T1 FLC cannot implement the complex control surface of an IT2 FLC given the same rule base.

### 2. 4 Representation of a Nonlinear system

Let us consider a class of discrete nonlinear dynamical systems described by the vector equation

$$x(k+1) = f(x(k), u(k))$$

$$y(k) = h(y(k), u(k))$$

$x$  is a one-dimensional state vector,  $u$  is a p-dimensional input vector and  $y$  is an m-dimensional output vector. The above system can be effectively modeled by fuzzy merging of equivalent linear systems in different operating regions using Takuge\_sugeno (T-S) fuzzy model.

T-S Fuzzy model

A T-S Fuzzy model is composed of  $J$  rules where  $j^{th}$  rule have the following form.

Rule: IF  $x_1(k)$  is  $F_1^j$  AND ... AND  $x_n(k)$  is  $F_n^j$  THEN

$x(k+1) = A_j x(k) + B_j u(k)$ ,  $y(k) = C_j x(k) + D_j u(k)$ , Where  
 $x = [x_1, x_2, \dots, x_n]^T$   $j = 1, \dots, r$ . Given a current state vector  $x(k)$  and an input vector  $u(k)$ , the T-S fuzzy model inters  $x(k+1)$

$$\text{as } x(k+1) = \frac{\sum_{j=1}^r \mu_j (A_j x(k) + B_j u(k))}{\sum_{j=1}^r \mu_j}$$

$$y(k) = \frac{\sum_{j=1}^r \mu_j (C_j x(k) + D_j u(k))}{\sum_{j=1}^r \mu_j}$$

Where  $\mu_j = \prod_{i=1}^r \mu_j^i(x_i)$ ,  $\mu_j^i(x_i)$  is the membership function of the fuzzy term  $F_j^n$   $j = 1, 2, \dots, r$ .

The overall fuzzy system can be simplified into  
 $x(k+1) = \bar{A} x(k) + \bar{B} u(k)$   
 $y(k) = \bar{C} x(k) + \bar{D} u(k)$  the Nonlinear system  $x(k+1) = f(x(k), u(k))$ ,  $y(k) = h(x(k), u(k))$  where

$$\bar{A} = \sum_{j=1}^r \delta_j A_j, \bar{B} = \sum_{j=1}^r \delta_j B_j, \bar{C} = \sum_{j=1}^r \delta_j C_j, \bar{D} = \sum_{j=1}^r \delta_j D_j$$

$$\delta_j = \frac{\mu_j}{\sum_{j=1}^r \mu_j} \quad \sum_{j=1}^r \delta_j = 1$$

The overall system is nonlinear since  $\bar{A}$  is a function of  $\delta_j$  and  $\delta_j$  is a function of  $x(k)$

### 2. 5 Continuous time T-S fuzzy model

“Continuous time counterpart of the overall fuzzy system is  $\dot{x} = \bar{A} x + \bar{B} u$ ,  $y = \bar{C} x + \bar{D} u$  where

$$\dot{x} = \sum_{j=1}^r \delta_j (A_j x + B_j u), \bar{A} = \sum_{j=1}^r \delta_j A_j,$$

$$\bar{B} = \sum_{j=1}^r \delta_j B_j, \bar{C} = \sum_{j=1}^r \delta_j C_j, \bar{D} = \sum_{j=1}^r \delta_j D_j$$

Identifying the linear model parameters. The parameters  $A_j$  and  $B_j$  can be found

- By linearizing the nonlinear system dynamics

Example: suppose the nonlinear dynamic is  $\dot{x} = F(x, u) = (x + x^2) + u$  the sum is to find A and B such that in  $u$  neighborhood of an operating point  $F(x, u) = (Ax + Bu)$

- When  $x_0 = 0$ ,  $A = \frac{\partial f}{\partial x}$ ,  $B = \frac{\partial f}{\partial u}$  (Using Taylor's series expansion)
- When  $x_0 \neq 0$ , A and B can be found out for affine type systems i.e.  $\dot{x} = f(x) + g(x)u$  in that case, if  $a_i^T$  denote the  $i$ th row of A.

Then  $a^2 = \frac{\partial f}{\partial x} + \frac{\text{linear } \partial f}{\sum \partial u}$ ,  $B = g(x, u)$  [reference system and control .H.Zak]. Thus two rules of T-S fuzzy model parameters are  $B_j$

- R1: If  $x = 0$ ,  $\dot{x} = x + u$ ,  $A_1 = 1$ ,  $B_1 = 1$
- R1: If  $x = 1$ ,  $\dot{x} = 2x + u$ ,  $A_2 = 2$ ,  $B_2 = 1$

The linear model parameters  $A_j, s'$  and  $B_j, s'$  also be identification

- From the input-output data of the system using a fuzzy neural network (FNN)
- When using a FNN the elements of  $A_j$  and  $B_j$  are the weights of the neural network
- Least square cost function is used to find the proper weights.
- Weights are updated using the standard gradient descent algorithm.

T-S fuzzy model with a common input matrix

- Discrete time T-S fuzzy model  
 $x(k+1) = \bar{A} x + \bar{B} u(k)$
- Continuous time T-S fuzzy model  $\dot{x} = \bar{A} x + \bar{B} u$

Where  $\bar{A} = \sum_{j=1}^r \delta_j A_j$ ,  $\bar{B} = \sum_{j=1}^r \delta_j B_j$  the system will have a common input matrix when  $B_j = B_j$  is a constant matrix. Utility of common input matrix. Suppose we design individual linear controller for individual subsystems. This control action corresponding to  $j$ th subsystems is denoted by  $u_j(k)$ . If all linear subsystems have a common input matrix B than an overall control input of the from  $u(k) = \sum_{j=1}^r \delta_j u_j(k)$  will carry than the individual subsystem are excited by inspective control inputs.

Controller design with common input matrix Many researchers have made the system stable by using input data matrix which can be illustrated as follows:

Suppose the individual control input has a form  $u_j(k) = -k_j x(k)$  for discrete time. T-S fuzzy models which

- the overall system can be made stable if
- There exists a common input matrix B for all subsystems
- The individual gain matrices  $K_j$  is such that  $A'_j = A_j - B_j K_j$  have singular values less than unity

For continuous T-S fuzzy model, the overall system can be made stable if

- There exists a common input matrix B for all subsystems
- The individual gain matrices  $K_j$  are designed such that  $\frac{1}{2}(A_j'^T + A_j')$  have action part's stability signal values

, where  $A'_j = A_j - B_j K_j$  where,  $u_j = -k_j x_j$  for all system controller  $u(k) = \sum_{j=1}^r \delta_j u_j(k)$ .

The system's stability is dependent on Hrmashan part  $\{\frac{1}{2}(A'^T_j + A'_j), A'_j\}$

For both continuous and discrete time systems the overall system can be made stable if

- There exists a common input matrix B for all subsystems.
- The individual gain matrices  $K_j$ 's are designed such that  $A'_j = A_j - B_j K_j$ 's and symmetric [17,18]

Many fuzzy clustering studies have been conducted based on dissimilar and similar relationships between plants. Subsequently rules were extracted utilizing fuzzy clustering method [35-37]. Permanent magnet synchronous motors have been used as servo motors under vector control techniques and various control methods have been applied to (permanent magnet synchronous motor)PMSM motors [38]-[39]. There are two types of PMSM. The first one is Surface PMSM(SPMSM) and the other is interior PMSM(IPMSM(interior permanent magnet synchronous motor)). In the control of SPMSM, the system can be considered as linear with the d-axis current controlled to be zero. In this case, SPMSM can be modeled as DC motors [40][41]. In the T-S fuzzy identification of IPMSM, a set of local dynamic linear models will be provided with high accuracy. T-S fuzzy identification can provide an accurate system description with membership functions and a series of linear dynamic equations [42 -44]. One of the best control method for nonlinear system is T-S fuzzy control. In the actual IPMSM, it is very difficult to get the parameters of IPMSM. An efficient method is used to derive T-S fuzzy model of IPMSM using the data from the actual IPMSM.

**2. 6 Linear controller using robust control approach**

TS fuzzy model is normally expressed in terms of a single linear plant while the rest of the linear models are expressed as a disturbances to this. The norm bound on the disturbance is computed based on the norm bound of the controller which is designed to make the overall system Lyapunov stable.

The T-S model is expressed in terms of r fuzzy rules:  
 Rule i: if xi (t) is  $F_i^n$  AND .....AND xn(t)is  $F_i^n$  THEN

$$x(t) = A_i x(t) + B_i u(t) \quad F_j^n \quad j=1,2,\dots,n \text{ is the } j^{th} \text{ fuzzy set of}$$

the  $i^{th}$  rule . Let  $\mu_j = \prod_{j=1}^r \mu_j^j(x_j)$ . Where  $\mu_j^j(x_j)$  is the membership function of the fuzzy set

$F_i^n \quad j=1,2,\dots,r$  the overall system is

$$x(t) = \sum_{j=1}^r \delta_j (A_j r(t) + B_j u(t)) \text{ where}$$

$$\delta_j = \frac{\mu_j}{\sum_{j=1}^r \mu_j} \sum_{k=1}^r \delta_j = 1 \cdot$$

The T-S model linear plant with nonlinear disturbance

The T-S fuzzy model can be rewritten as  $\dot{x}(t) = Ax(t) + Bu(t) + \sum_{j=1}^r \delta_j (A_j - A)x(t) + \sum_{j=1}^r \delta_j (B_j - B)u(t)$   
 $Ax(t) + Bu(t) + F(x(t), u(t))$  where  $Ax(t) + Bu(t)$  is the linear system and  $F(x(t) + u(t))$

is the nonlinear disturbance given by  $F(x(t), u(t)) = f(x(t) + Bh1(x(t)) + Bh2(u(t)))$

Computing the norm bounds of f, h1 and h2 controllers are designed to make the T-S fuzzy model Lyapunov stable. S;H.Zak(1999) and( Prem Kumar PI.Kar and I Behera(2006)) [45-46] have proposed several applications of T-S Fuzzy model when it is Lyapunov stable. For a control system, the fundamental requirement is stability. While numerous high efficient converters have been constructed for various applications, there have been continuing efforts devoted to the stability analysis of power electronic converters [47]. A nonlinear system approach was developed for analysis and design of power electronic converters [48], where the DC-DC converter was modeled as a differential equation with a bilinear term and input saturation (the hard limit on the duty cycle). Another non linear system approach uses boost, buck-boost converters which have been used to condition the power supplied by photovoltaic batteries [49]. Of late, different control approaches have been applied to space vector modulated direct torque controlled IPMSM (interior permanent magnet synchronous motor) drives in the search for more desirable drive performances in terms of both steady state and transient responses [50-55]. As far as intelligent based direct torque control schemes are concerned, some Fuzzy controlled DTCs [50] and Neuro-Fuzzy controlled DTCs [51] have been reported. Despite a more robust performance especially in the case of ill-defined and uncertain systems, the fuzzy controller still encounters the lack of a systematic method for tuning. Such a difficulty was resolved by adding the learning capability of neural networks, but the performance in the presence of disturbances, parameters variation and system uncertainties was not optimal. Some other researchers proposed the direct torque control schemes based on adaptive controllers such as input-output feedback linearization [56] and adaptive back-stepping [57]. Although, a much smoother steady state performance were obtained, the transient drive response was not satisfactory which was mainly due to the sluggish estimation of motor parameters through the generated adaptation laws. In addition, all adaptive based DTCs demand a precise motor model, thus some modeled dynamics and disturbances could considerably deteriorate the drive performance.

**2. 7 Fuzzy controller using LMI technique**

In this control strategy the stability of the closed loop system is guaranteed by finding a common Lyapunov function for all the local linear models. This can be expressed in the form of a Linear Matrix Inequality (LMI). A stable fuzzy controller can be designed by solving the LMI's. Let us consider the follow-

ing T-S Fuzzy model which is locally described by  $i$ th rule. According to  $i$ th rule, if  $x_1(t)$  is F1 and  $x_2(t)$  is F2 and  $x_n(t)$  is  $F_n^r$  THEN  $\dot{x}(t) = A_i x(t) + B_i u(t)$

$$t=1,2,\dots,r. \quad u(t) = -k_i x(t) \quad t=1,2,\dots,r$$

In addition, as described earlier, given a current state vector  $x(t)$  and an input  $u(t)$  the T-S model infers that the value of  $\dot{x}(t)$  can change as follows:

$$\dot{x}(t) = \sum_{j=1}^r \delta_j (A_j x(t) + B_j u(t)). \text{ Where } \delta_j \text{ have been defined earlier.}$$

The final output of the fuzzy controller is  $u(t) = \sum_{j=1}^r \delta_j K_j x(t)$  where  $u_i = -k_i x_i(t)$ , for individual closed loop. The subsystem becomes

$$\dot{x}(t) = \sum_{j=1}^r \delta_j (A_j x(t) - B_j \sum_{j=1}^r \delta_j K_j x(t)). \text{ After simplification } \dot{x} \text{ can be written as}$$

$$\dot{x}(t) = \sum_{j=1}^r \delta_j^2 H_j x(t) + 2 \sum_{j=1}^r \delta_j \delta_i \left\{ \frac{H_{ij} + H_{ji}}{2} \right\} x(t)$$

$$\text{where } H_{ij} = A_i - B_i K_j.$$

Consider a Lyapunov function candidate,  $V = x^T P_x$  and  $\dot{V} = \dot{x}^T P_x + x^T P_x$ , giving

$$\dot{x}(t) = \sum_{j=1}^r \delta_j^2 H_j x(t) + 2 \sum_{j=1}^r \delta_j \delta_i \left\{ \frac{H_{ij} + H_{ji}}{2} \right\} x(t)$$

where we can write

$$\dot{v} = \sum_{j=1}^r \delta_j^2 x^T H_j^T P_x + 2 \sum_{j=1}^r \delta_j \delta_i x^T \left\{ \frac{H_{ij} + H_{ji}}{2} \right\} P_x$$

$$+ x^T P \sum_{j=1}^r \delta_j^2 H_j x + 2 x^T P \sum_{j=1}^r \delta_j \delta_i \left\{ \frac{H_{ij} + H_{ji}}{2} \right\} x$$

$$\dot{v} = \sum_{j=1}^r \delta_j^2 x^T (H_j^T P_x + P H_j) X$$

$$+ 2 \sum_{j=1}^r \delta_j \delta_i x^T \left( \frac{H_{ij} + H_{ji}}{2} \right)^T P_x + P \left( \frac{H_{ij} + H_{ji}}{2} \right) x$$

Since  $\delta_j$  is a position quantity,  $\dot{v}$  will be negative definite if  $H_j^T P_x + P H_j < 0$  for  $r=1,\dots,r$  LMI eq.

$$\left( \frac{H_{ij} + H_{ji}}{2} \right)^T P + P \left( \frac{H_{ij} + H_{ji}}{2} \right) \leq 0, i < j, \delta_j \delta_i \neq 0, \dots, \text{LMI eq.}$$

The above expressions are basic stability conditions. The controller parameter  $K_j$  is hidden in that expression. The above can be further re-expressed in different suitable forms and the controller parameter  $K_j$  can then be obtained by solving those equations stated earlier.

Thus  $u_j = k_j x_j, u = \sum_{j=1}^r \delta_j u_j$  For discrete time case the equilibrium point of the overall fuzzy system is generally asymptotically stable if there exists a common positive definite

matrix P such that  $H_i^T P_x H_{ij} - P < 0$  for  $r=1,\dots,r$ .

LMI eq. is normally expressed (for discrete as well as for continuous time) as  $\left( \frac{H_{ij} + H_{ji}}{2} \right)^T P + P \left( \frac{H_{ij} + H_{ji}}{2} \right) \leq 0, i < j, \delta_j \delta_i \neq 0$

There are various algorithms available in literature { H.O.Wang K.Tanaka and M.F.Griffen (1996), E.Kian and D.Kim (2001), H.K.Larn and F.H.F.Leung and Peter K.S.Tam.A.(2002), K.Tanaka, T.Ievade and H.O.Wang(May 1998.), E.Kain and H.Lee(Oct 2000), C.H Fang Y-S Liui.S-W Kau. I.Hong and C-H Lee(June 2006) and D. Giaouris, S. Banerjee, B. Zahawi, and V. Pickert, (May 2008) [57-63]}. on how to get the controller parameters by solving the above LMI's. Floquet theory has also been used to study the stability of system trajectories by deriving the absolute value of the eigenvalues of the monodromy matrix (i.e., the so-called Floquet multipliers of the system) [64]-[65]. The implementation of these strategies is still not widely adopted since they are vulnerable to noise and suffer from a high-computation-time requirement [66]. The TS fuzzy approach (model based or non model based) has already been applied to control power electronic converters [68], [67]. One of the main drawbacks of these previous attempts is the derivation of the fuzzy model from the average dynamical model of the converter, thus ignoring all converter fast-scale instabilities as outlined previously.

### 3 CONCLUSION

The research on the intelligent system fuzzy was reviewed with a focus on the historical development of new technical and strategies to improve the activity of the intelligent control systems. As described the above, in the search for intelligent control, significant effort has been devoted to the development of new control technique and active sites on intelligent, as well as elucidating the major methods. This has led to significant progress in the field of an intelligent control systems fuzzy, especially in least years. However, the development of an intelligent control with fuzzy is still needed. The drawback of both general and Lyapunov like Mamdani type (fuzzy logic controller) FLC is that the parameters associated with the FLC are heuristically updated. In general, Takugeno type fuzzy logic controller is an example of indirect adaptive control. The main steps are identifying the nonlinear system in terms of T-S fuzzy model and designing the controller based on the identified T-S fuzzy model. There are three different control approaches using a T-S fuzzy model the first controller design with common input matrix, the second linear controllers using robust control approach and the third controller design using LMI techniques.

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