

MODELING OF GRAPHENE NANORIBBON FIELD EFFECT TRANSISTOR

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MODELING OF GRAPHENE NANORIBBON FIELD EFFECT TRANSISTOR

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requirements for the award of the degree of
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Dedicated to Emam Zaman and my beloved family

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ABSTRACT

The scaling of Field Effect Transistor (FET) at nanoscale assures better performance of the device. The phenomenon of downsizing the device dimensions has led to challenges such as short channel effects, leakage current, interconnect difficulties, high power consumption and quantum effects. Therefore, new materials and device structures are needed as alternatives to overcome these challenges. In this research, an analytical model for Trilayer (ABA-stacked) Graphene Nanoribbon carrier statistics based on quantum confinement effect is presented. To this end, density of states, carrier concentration and ballistic conductance of Trilayer Graphene Nanoribbon (TGN) as an FET channel are modeled. Besides that, scaling behaviors of p-n junction, Homo junction, Schottky-barrier diode and Schottky-barrier FET based on the Graphene Nanoribbon application are analytically studied. This is demonstrated in the proposed structure of TGN Schottky-barrier FET that exhibits negligible short channel effects, improved on current, pragmatic threshold voltage, very good subthreshold slope, and fast transient between on-off states to meet the International Technology Roadmap for Semiconductors (ITRS) near-term guidelines. Therefore, the proposed model is suitable for a high speed switching application because the value of subthreshold slope for the proposed transistor is less than the ideal value of 60 mV/decade. A small value of subthreshold slope denotes a small change in the input bias which can modulate the output current and would lead to less power consumption. Finally, an analytical modeling of Graphene-based NO₂ gas sensor is proposed. MATLAB software was used to implement the numerical methods for modeling and data analysis. Observations of the presented models showed acceptable agreement with the published data.

ABSTRAK

Penskalaan Transistor Kesan Medan (FET) pada tahap nanometer menjamin prestasi yang lebih baik untuk peranti berkenaan. Fenomena pengecilan dimensi peranti membawa beberapa cabaran seperti kesan saluran pendek, arus kebocoran, kesukaran penyambungan, penggunaan kuasa yang tinggi dan kesan kuantum. Oleh itu bahan-bahan baru dan struktur peranti diperlukan sebagai alternatif untuk mengatasi cabaran ini. Dalam penyelidikan ini model analisis statistik pembawa tiga lapisan (susunan ABA) Nanoribbon Grafin berdasarkan kesan berpantang kuantum digunakan. Untuk maksud ini ketumpatan keadaan, kepekatan pembawa dan kealiran balistik Nanoribbon Grafin tiga lapisan (TGN) sebagai saluran FET dimodelkan. Selain itu perilaku berskala simpang p-n, simpang Homo, diod halangan-Schottky dan FET halangan-Schottky berdasarkan aplikasi Nanoribbon Grafin dianalisis secara analitikal. Ini menunjukkan bahawa struktur cadangan TGN FET halangan-Schottky mempamerkan kesan saluran pendek yang boleh diabaikan, memperbaiki arus voltan ambang pragmatik, sub-ambang cerun yang sangat baik, cepat bertukar antara keadaan hidup-mati untuk memenuhi garis panduan *International Technology Roadmap for Semiconductors (ITRS)* dalam jangka masa terdekat. Dengan itu model yang dicadangkan sesuai untuk aplikasi pensuisan berkelajuan tinggi kerana nilai cerun sub-ambang untuk transistor yang dicadangkan adalah kurang daripada nilai ideal 60 mV/dekad. Satu nilai yang kecil cerun sub-ambang menandakan perubahan kecil pincangan input yang boleh memodulasi output semasa dan mengurangkan penggunaan kuasa. Akhirnya, pemodelan analitikal Grafin berasaskan pengesan gas NO₂ telah dicadangkan. Perisian MATLAB digunakan untuk melaksanakan kaedah berangka untuk pemodelan dan penganalisan data. Pemerhatian terhadap model yang dibentangkan menunjukkan persamaan yang boleh diterima dengan data yang diterbitkan.

TABLE OF CONTENTS

CHAPTER	TITLE	PAGE
	DECLARATION	ii
	DEDICATION	iii
	ACKNOWLEDGEMENT	iv
	ABSTRACT	v
	ABSTRAK	vi
	TABLE OF CONTENTS	vii
	LIST OF TABLES	x
	LIST OF FIGURES	xi
	LIST OF SYMBOLS	xiv
	LIST OF ABBREVIATIONS	xvii
	LIST OF APPENDICES	xix
1	INTRODUCTION	1
	1.1 Background Study	1
	1.2 Problem Statement	3
	1.3 Research Objective	6
	1.4 Scope of Study	6
	1.5 Research Contributions	7
	1.6 Thesis Organization	8
2	LITERATURE REVIEW	10
	2.1 Introduction	10
	2.2 Band Structure of Graphene Nanoribbon	12
	2.3 Basic Geometries of Graphene Nanoribbon	16

2.4	Monolayer Graphene Nanoribbon	19
	2.4.1 Monolayer Graphene Nanoribbon P-N Junction	20
	2.4.2 Monolayer Graphene Nanoribbon Homo- junction	22
2.5	Bilayer Graphene Nanoribbon	23
	2.5.1 Bilayer Graphene Nanoribbon Schottky Diode	24
2.6	Trilayer Graphene Nanoribbon	25
	2.6.1 Configuration of Trilayer Graphene Nanoribbon	26
	2.6.2 ABA-Stacked Trilayer Graphene Nanoribbon	27
	2.6.3 Band Structure of TGN with ABA Staching	28
	2.6.4 Trilayer Graphene Nanoribbon Schottky- Barrier FET	29
2.7	Monolayer Graphene FET based Gas Sensors	30
2.8	Summary	33
3	RESEARCH METHODOLOGY	34
	3.1 Introduction	34
	3.2 Device Modeling	34
	3.3 Research Framework	35
	3.4 Carrier Transport Models Classification	39
	3.5 Research Activities	41
	3.6 Summary	42
4	MONOLAYER, BILAYER AND TRILAYER GRAPHENE NANORIBBON FET ANALYTICAL MODELS	43
	4.1 Introduction	43
	4.2 Built-in Potential Barrier of Monolayer GNR P-N Junction	44

4.2.1	Space Charge Width Junction Capacitance in Monolayer GNR P-N Junction	45
4.3	Proposed Model of Monolayer GNR Homo- junction	48
4.3.1	Homo-junction Configuration	51
4.4	Proposed Model of BGN Schottky Diode	54
4.4.1	Current-Voltage Characteristic of BGN Schottky Diode	55
4.5	Proposed Model of ABA-stacked TGN	63
4.5.1	Carrier Concentration of ABA-stacked TGN in Degenerate and Non-Degenerate Regimes	66
4.5.2	Conductance Model of ABA-stacked TGN	69
4.5.3	Proposed Model of ABA-stacked TGN Schottky-Barrier FET	71
4.5.3.1	Current-Voltage Characteristic of ABA-stacked TGN SB FET	74
4.6	Summary	85
5	GRAPHENE FET BASED GAS SENSOR APPLICATION	87
5.1	Introduction	87
5.2	Proposed Model of Monolayer Graphene-based NO ₂ Sensor	88
5.3	Summary	96
6	CONCLUSION AND FUTURE WORK	97
6.1	Introduction	97
6.2	Conclusions	98
6.3	Future Work	100
	REFERENCES	101
	Appendices A-F	116-136

LIST OF TABLES

TABLE NO	TITLE	PAGE
3.1	Relation between current-voltage characteristic of FET based device and analytical models	37
3.2	Classification of carrier transport models for FET based device according to the channel length.	40
4.1	Subthreshold slope of TGN SB FET at different values of V_{DS} .	84

LIST OF FIGURES

FIGURE NO	TITLE	PAGE
2.1	Schematic of GNR transistor.	12
2.2	lattice of graphene.	13
2.3	Arrangements of GNR (a) armchair (b) zigzag.	17
2.4	The steps of unzipping the CNTs to form GNRs.	19
2.5	Doping in GNR p-n junction.	21
2.6	Structure of BGN with AB stacking.	23
2.7	TGN as a 1D material with quantum confinement effect on two cartesian directions.	25
2.8	Atomic structures of TGN with (a) ABA (Bernal) stacking and (b) ABC (rhombohedral) stacking.	26
2.9	ABA-stacked TGN.	27
3.1	Research operational framework.	36
4.1	Ideal capacitance versus applied voltage of (a) Si p-n junction (b) monolayer GNR p-n junction capacitor.	47
4.2	The band structure of monolayer GNR.	50
4.3	The proposed schematic of GNR schottky contact.	51
4.4	Numerical solution on the current of GNR homo-junction.	53
4.5	Comparison between presented model and extracted data from graphene–silicon schottky contact.	53
4.6	Comparison between GNR schottky barrier with silicon schottky diode and silicon p-n junction diode.	54
4.7	Schematic of BGN schottky contact.	55
4.8	The energy band structure of BGN near the Fermi level.	56

4.9	Rectification I-V characteristic of BGN schottky diode ($V_{\text{turn-on}} = 0.89\text{V}$).	59
4.10	I-V characteristic of BGN schottky diode at different temperatures.	60
4.11	I-V characteristic of BGN schottky diode at various widths.	60
4.12	Turn-on voltage versus width of BGN schottky diode ($T = 200\text{ °K}$).	61
4.13	Comparison between BGN schottky diode with silicon schottky diode and silicon p-n junction diode.	62
4.14	Comparison between the proposed model with graphene- silicon schottky diode and monolayer GNR homo-junction contact.	62
4.15	Band structure of ABA-stacked TGN with overlap biased ($V = 0.3\text{ V}$).	64
4.16	The DOS of the TGN with ABA stacking.	65
4.17	The effect of applied voltage on the curvature of the E-K graph (effective mass) in ABA-stacked TGN.	66
4.18	ABA-stacked TGN carrier concentration as a function of normalized Fermi energy.	67
4.19	Comparison between the presented model and non- degenerate approximation.	68
4.20	Comparison between the presented model, non-degenerate and degenerate approximations.	69
4.21	Conductance of TGN with ABA stacking at different temperatures.	71
4.22	Schematic of TGN SB contact.	71
4.23	Schematic representation of TGN SB FET.	72
4.24	Simulated I_D (μA) versus V_{DS} (V) plots of TGN SB FET [$L = 25\text{ nm}$, $V_{\text{GS}} = 0.5\text{ V}$].	75
4.25	I_D (μA) - V_{DS} (V) characteristic of TGN SB FET at different values of V_{GS} for $L = 100\text{ nm}$.	76

4.26	Impact of the channel length scaling on the transfer characteristic for $V_{GS}=0.5$ V.	77
4.27	The current-voltage characteristic of the proposed model and MOSFET with SiO_2 gate insulator, ($V_{GS}=0.5$ V).	79
4.28	Comparison between the proposed model with a TGN MOSFET with an ionic liquid gate, $C_{ins} \gg C_q$ ($V_{GS}=0.5$ V).	80
4.29	Comparison between the proposed model with a TGN MOSFET with a 3nm ZrO_2 wrap around gate, $C_{ins} \approx C_q$ ($V_{GS}=0.37$ V).	81
4.30	Comparison between the proposed model with a TGN MOSFET with a 3nm ZrO_2 wrap around gate, $C_{ins} \approx C_q$ ($V_{GS}=0.38$ V).	81
4.31	Subthreshold regime of TGN SB FET at different values of V_{DS} for $L=25$ nm.	83
4.32	$I_D(\mu A) - V_{GS}$ (V) characteristic of TGN SB FET at different values of V_{DS} .	84
5.1	Graphene sensor exposed to NO_2 gas.	88
5.2	The energy band structure of small-width graphene.	89
5.3	Spin-polarized DOS of the small-width graphene super cells with adsorbed NO_2 (α is the factor of NO_2 concentration).	93
5.4	The $I_D - V_{DS}$ characteristic of the proposed model and NO_2 gas sensor when gas concentration is 100 ppm.	94
5.5	The $I_D - V_{DS}$ characteristic of the proposed model and NO_2 gas sensor when gas concentration is 500 ppm.	94
5.6	Comparison between the transfer characteristic ($I_D - V_{DS}$) of the presented model with experimental extracted data for two different concentrations of complementary NO_2 .	95

LIST OF SYMBOLS

a_1, a_2	-	Vectors of Lattice
a_{c-c}	-	Carbon-Carbon (C-C) bond length
C	-	Chiral vector
$D(E)$	-	Density of State
E_c	-	Conduction band
E_f	-	Fermi energy level
E_g	-	Band gap energy
E_v	-	Valence band
G	-	Conductance
h	-	Plank's Constant
k	-	Wave Vector
k_B	-	Boltzmann's Constant
L	-	Length of the nanoribbon
m^*	-	Effective mass
N	-	Number of dimer lines
N_c	-	Competition Degree
η_f	-	Normalized Fermi energy
Q	-	Charge
t	-	C-C bonding Energy
T	-	Temperature
v_F	-	Fermi velocity
eV	-	Electron-volt
$f(E)$	-	Fermi-Dirac integral
$1D$	-	1-Dimensional
$2D$	-	2-Dimensional
n	-	Free electrons concentration

p	-	Free holes concentration
N_A	-	Impurity (accepter) concentration in p-type silicon
N_B	-	Impurity concentration in (n or p-type) bulk silicon
N_D	-	Impurity (donor) concentration in n-type silicon
L_g	-	Channel length
L_{eff}	-	Effective channel length
μ_n	-	Electron mobility in the channel
μ_p	-	Hole mobility in the channel
μ_{eff}	-	Effective channel mobility
λ	-	Channel length modulation factor
ϵ	-	Dielectric constant
ϵ_s	-	Permittivity of silicon
α	-	Body factor term
γ	-	Body-effect coefficient
t_{ox}	-	Oxide thickness
W	-	Effective or electrical channel width
W_d	-	Channel-depletion width
W_j	-	Junction width
X_j	-	Junction depth
C_{ox}	-	Capacitance per unit area
AC	-	Alternating current
DC	-	Direct current
V_D	-	Drain voltage
V_{DD}	-	Power supply voltage
V_{DS}	-	Drain to source voltage
V_{Dsat}	-	Drain saturation voltage
V_G	-	Gate voltage
V_{GS}	-	Gate to source voltage
V_{PT}	-	Punch-through voltage
V_{SB}	-	Source to bulk voltage
V_T	-	Threshold Voltage
V_{T0}	-	Threshold voltage for $V_{SB}=0$

ΔV_{DS}	-	Change in the drain-source voltage
ΔV_T	-	Change in the threshold voltage
S_T	-	Subthreshold swing
I_D	-	Drain current in a MOSFET
I_{DS}	-	Drain to source current
I_{OFF}	-	Off-state current or leakage current
I_{ON}	-	On-state current or drive current

LIST OF ABBREVIATIONS

<i>BGN</i>	-	Bilayer Graphene Nanoribbon
<i>BTE</i>	-	Boltzmann Transport Equation
<i>CAD</i>	-	Computer Aided Design
<i>CLM</i>	-	Channel Length Modulation
<i>CMOS</i>	-	Complementary Metal Oxide Semiconductor
<i>CNT</i>	-	Carbon Nanotube
<i>C-V</i>	-	Capacitance-Voltage Characteristics
<i>DGFET</i>	-	Double-gate MOSFET
<i>DIBL</i>	-	Drain induced barrier lowering
<i>DOS</i>	-	Density Of State
<i>DSOI</i>	-	Drain and Source on Insulator
<i>ECAD</i>	-	Electrical Computer Aided Design
<i>FDI</i>	-	Fermi-Dirac integral
<i>FET</i>	-	Field Effect Transistor
<i>GNR</i>	-	Graphene Nanoribbon
<i>GNERFET</i>	-	Graphene Nanoribbon Field Effect Transistor
<i>GIDL</i>	-	Gate Induced Drain Leakage
<i>HBT</i>	-	Heterojunction Bipolar Transistor
<i>HDD</i>	-	Highly Doped Drain
<i>ITRS</i>	-	International Technology Roadmap for Semiconductors
<i>I-V</i>	-	Current-Voltage Characteristics
<i>LDD</i>	-	Lightly Doped Drain
<i>LOCOS</i>	-	Local Oxidation of Silicon
<i>MOSFETs</i>	-	Metal Oxide Semiconductor Field Effect Transistor
<i>ND</i>	-	Non-degenerate
<i>NMOS</i>	-	n-channel MOSFET

<i>PECVD</i>	-	Plasma Enhanced Chemical Vapor Deposition
<i>PMOS</i>	-	p-channel MOSFET
<i>RIE</i>	-	Reactive Ion Etching
<i>SB</i>	-	Schottky-barrier
<i>SCE</i>	-	Short Channel Effect
<i>S/D</i>	-	Source and Drain
<i>SEM</i>	-	Scanning Electron Microscopy
<i>SGFET</i>	-	Single-gate MOSFET
<i>SOI</i>		Silicon On Insulator
<i>TCAD</i>		Technology Computer Aided Design
<i>TED</i>	-	Transient Enhanced Diffusion
<i>TEM</i>	-	Tunneling Effect Microscopy
<i>TGN</i>	-	Trilayer Graphene Nanoribbon
<i>VLSI</i>	-	Very Large Scale Integrated

LIST OF APPENDICES

APPENDIX	TITLE	PAGE
A	Quasi Three-Dimensional Model	116
B	Quasi Two-Dimensional Model	120
C	Quasi One-Dimensional Model	123
D	Degenerate Intrinsic Velocity	127
E	Gamma Function	130
F	Publications	131

CHAPTER 1

INTRODUCTION

1.1 Background Study

The approaching scaling of Field Effect Transistors (FETs) in nanometer scale assures the smaller dimension, low-power consumption, very large computing power, low energy delay product and high density as well as high speed in processor. The downscaling phenomena of device dimensions lead to some problems such as short-channel effects, gate-leakage current, and so forth. Therefore, novel device structures and materials like graphene, carbon nanotube (CNT), nano scroll, and nano wire are explored for experimentation; more challenges as well as opportunities emerge to expand the vision encountered in the International Technology Roadmap for Semiconductors (ITRS).

According to the Moore's law, the number of transistors per square inch on integrated circuits doubles approximately every two years (Gordon, 1965). It is noteworthy that the capabilities of many digital electronic devices such as processing speed, memory capacity, sensors and even the number and size of pixels in digital cameras are strongly linked to Moore's law. All of these are improving exponentially rates as well, which has dramatically enhanced the impact of digital electronics in nearly every segment of the world economy. In future, nanoelectronic devices will be scaled down to nanoscale size to meet the Moore's law, and therefore, will operate in the degenerate limit, which makes the degenerate approximation more dominant in the future nanoscale device modeling.

Diamond and graphite are the materials which are extensively investigated in nanoelectronic. Since diamond's unusual bonding attributes makes it hard to be naturally created, the lately discovered allotropes like fullerenes and nanotubes are taken into consideration closely by scientists researching in the fields of biology, chemistry, physics and material science (Gogotsi *et al.*, 1999; Irifune *et al.*, 2003). All the structural studies on graphite, fullerenes and nanotubes start with graphene. Graphene is the name given to a single layer of carbon atoms in form of honeycomb lattice which is the basic structure of the graphite based materials such as nanotubes and fullerenes contain pentagons (Entani *et al.*, 2010; Zhang *et al.*, 2010b; Castro Neto *et al.*, 2009b).

Due to its unique structure, excellent electronics (McEuen *et al.*, 2002), optical (Misewich *et al.*, 2003; Chen *et al.*, 2005) and physical properties, graphene nanoribbon (GNR) has recently been considered for new device applications in the future. Consequently, prototype structures indicating excellent performance for transistors (Javey *et al.*, 2003), interconnects (Li *et al.*, 2003), electromechanical switches (Jang *et al.*, 2005), infrared emitters and biosensors (Kong *et al.*, 2000) have been demonstrated.

It is reported that neither the velocity of the charge carriers at the upper part of the valence band, nor the velocity at the lower part of the conduction band is reduced, which is a common attribute of most materials. In fact, it stays constant throughout the bands (Geim and Novoselov, 2007). The low scattering rates and the electronic structure of GNR result in an excellent electronic transmission which is adjustable by doping or using electrostatic field. It can serve as interconnects due to its high conductivity. Since it can be gated, it could be used as a channel in novel transistors. Because of the stable and inert properties of GNR, it could be adopted to make big areas that have low defect densities and low electronic scattering rates (Geim and Novoselov, 2007).

A significant contributing reason to GNR's importance is the specific nature of its charge carriers, which is related to the fact that its charge carriers mimic relativistic particles, and is simply described using the Dirac Equation rather than the

Schrödinger Equation (Wehling *et al.*, 2008; Novoselov *et al.*, 2005). The Schrödinger Equation contributes in giving an illustration of electronic properties of materials in condensed matter physics (Wehling *et al.*, 2008; Novoselov *et al.*, 2005). GNR's high electron propagation is essential in creating high speed and high performance transistors. A GNR Metal Oxide Semiconductor Field Effect Transistor (GNR MOSFET) is an appliance, in which a GNR can be applied as the channel of a FET-like device (Schwierz, 2010). However, for GNR MOSFET's being used in realistic IC applications, material properties such as the energy band gap (EG) should be closely controlled. The method of preparing multilayer GNRFET is both appealing and amazing. Trilayer graphene nanoribbon (TGN) as a multilayer GNR can be piled up independently relying on the horizontal shift between consecutive graphene planes, which results in a variety of electronic properties and band structures.

The outcome of this study suggests that graphene based devices have potential to replace conventional silicon MOSFETs in driving the technology forward. It can also be used to evaluate the potential of GNR in integrated circuits incorporating both analog and digital functions which are recognized to exceed CMOS capabilities in term of scalability, speed and power consumption.

1.2 Problem Statement

The GNR (Monolayer, bilayer and trilayer) can be used as a transistor channel in the future. It has unique electronic characteristics such as symmetrical band structures, ballistic transport, and high current. In fact, the development of GNRFET is possible. The aim of this study is to analytically model the p-n and homo junctions of Monolayer GNR, bilayer graphene nanoribbon (BGN) schottky diode, the carrier concentration, ballistic conductance, and ballistic carrier transport of TGN, TGN schottky-barrier (SB) FET, graphene based NO₂ gas sensor and compared with published data. Despite all the research work, at the present moment, the following characteristics of GNR are not clear:

i. Short channel effect in nanoscale devices

The downsizing of channel length in a planar MOSFET causes short channel effect, leakage current, interconnect difficulties, high power consumption and quantum effect. When the channel length reaches nano meter scale, the conventional device modeling is no longer precise due to some parameters. Therefore, new device structures and materials such as GNRs are discovered as an alternative to overcome the challenges.

ii. P-N and homo junctions of monolayer GNRFET modeling

The p-n junction is an essential building block for electronic components. It is expected that GNR p-n and homo junction properties will be different from the traditional semiconductor p-n junctions. Developing a quantitative understanding of GNR p-n and homo junctions is a significant step towards developing novel devices such as GNR transistors and filters. Monolayer GNR p-n and homo junction has turned out to be of significant attention due to the fact that it presents better performance over conventional semiconductor p-n junction diodes in terms of electrical parameters such as turn-on voltage. In this research, a quantitative study of the near equilibrium I-V characteristics of GNR p-n and homo junctions is presented.

iii. Carrier statistics for TGN in Degenerate and Non-degenerate regimes

In previous models, most of the works are based on the charge or non-equilibrium Green Function calculations and three dimensional (3D) modes for the carrier statistics modeling of nanoscale transistor are explored. However, in this case, a one dimensional (1D) calculation for nanoscale devices will be adopted. Majority of the models calculated carrier concentration of monolayer GNR and BGN using the Maxwell Boltzmann approximation (non-degenerate regime). In this study, 1D visualization of carrier movement based on the band structure of TGN in the presence of a perpendicular electric field is employed. Here, an analytical model of TGN carrier statistics as a fundamental parameter on FET in corporation with a

numerical solution is proposed in the degenerate and non-degenerate limits. Furthermore, the efficiency of electron transport is the important quantity that defined as conductance (Datta, 2002). In this research, an introduction of the analytical model and numerical solution of TGN ballistic conductance is also presented. The conductance model can be adopted to derive current-voltage characteristic of TGNFET modeling.

iv. Ballistic carrier transport model for GNRFET structure in Degenerate and Non-degenerate regimes

The carrier transport features for long channel MOSFET model are no longer capable of describing carrier transport perfectly even for sub-100nm MOSFETs. The scattering-dominant transport mainly phonon, coulomb and surface roughness scattering usually occurs in the classical devices. The model is basically obtained from the Boltzmann Transport Equation (BTE) in a classical manner by invoking many simplifying closure approximations. To incorporate the quantum-mechanical effects into classical device simulation, BTE can be coupled to the Schrödinger or Wigner equations. Consequently, it is necessary to take the quantum transport into consideration when describing non-classical current transport models for nanoscale transistors such as GNRFET which operates in the quasi-ballistic transport regime. Therefore, simulation studies that depend on conventional models may incorrectly forecast device performance and physics. It is notable that the ballistic carrier transport model can be utilized to derive current-voltage characteristic of nanoscale GNRFET modeling. In this study, analytical models of monolayer GNR p-n and homo junction diodes, BGN schottky diode and TGN SB FET are developed, which can be adopted for the GNRFET optimization.

v. The monolayer graphene FET based gas sensor modeling

In order to higher accuracy, faster response time and increased sensitivity, sensor technology needs to be developed. Therefore, carbon based materials as a future candidate on sensor technology is promising to response to the huge demand for higher accuracy, faster response time, and increased sensitivity of a sensor. Due

to the unique electronic and elasticity properties such as large surface-to-volume ratio, high conductivity, high mobility, strong mechanical, low energy dynamics of electrons with atomic thickness and flexibility, graphene can be utilized in the creation of nanoscale sensors with low power requirements. In this study, the potential of monolayer graphene in generating NO₂ gas sensor is investigated. It is concluded that graphene has great potential as a material for ultra-sensitive gas sensor by optimizing of the device structure.

1.3 Research Objective

The purpose of this study is on the modeling and simulation of GNRs (monolayer, bilayer and trilayer) FET as a 1D device. The objectives of this study are as follow:

- i. To analytically model the p-n and homo junctions for monolayer GNR.
- ii. To analytically model the carrier statistics and conductance for TGN.
- iii. To formulate analytical and semi-empirical equations for ballistic carrier transport in GNR-FET.
- iv. To analytically model GNR-FET based devices.

1.4 Scope of Study

The implementation of this research includes the following:

- i. The enhancement of the p-n and homo junction analytical models for monolayer GNR.

- ii. The enhancement of the carrier concentration and conductance analytical models for TGN.
- iii. The enhancement of the ballistic carrier transport analytical model for GNR-FET.
- iv. Analytical modeling of GNR based devices such as monolayer graphene FET based gas sensor.
- v. Comparison between the proposed models and published data in terms of physical structure and electrical performance of the devices.

1.5 Research Contributions

There are many challenges in the downscaling procedure of conventional MOSFETs, such as short-channel effects, gate-leakage current, and so forth. Therefore, new materials and structure similar to multiple gate MOSFETs, CNT-FETs, GNR-FETs and molecular based transistors are significant to overcome the downscaling problems. This study mainly focuses on developing a physical model based on GNR-FET to find out device behavior, which are very important for optimizing electronic device performance. This research is basically different from other related investigations that are explained as follows:

- i. In this study, the quantum confinement effect for modeling transport phenomena in 1D GNR-FETs is employed. The energy band structure is the start point of all calculations. The carrier statistics in corporation with a numerical solution for low-dimensional nanostructure is elaborated.

- ii. The research develops the analytical models of monolayer GNR p-n and homo junctions, BGN schottky diode and TGN SB FET as a high speed switch.
- iii. A general analysis of recent developments in NO₂ gas nanoscale sensor based on monolayer graphene is also presented in this research.

1.6 Thesis Organization

This chapter briefly shows problem statements, objectives and scope of this research. The rest of the thesis is organized to elaborate the key aspects of this research. This section gives an outline of the thesis as follow:

Chapter 2 explains the historical overview of GNR (monolayer GNR, BGN and TGN). It presents a comprehensive overview of energy band structure, which is the key point to understand transport phenomena in quasi 1D material such as GNR. It inclusively reviews the related research in basic geometries of GNR. Furthermore, the historical study of monolayer GNR p-n and homo junctions, BGN schottky diode, TGN SB FET and monolayer graphene FET based gas sensor is briefly presented in this chapter.

Chapter 3 describes the methodology involve in this research. In general, the activities needed for this research is categorized into three phases as described in this chapter. At the next, a general description of the system design and development process is discussed. Finally, the framework of this research is introduced which includes the study in the modeling part and simulation part by MATLAB software. In simulation part parallel to the modeling study, MATLAB software programming will be used intensively.

Chapter 4 outlines the proposed methods for modeling and simulation study of GNR (monolayer GNR, BGN and TGN) based FET models. This chapter proposes analytical modeling of monolayer GNR p-n and homo junction, BGN

schottky diode performance. Additionally, quantum confinement effect of TGN carrier concentration, the effect of applied voltage on the TGN carrier effective mass, the conductance of TGN and also analytical modeling of TGN SB FET for high speed switching applications are discussed in this chapter. At the end, the simulated results are shown and discussed.

Chapter 5 presents the monolayer graphene FET based gas sensor application. Analytical modeling of monolayer graphene FET based NO₂ gas sensor is presented in this chapter. The comparison of proposed model with published data is illustrated by diagrams and charts, and good agreement is reported.

Chapter 6 briefly summarizes the thesis with some conclusions. However, the proposed models show a promising improvement in obtained results. Furthermore, the challenging and emerging trends identified for future research are also suggested in this chapter.

REFERENCES

- Abergel, D. S. L., Apalkov, V., Berashevich, J., Ziegler, K., and Chakraborty, T. (2010). Properties of graphene: a theoretical perspective. *Advances in Physics*. 59(4): 261-482.
- Ahmadi, M. T., Johari, Z., Amin, N. A., Fallahpour, A., and Ismail, R. (2010). Graphene nanoribbon conductance model in parabolic band structure. *J. of Nanomaterials*. 2010(2010): 753738.
- Ahmadi, M. T., Johari, Z., Amin, N. A., and Ismail, R. (2011). Band energy effect on carrier velocity limit in graphene nanoribbon. *journal of Experimental Nanoscience*. 7(1): 62-73.
- Ahmadi, M. T., Heong, Y. W., Saad, I., and Ismail, R. (2009). MOSFET-Like Carbon Nanotube Field Effect Transistor Model. *Technical Proceeding of Nanotech Conference & Expo 2009*. 3: 574-579.
- Ahmadi, M. T., Ismail, R., Michael, L. P. T., and Arora, V. K. (2008). The Ultimate Ballistic Drift Velocity in Carbon Nanotubes. *Journal of Nanomaterials*. 2008(2008): 769250.
- Ahmadi, M. T., Rahmani, M., Ghadir, M. H., and Ismail, R. (2012). Graphene Nanoribbon Homo Junction Characteristics. *Science of Advanced Materials*. 4(7): 753-756.
- Alam, K. (2009). Transport and performance of a zero-Schottky barrier and doped contacts graphene nanoribbon transistors. *Semiconductor Science and Technology*. 24(1): 015007.
- Anantram, M. P., Lundstrom, M. S. and Nikonov, D. E. (2008). Modeling of Nanoscale Devices. *Processing of the IEEE*. 96(9).
- Aoki, M. and Amawashi, H. (2007). Dependence of band structures on stacking and field in layered graphene. *Solid State Communications*, 142(3): 123-127.

- Appenzeller, J., Sui, Y., and Chen, Z. H. (2009). Graphene nanostructures for device applications. *2009 Symposium on Vlsi Technology, Digest of Technical Papers*. 124-126.
- Arora, N. D., and Sharma, M. S. (1991). MOSFET substrate current model for circuit simulation. *Electron Devices, IEEE Transactions on*. 38(6): 1392-1398.
- Avetisyan, A. A., Partoens, B., and Peeters, F. M. (2010). Stacking order dependent electric field tuning of the band gap in graphene multilayers. *Physical Review B*. 81(11): 115432.
- B.J Sheu, D. L. S., Ko, P.K., and Berkeley, M.C. (1987). Short-channel IGFET model for MOS transistors. *IEEE Journal of Solid State Circuits*. 22(4): 558-566.
- Bell, D. C. (2009). Contrast Mechanisms and Image Formation in Helium Ion Microscopy, Microscopy and Microanalysis. *Microscopy and Microanalysis*. 15(2): 147.
- Bresciani, M., Palestri, P., Esseni, D., and Selmi, L. (2010). Simple and efficient modeling of the E-k relationship and low-field mobility in Graphene Nano-Ribbons. *Solid-State Electronics*. 54(9): 1015-1021.
- Buddharaju, K.D., Singh, N., Rustagi, S.C., Teo, S.H.G., Wong, L.Y., Tang, L.J., Tung, C.H., Lo, G.Q., Balasubramanian, N. and Kwong, D.L. (2007). Gate-all around Si-nanowire CMOS inverter logic fabricated using top-down approach. *Proceedings of the IEEE 37th European Solid-State Device Research Conference (ESSDERC 2007)*, Munich, Germany: 303-306.
- Castro, E. V., Novoselov, K. S., Morozov, S. V., Peres, N. M. R., Lopes Dos Santos, J. M. B., Nilsson, J., Guinea, F., Geim, A. K., and Castro Neto, A. H. (2010). Electronic properties of a biased graphene bilayer. *Journal of Physics-Condensed Matter*. 22(17): 175503.
- Castro, E. V., Peres, N. M. R., Lopes Dos Santos, J. M. B., Guinea, F., and Castro Neto, A. H. (2008). Bilayer graphene: gap tunability and edge properties. *International Conference on Theoretical Physics*. Dubna-Nano, 129.
- Castro Neto, A. H., Guinea, F., Peres, N. M. R., Novoselov, K. S., and Geim, A. K. (2009). The electronic properties of graphene. *Rev. Mod. Phys.* 81(1): 109-162.

- Cheianov, V. V., Fal'ko, V., and Altshuler, B. L. (2007). The focusing of electron flow and a veselago lens in graphene p-n junctions. *Science*. 315(5816): 1252-1255.
- Cheianov, V. V., and Fal'ko, V. I. (2006). Selective transmission of Dirac electrons and ballistic magnetoresistance of $\{n-p\}$ junctions in graphene. *Phys. Rev. B*. 74: 041403.
- Chen, C.-C., Aykol, M., Chang, C.-C., Levi, A. F. J., and Cronin, S. B. (2011). Graphene-Silicon Schottky Diodes. *Nano Letters*. 11(5): 1863-1867.
- Chen, J., Perebeinos, V., Freitag, M., Tsang, J. C., Fu, Q., Liu, J., and Avouris, P. (2005). Bright infrared emission from electrically induced excitons in carbon nanotubes. *Science*. 310(5751): 1171–1174.
- Chen, Y., Gao, B., Zhao, J. X., Cai, Q. H., and Fu, H. G. (2011c). Si-doped graphene: an ideal sensor for NO- or NO₂-detection and metal-free catalyst for N₂O-reduction. *Journal of Molecular Modeling*. 18(5): 2043-54
- Chen, Z., Lin, Y. M., Michael, J. Rooks, and Avouris, P. (2007). Graphene non-ribbon electronics. *Physica E*. 40.
- Cheraghchi, H., and Esmailzade, H. (2010). A gate-induced switch in zigzag graphene nanoribbons and charging effects. *Nanotechnology*. 21(20): 205306.
- Chiu, H. Y., Perebeinos, V., Lin, Y. M., and Avouris, P. (2010). Controllable p-n junction formation in monolayer graphene using electrostatic substrate engineering. *Nano Letters*. 10(11): 4634-4639.
- Choucair, M., and Stride, J. New graphene having cavities in it, useful for reinforcing a composite and for manufacturing e.g. electronic device, sensor and battery. *Newsouth Innovations Pty Ltd, WO2009029984-A1; WO2009029984-A8*.
- Cohen-Karni, T., Qing, Q., Li, Q., Fang, Y., and Lieber, C. M. (2010). Graphene and Nanowire Transistors for Cellular Interfaces and Electrical Recording. *Nano Letters*. 10(3): 1098-1102.
- Coletti, C., Riedl, C., Lee, D. S., Krauss, B., Patthey, L., Klitzing, K. V., Smet, J. H., and Starke, U. (2010). Band structure engineering of epitaxial graphene on SiC by molecular doping. *Physical Review B*. 81(23): 235401.
- Craciun, M. F., Russo, S., Yamamoto, M., Oostinga, J. B., Morpurgo, A. F., and Tarucha, S. (2009). Trilayer graphene: a semimetal with gate-tunable band overlap. *Nature Nanotechnology*. 4, 383-388.

- Craciun, M. F., Russo, S., Yamamoto, M., and Tarucha, S. (2011). Tuneable electronic properties in graphene. *NanoToday Press*. 6(1): 42-60.
- Dankerl, M., Hauf, M. V., Lippert, A., and HESS, L. H. (2010). Graphene Solution-Gated Field-Effect Transistor Array for Sensing Applications. *Advanced Functional Materials*. 20(18): 3117-3124.
- Datta, S. (2002). *Electronic Transport in Mesoscopic Systems*. Cambridge, UK: Cambridge University Press.
- Datta, S. (2005). *Quantum Transport: Atom to Transistor*. New York, Published in the United States of America by Cambridge University Press.
- Debdeep, J., Tian, F., Qin, Z., and Huili, X. (2008). Zener tunneling in semiconducting nanotube and graphene nanoribbon p-n junctions. *Applied Physics Letters*. 93(11): 112106-1—112106-3
- Dong, X., Fu, D., Fang, W., Shi, Y., Chen, P., and Li, L. J. (2009). Doping Single-Layer Graphene with Aromatic Molecules. *Small*. 5(12): 1422-1426.
- Entani, S., Sakai, S., Matsumoto, Y., Naramoto, H., Hao, T., and Maeda, Y. (2010). Interface Properties of Metal/Graphene Heterostructures Studied by Micro-Raman Spectroscopy. *Journal of Physical Chemistry C*. 114(47): 20042-20048.
- Eriksson, J., Rorsman, N., and Zirath, H. (2003). 4H-Silicon Carbide Schottky Barrier Diodes for Microwave Applications. *IEEE Transactions On Microwave Theory And Techniques*. 51(3): 796-804.
- Fang, F. F., and Fowler, A. B. (1970). Hot Electron Effects and Saturation Velocities in Silicon Inversion Layers. *Journal of Applied Physics*. 41(4): 1825-1831.
- Fallahpour, A. H., Ahmadi, M. T. (2012). *Advanced Nanoelectronics. Chapter 10: Silicon Nanowire Field Effect Transistor Modeling*. Editors: Ismail, R., Ahamdi, M. T., Anwar, S. Taylor and Francis.
- Fiori, G., Yoon, Y., Hong, S., Jannacconet, G., and Guo, J. (2007). Performance Comparison of Graphene Nanoribbon Schottky Barrier and MOS FETs. *Electron Devices Meeting, 2007. IEDM 2007. IEEE International*. 757-760.
- Fowler, J. D., Allen, M. J., Tung, V. C., Yang, Y., Kaner, R. B., Weiller, B. H. (2009). Practical Chemical Sensors from Chemically Derived Graphene. *ACS Nano*. 3(2): 301-306.
- Geim, A. K., and Novoselov, K. S. (2007). The rise of graphene. *Nature Materials*. 6: 183-191.

- Ghosh, A., Dattatray, J. L., Panchakarla, L. S., Govindaraj, A., and Rao, C. N. R. (2009). NO₂ and Humidity Sensing Characteristics of Few-layer Graphene. *Chemical Physics, Chemistry and Physics of Materials Unit, Jawaharlal Nehru Centre for advanced Scientific Research, Jakkur, P.O., Bangalore 560064, India.*
- Gogotsi, Y. G., Kailer, A., and Nickel, K. G. (1999). Materials: Transformation of diamond to graphite. *Nature*, 401(6754): 663-664.
- Gorden, E. M. (1965). Cramming more components onto integrated circuits. *Electronics*, 38.
- Gorjizadeh, N. and Kawazoe, Y. (2010). Chemical Functionalization of Graphene Nanoribbons. *Journal of Nanomaterials*, 2010(2010): 513501.
- Guinea, F., Castro Neto, A. H., and Peres, N. M. R. (2006). Electronic states and Landau levels in graphene stacks. *Phys. Rev. B*, 73(24): 245426.
- Guinea, F., Castro Neto, A. H., and Peres, N. M. R. (2007). Interaction effects in single layer and multi-layer graphene. *European Physical Journal-Special Topics*, 148(20): 117-125.
- Guinea, F., Castro Neto, A. H., and Peres, N. M. R. (2007). Electronic properties of stacks of graphene layers. *Solid State Communications*. 143(1-2): 116-122.
- Guo, B., Fang, L., Zhang, B. and Gong, J. R. (2011). Graphene Doping: A Review. *Insciences J.* 1(2): 80-89.
- Guttinger, J., Stampfer, C., Molitor, F., Graf, D., Ihn, T., and Ensslin, K. (2008). Coulomb oscillations in three-layer graphene nanostructures. *New Journal of Physics*. 10:125029.
- Han, M. Y., Özyilmaz, B., Zhang, Y., and Kim, P. (2007). Energy Band-Gap Engineering of Graphene Nanoribbons. *Phys Rev Lett*. 98(20): 206805.
- Hill, E.W., Vijayaraghavan, A. & Novoselov, K. (2011). Graphene Sensors. *IEEE Sensors Journal*. 11(12): 3161-3170.
- Hu, Y. H., Wang, H., and Hu, B. (2010). Thinnest Two-Dimensional Nanomaterial—Graphene for Solar Energy. *ChemSusChem*. 3(7): 782–796.
- Huang, B., Li, Z., Zhou, G., Hao, S., Wu, J., Gu, B. L., Duan, W. (2008). Adsorption of Gas Molecules on Graphene Nanoribbons and Its Implication for Nanoscale Molecule Sensor. *J. Phys. Chem. C*. 112(35): 13442–13446.

- Huang, Y., Dong, X., Liu, Y., Li, L. J., and Chen, P. (2011). Graphene-based biosensors for detection of bacteria and their metabolic activities. *Journal of Materials Chemistry*. 21(33): 12358-12362.
- Irifune, T., Kurio, A., Sakamoto, S., Inoue, T., and Sumiya, H. (2003). Materials: Ultrahard polycrystalline diamond from graphite. *Nature*. 421: 599-600.
- J. Guo, A. J., Dai, H., Datta, S., and Lundstrom, M. (2003). Predicted Performance Advantages of Carbon Nanotube Transistors with Doped Nanotubes. *Condensed Matter*. 0309039.
- Jang, J. E., Cha, S. N., Choi, Y., Amaratunga, G. A. J., Kang, D. J., Hasko, D. G., Jung, J. E., and Kim, J. M. (2005). Nanoelectromechanical switches with vertically aligned carbon nanotubes. *Applied Physics Letters*. 87(16):163114 - 163116.
- Javey, A., Guo, J., Wang, Q., Lundstrom, M., and Dai, H. (2003). Ballistic carbon nanotube field-effect transistors. *Nature*. 424: 654-657.
- Jiao, L., Zhang, L., Wang, X., Diankov, G., and Dai, H. (2009). Narrow graphene nanoribbons from carbon nanotubes. *Nature*. 458(7240): 877-880.
- Jiménez, D. (2008). A current–voltage model for Schottky-barrier graphene-based transistors. *Nanotechnology*. 19(2008): 345204-345208.
- Jin, L., Hong Xia, L., Bin, L., Lei, C., and Bo, Y. (2010). Study on two-dimensional analytical models for symmetrical gate stack dual gate strained silicon MOSFETs. *Chin. Phys. B*. 19(10): 107302.
- Jin, S. (2006). Modeling of Quantum Transport in Nano-Scale MOSFET Devices. Ph.D. dissertation, Seoul National University.
- Jin, X., Zhi-Xiong, Y., Wei-Tao, X., Li-Xin, X., Hui, X., and Fang-Ping, O. Y. (2012). Electronic properties of graphene nanoribbon doped by boron/nitrogen pair: a first-principles study. *Chin. Phys. B*. 21 (2): 027102.
- Johari, Z., Ahmadi M. T., Chang Yih, D. C., Amin, N. A., and Ismail, R. (2010). Modelling of Graphene Nanoribbon Fermi Energy. *Journal of Nanomaterials*. 2010(2010): 909347.
- Kargar, A., and Chengkuo, L. (2009). Graphene nanoribbon schottky diodes using asymmetric contacts, *Nanotechnology, 2009. IEEE-NANO 2009. 9th IEEE Conference on*. 243-245.

- Kargar, A., and Wang, D.L. (2010). Analytical modeling of graphene nanoribbon Schottky diodes. *Carbon Nanotubes, Graphene, and Associated Devices III* 7761. DOI: 10.1117/12.871883.
- Katsnelson, M. I., Novoselov, K. S., and Geim, A. K. (2006). Chiral tunneling and the Klein paradox in graphene. *Nature Physics*. 2: 620-625.
- Ko, G., Kim, H. Y., Ahn, J., Park, Y. M., Lee, K. Y., and Kim J. (2010). Graphene-based nitrogen dioxide gas sensors. *Current Applied physics*. 10(4): 1002-1004.
- Kong, J., Franklin, N. R., Zhou, C., Chapline, M. G., Peng, S., Cho, K., and Dai, H. (2000). Nanotube molecular wires as chemical sensors. *Science*. 287(5453): 622–625.
- Koshino, M. (2008). Electron delocalization in bilayer graphene induced by an electric field. *Phys. Rev. B*. 78(15): 155411.
- Koshino, M. (2009). Electronic transport in bilayer graphene. *New J. Phys.* 11(9): 095010.
- Koshino, M. (2010). Interlayer screening effect in graphene multilayers with ABA and ABC stacking. *Phys. Rev. B*. 81(12):125304.
- Koshino, M., and McCann, E. (2009b). Gate-induced interlayer asymmetry in ABA-stacked trilayer graphene. *Phys. Rev. B*. 79(12): 125443.
- Koshino, M., and McCann, E. (2009a). Trigonal warping and Berry's phase π in ABC-stacked multilayer graphene. *Phys. Rev. B*. 80(16): 165409.
- Koshino, M., McCann, E. (2010). Parity and valley degeneracy in multilayer graphene. *Phys. Rev. B* 81(11): 115315.
- Krowne, C. M. (2010). Intrinsic quantum conductances and capacitances of nanowires and nanocables. *Physics Letters A*. 374(4): 614-619.
- Kumar, S. B., Guoa, J. (2012). Chiral tunneling in trilayer graphene. *Applied Physics Letters*. 100(16): 163102.
- Kumazaki, H., Hirashima, D. S. (2009). Spin-Polarized Transport on Zigzag Graphene Nanoribbon with a Single Defect. *Journal of the Physical Society of Japan*. 78(9): 094701.
- Kyle R. R., Yang, W., Ringer, S. P., and Braet, F. (2010). Toward Ubiquitous Environmental Gas Sensors Capitalizing on the Promise of Graphene. *Environ. Sci. Technol.* 44(4): 1167–1176.

- Latil, S., and Henrard, L. (2006). Charge carriers in few-layer graphene films. *Physical Review Letters*. 97(3): 036803.
- Li H., Xu C., and Srivastava, N. (2009a). Carbon Nanomaterials for Next-Generation Interconnects and Passives: Physics, Status, and Prospects. *IEEE Transactions On Electron Devices*. 56(9):1799-1821.
- Li J., Ye Q., Cassell, A., Tee Ng, H., Stevens, R., Han, J., and Meyyappan M. (2003). Bottom-up approach for carbon nanotube interconnects. *Appl. Phys. Lett.* 82(15): 2491–2493.
- Li, T. S., Chang, S. C., and Lin, M. F. (2009b). Electron transport in nanotube-ribbon hybrids. *Physics of Condensed Matter*. 70(4): 497–505.
- Li, T. S., Huang, Y. C., Chang, S. C., Chuang, Y. C., and Lin, M. F. (2008a). Transport properties of AB-stacked bilayer graphene nanoribbons in an electric field. *European Physical Journal B*. 64(1): 73-80.
- Li, X. F., Wang, L. L., Chen, K. Q., and Luo, Y. (2012). Electronic transport through zigzag/armchair graphene nanoribbon heterojunctions. *Journal of Physics: Condensed Matter*. 24(9): 095801.
- Li X., Wang, X., Zhang, L., Lee, S., and Dai, H. (2008b). Chemically Derived, Ultrasoft Graphene Nanoribbon Semiconductors. *Science*. 319(5867):1229-1232.
- Li, Y. F., Li, B. R., and Zhang, H. L. (2009c). The computational design of junctions between carbon nanotubes and graphene nanoribbons. *Nanotechnology*. 20(22): 225202.
- Liang, G. C., Neophytou, N., Nikonov, D. E., and Lundstrom, M. S. (2007). Performance projections for ballistic graphene nanoribbon field-effect transistors. *Ieee Transactions on Electron Devices*. 54(4): 677-682.
- Liang, Q., and Dong, J. (2008). Superconducting switch made of graphene–nanoribbon junctions. *Nanotechnology*. 19(35): 355706.
- Liao, L., Bai, J., Cheng, R., Lin, Y., Jiang, S., Qu, Y., Huang, Y., and Duan, X. (2010). Sub-100 nm Channel Length Graphene Transistors. *Nano Letters*. 10(10): 3952-3956.
- Low, T., Hong, S., Appenzeller, J., Datta, S., and Lundstrom, M. S. (2009). Conductance asymmetry of graphene p-n junction. *IEEE Trans. Electron Devices*. 56(6): 1292-1299.

- Lundstrom, M. (1997). Elementary scattering theory of the Si MOSFET. *IEEE Electron. Device Lett.* 18, 361–363.
- Lundstrom, M., and Guo, J. (2006). Nanoscale transistors: device physics, modeling and simulation. *Springer, Birkhäuser- Technology & Engineering.* 217 pages.
- M. F. Craciun, S. R., Yamamoto, M., and Tarucha, S. (2011). Tuneable electronic properties in graphene. *NanoToday Press.* 6(1).
- Majumdar, K., Murali, K.V. R. M., Bhat, N., and Lin, Y. M. (2010). Intrinsic Limits of subthreshold slop in biased bilayer graphene transistor. *Applied Physics Letters.* 96(12):123504.
- Mayorov, AS, Gorbachev, RV, Morozov, SV, Britnell, L, Jalil, R, Ponomarenko, LA, Blake, P, Novoselov, KS, Watanabe, K, Taniguchi, T, Geim, AK. (2011). Micrometer-Scale Ballistic Transport in Encapsulated Graphene at Room Temperature. *Nano Lett.* 11: 2396-2399.
- McEuen, P. L., Fuhrer, M. S., and Park, H. (2002). Single-walled carbon nanotube electronics. *Nanotechnology, IEEE Transactions on.* 1(1):78-85.
- Meric, I., Han, M. Y., Young, A. F., Ozilmaz, B., Kim, P. H., and Shepard, K. L. (2008). Current saturation in zero-bandgap, topgated graphene field-effect transistors. *Nature nanotechnology.* 3(11): 654-659.
- Miao Zhou, Y. L., Yong Qing, C., Zhang, C., and Feng, Y. P. (2011). Adsorption of gas molecules on transition metal embedded graphene: a search for high-performance graphene-based catalysts and gas sensors. *Nanotechnology.* 22(38): 385502.
- Misewich, J. A., Martel, R., Avouris, P., Tsang, J. C., Heinze, S., and Tersoff J. (2003). Electrically induced optical emission from a carbon nanotube FET. *Science.* 300(5620): 783–786.
- Muller, J. E. (1992). Textite effect of a nonuniform magnetic field on a two-dimensional electron gas in the ballistic regime. *Phys. Rev. Lett.*
- Naeemi, A., and Meindl J. D. (2007). Conductance modeling for graphene nanoribbon (GNR) interconnects. *Electron Device Letters, IEEE.* 28(5): 428-431.
- Nakada K., F. M., Dresselhaus, G., and Dresselhaus, M. S. (1996). Edge state in graphene ribbons: Nanometer size effect and edge shape dependence. *Phys. Rev. B* 54(24): 17954-17961.

- Neamen, D. A. (2011). *Semiconductor Physics and Devices*. Third Edition. University of New Mexico.
- Ni, Z. H., Wang, H. M., Lua, Z. Q., Wang, Y. Y., Yu, T., Wub, Y. H., and Shena, Z. X. (2009). The effect of vacuum annealing on graphene. *Journal of RAMAN Spectroscopy*.41(5): 479–483.
- Novoselov, K. S., Geim, A. K., Morozov S.V., Jiang D., Katsnelson M.I., Grigorieva I.V., Dubonos S.V., Firsov A.A. (2005). Two-dimensional gas of massless Dirac fermions in graphene. *Nature*. 438:197-200.
- Ouyang, Y., Dai, H., and Guo, J. (2009). Multilayer Graphene Nanoribbon for 3D Stacking of the Transistor Channel. *Electron Devices Meeting (IEDM), IEEE International*:1-4.
- Ouyang, Y., Yoon, Y., and Guo, J. (2007). Scaling behaviors of graphene nanoribbon FETs: a three-dimensional quantum simulation study. *IEEE Transactions on Electron Devices* 54: 2223-2231.
- Peres, N. M. R., Neto, A. H. C., Guinea, F. (2006). Conductance quantization in mesoscopic graphene. *Physical Review B*. 73(19): 195411-195419.
- Pierret R. F. (2003). Advanced Semiconductor Fundamentals. *Prentice Hall, Englewood Cliffs, NJ*.
- Polyanin, A.D. (2004). Cubic Equation.
- Pramanik, A., and Kang, H. S. (2011). Density Functional Theory Study of O₂ and NO Adsorption on Heteroatom-Doped Graphenes Including the van der Waals Interaction. *Physical Chemistry C*. 115(22): 10971-10978
- Rahmani, M., Ahmadi, M. T., Ghadiry, M. H., Anwar, S., and Ismail, R. (2012a). The Effect of Applied Voltage on the Carrier Effective Mass in ABA Trilayer Graphene Nanoribbon. *Journal of Computational and Theoretical Nanoscience*. 9: 1–4.
- Rahmani, M., Ahmadi, M. T., Kiani, M. J., and Ismail, R. (2012b). Monolayer Graphene Nanoribbon P-n Junction. *Journal of Nanoengineering and Nanomanufacturing*. 2: 1–4.
- Rahmani, M., Ahmadi, M. T., Karimi F.A., H., kiani, M. J., Akbari, E., and Ismail, R. (2012c). Analytical Modeling of Monolayer Graphene-based NO₂ Sensor. *Sensor Letters*. 10:1-6.
- Rahmani, M., Ahmadi, M. T., Ismail, R., and Ghadiry, M. H. (2013). Performance of Bilayer Graphene Nanoribbon Schottky Diode in Comparison with

- Conventional Diodes. *Journal of Computational and Theoretical Nanoscience*. 10: 1–5.
- Rahmani, M., Ahmadi, M. T., Karimi F. A., H., and Ismail, R. (2012e). The Effect of Bilayer Graphene Nanoribbon Geometry on Schottky Diode Performance. *Nano*. (under review)
- Rahmani, M., Ahmadi, M. T., Karimi F. A., H., Saeidmanesh, M., Akbari, E., and Ismail, R. (2012f). Analytical Modeling of Trilayer Graphene Nanoribbon Schottky-Barrier FET for High Speed Switching Applications. *Nanoscale Research Letters*. (Accepted)
- Rahmani, M., Ahmadi, M. T., Shayesteh, N., Amin, N. A., Ismail, R. (2011). Current-Voltage Modeling of Bilayer Graphene Nanoribbon Schottky Diode. *Proceeding of IEEE-RSM2011*. Kota Kinabalu, Malaysia.
- Rahmani, M., Mousavi, S. M., Sadeghi, H. (2012d). *Advanced Nanoelectronics. Chapter 8: Trilayer Graphene Nanoribbon Field Effect Transistor Modeling*. Editors: Ismail, R., Ahmadi, M. T., Anwar, S. Taylor and Francis.
- Ratinac, K. R., Yang, Ringer, S. P., and Braet, F. (2010). Toward Ubiquitous Environmental Gas Sensors-Capitalizing on the Promise of Graphene. *Environ. Sci. Technol.* 44(4): 1167–1176.
- Ray, B., and Mahapatra, S. (2009). Modeling of Channel Potential and Subthreshold Slope of Symmetric Double-Gate Transistor. *IEEE Transactions on Electron Devices*. 56(2): 260-266.
- Rechem, D., Latreche, S., and Gontrand, C. (2009). Channel length scaling and the impact of metal gate work function on the performance of double gate-metal oxide semiconductor field-effect transistors. *journal of physics*. 72(3): 587-599.
- Rozhkova, A.V., Giavarasa, G., Bliokha, Y. P., Freilikhera, V., and Noria, F. (2011). Electronic properties of mesoscopic graphene structures: Charge confinement and control of spin and charge transport. *Physics Reports*. 503(2-3):77-114.
- Ryzhii, V., Ryzhii, M., Shur, M. S., Mitin, V. (2009). Graphene tunneling transit-time terahertz oscillator based on electrically induced p-i-n junction. *Appl Phys Express*. 2(1): 1-2.
- Saad, I., Michael, L. P. T., Ahmadi, M. T., Ismail, R., and Arora, V. K. (2010). The Dependence of Saturation Velocity on Temperature, Inversion Charge and

- Electric Field in a Nanoscale MOSFET. *Nanoelectronics and Materials*. 3(2010):17-34.
- Sadeghi, H., Ahmadi, M. T., Mousavi, S. M., and Ismail R. (2012). Channel Conductance of ABA Stacking Trilayer Graphene Field Effect Transistor. *Modern Physics Letters B*. 26(8): 1250047.
- Saito, R., Dresselhaus G., and Dresselhaus M. S. (1998). *Physical properties of carbon nanotubes*. Imperial College Press, Technology & Engineering. University of Electro-Communications, Tokyo. 259.
- Sankaran, S., and Kenneth, K. O. (2005). Schottky Barrier Diodes for Millimeter Wave Detection in a Foundry CMOS Process. *IEEE Electron Device Lett*. 26(7): 492-494.
- Saurabh, S., Jagadesh, K. M. (2009). Impact of Strain on Drain Current and Threshold Voltage of Nanoscale Double Gate Tunnel Field Effect Transistor: Theoretical Investigation and Analysis. *Jpn. J. Appl. Phys.* 48(2009): 064503-064510.
- Schwierz, F. (2010). Graphene transistors. *Nature Nanotechnology*. 5: 487-496.
- Scipioni, L., Notte, J., Sijranddij, S., and Grin, B.J. (2008). Helium ion micro-scope. *Adv Mater Proc*.
- Shayesteh, N., Ahmadi, M. T., Rahmani, M., Amin, N.A., Shayesteh, H., and Ismail R. Monolayer Graphene Nanoribbon p-n Junction. *IEEE-RSM2011 Proc. 2011*. Kota Kinabalu, Malaysia.
- Shur, M., Rumyantsev, S., Liu, G., and Balandin, A.A. Electrical and Noise Characteristics of Graphene Field-Effect Transistors. 145 - 149 *21st International Conference on Noise and Fluctuations 2011*. Toronto.
- Stauber, T., Peres, N. M. R., Guinea, F., and Castro Neto, A. H. (2007). Fermi liquid theory of a Fermi ring. *Phys. Rev. B* 75(11): 115425.
- Stephen Thornhill, ET. al. (2008). Graphene Nanoribbon Field-effect Transistors. *IEEE Sensors Journal*. 978(1): 4244-1684.
- Svilicic, B., Jovanovic, V., Suligoj, T. (2008). Vertical Silicon-on-Nothing FET: Subthreshold Slope Calculation Using Compact Capacitance Model. *Informacije MIDE M Journal of Microelectronics, Electronic Components and materials* (0352-9045). 38(1): 1-4.

- T.Cohen-Karni, Qing, Q., Li, Q., Fang, Y., and Lieber, C. (2010). Graphene and Nanowire Transistors for Cellular Interfaces and Electrical Recording. *Nano Letters*. 10(3): 1098-1102.
- Takane, Y. (2010). Anomalous Enhancement of the Boltzmann Conductivity in Disordered Zigzag Graphene Nanoribbons. *Journal of the Physical Society of Japan*. 79(2): 024711.
- Tang, S., and Cao, Z. (2011). Adsorption of nitrogen oxides on graphene and graphene oxides: Insights from density functional calculations. *J. Chem. Phys.* 134(4): 044710.
- Terronesa, M., Botello-Méndezb, A., and Campos-Delgadoc, J. (2010). Graphene and graphite nanoribbons: Morphology, properties, synthesis, defects and applications. *Nano today*. 5(4): 351-372.
- Thompson, S., Packan, P., and Bohr, M. (1999). MOS Scaling: Transistor Challenges for the 21st Century. *Intel Technology Journal*. 2(3): 1-19.
- Tworzydło, J., Trauzettel, B., Titov, M., Rycerz, A., and Beenakker, C. W. J. (2006). Sub-poissonian shot noise in graphene. *Phys. Rev. Lett.* 96(24): 246802.
- Wakabayashi, K., Fujita, M., Ajiki, H., and Sigrist, M. (1999). Electronic and magnetic properties of nanographite ribbons. *Physical Review B*. 59(12): 8271-8282.
- Wang, H., Maiyalagan, T., and Wang, X. (2012). Review on Recent Progress in Nitrogen-Doped Graphene: Synthesis, Characterization, and its Potential Applications. *ACS Catal.* 2 (5): 781–794.
- Watanabe, E., Yamaguchi, S., Nakamura, J., and Natori, A. (2009). Ballistic thermal conductance of electrons in graphene ribbons. *Phys. Rev. B*. 80(8).
- Wehling, T., Novoselov, K., Morozov, S., Vdovin, E., Katsnelson, M., Geim, A., and Lichtenstein, A. (2008). Molecular doping of graphene. *Nano Letters*. 8(1): 173-177.
- Williams, J. R. (2009). Electronic Transport in Graphene: p-n Junctions, Shot Noise and Nanoribbons. *Harvard University Cambridge, Massachusetts*: 3365482
- Wong, H. (2000). Drain breakdown in submicron MOSFETs: a review. *Microelectronics Reliability*. 40(1): 3-15.
- Xu Y., and Ke, S. H. (2010). The infrared spectra of ABC-stacking tri- and tetra-layer graphenes. *Mesoscale and Nanoscale Physics*.

- Yin, G., Liang, Y. Y., Jiang, F., Chen, H., Wang, P., Note, R., Mizuseki, H., and Kawazoe, Y. (2009). Polarization Induced Switching Effect in Graphene Nanoribbon Edge-Defect Junction. *J Chem Phys.* 131(23): 234706.
- Yoon, Y., Fiori, G., Hong, S., Iannaccone, G., and Guo, J. (2008). Performance comparison of graphene nanoribbon FETs with Schottky contacts and doped reservoirs. *IEEE Trans. Electron Devices.* 55(9): 2314-2323.
- Yu Ming, L., Farmer, D. B., Tulevski, G. S., Sheng, X., Gordon, R. G., Avouris, P. (2008). Chemical Doping of Graphene Nanoribbon Field-Effect Devices *IEEE.* 27-28.
- Yu, S. S., Zheng, W. T., and Jiang, Q. (2010). Electronic Properties of Nitrogen-/Boron-Doped Graphene Nanoribbons With Armchair Edges. *Nanotechnology, IEEE Transactions on.* 9(1): 78-81.
- Yuan, S., De Raedt, H., and Katsnelson, M. I. (2010). Electronic Transport in Disordered Bilayer and Trilayer Graphene. *Phys. Rev. B.* 82(23): 5409.
- Zhang, F., Sahu, B., Min, H., and MacDonald, A. H. (2010a). Band Structure of ABC-Stacked Graphene Trilayers. *Phys. Rev. B.* 82(3): 035409.
- Zhang, J., Wang, S. R., Wang, Y. M., Wang, Y., Zhu, B. L., Xia, H. J., Guo, X. Z., Zhang, S. M., Huang, W. P., and Wu, S. H. (2009). NO₂ sensing performance of SnO₂ hollow-sphere sensor. *Sensors and Actuators B-Chemical.* 135(2): 610-617.
- Zhang, Q., Fang, T., Xing, H., Seabaugh, A., and Jena, D. (2008). Graphene nanoribbon tunnel transistors. *IEEE Electron Device Lett.* 29(12): 1344-1346.
- Zhang, Y. H., Chen, Y. B., Zhou, K. G., Liu, C. H., Zeng, J., Zhang, H. L., and Peng, Y. (2009). Improving gas sensing properties of graphene by introducing dopants and defects: a first-principles study. *Nanotechnology.* 20(18): 185504-185512.
- Zhang, Y., Tan, Y. W., Stormer, H. L., and Kim, P. (2005). Experimental observation of the quantum Hall effect and Berry's phase in graphene. *Nature* . 438(201): 201.
- Zhang, Y. T., Jiang, H., Sun, Q., and Xie, X. C. (2010b). Spin polarization and giant magnetoresistance effect induced by magnetization in zigzag graphene nanoribbons. *Physical Review B.* 81(16): 165404-165409.

- Zhao, P., Choudhury, M., Mohanram, K., and Guo, J. (2008). Computational Model of Edge Effects in Graphene Nanoribbon Transistors. *Nano Research*. 1(5): 395-402.
- Zhu, J., and Woo, J. C. S. (2007). A novel graphene channel field effect transistor with Schottky tunneling source and drain. *Essderc 2007: Proceedings of the 37th European Solid-State Device Research Conference*: 243-246.
- Zhu, W. J., Perebeinos, V., Freitag, M., Avouris, P. (2009). Carrier scattering, mobilities, and electrostatic potential in monolayer, bilayer, and trilayer graphene. *Physical Review B*. 80(23): 235402.