

FUZZY NEURAL NETWORKS WITH GENETIC
ALGORITHM-BASED LEARNING METHOD

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To my father, and family members

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ABSTRACT

This thesis is on the reasoning of artificial neural networks based on granules for both crisp and uncertain data. However, understanding the data in this way is difficult when the data is so complex. Reducing the complexity of the problems that these networks are attempting to learn as well as decreasing the cost of the learning processes are desired for a better prediction. A suitable prediction in artificial neural networks depends on an in-depth understanding of data and fine tracking of relations between data points. Inaccuracies of the prediction are caused by complexity of data set and the complexity is caused by uncertainty and quantity of data. Uncertainties can be represented in granules, and the reasoning based on granules is known as granular computing. This thesis proposed an improvement of granular neural networks to reach an outcome from uncertain and crisp data. Two methods based on genetic algorithms (GAs) are proposed. Firstly, GA-based fuzzy granular neural networks are improved by GA-based fuzzy artificial neural networks. They consist of two parts: granulation using fuzzy c-mean clustering (FCM), and reasoning by GA-based fuzzy artificial neural networks. In order to extract granular rules, a granulation method is proposed. The method has three stages: construction of all possible granular rules, pruning the repetition, and crossing out granular rules. Secondly, the two-phase GA-based fuzzy artificial neural networks are improved by GA-based fuzzy artificial neural networks. They are designed in two phases. In this case, the improvement is based on alpha cuts of fuzzy weight in the network connections. In the first phase, the optimal values of alpha cuts zero and one are obtained to define the place of a fuzzy weight for a network connection. Then, in the second phase, the optimal values of middle alpha cuts are obtained to define the shape of a fuzzy weight. The experiments for the two improved networks are performed in terms of generated error and execution time. The results tested were based on available rule/data sets in University of California Irvine (UCI) machine learning repository. Data sets were used for GA-based fuzzy granular neural networks, and rule sets were used for GA-based fuzzy artificial neural networks. The rule sets used were customer satisfaction, uranium, and the datasets used were wine, iris, servo, concrete compressive strength, and uranium. The results for the two-phase networks revealed the improvements of these methods over the conventional one-phase networks. The two-phase GA-based fuzzy artificial neural networks improved 35% and 98% for execution time, and 27% and 26% for the generated error. The results for GA-based granular neural networks were revealed in comparison with GA-based crisp artificial neural networks. The comparison with other related granular computing methods were done using the iris benchmark data set. The results for these networks showed an average performance of 82.1%. The results from the proposed methods were analyzed in terms of statistical measurements for rule strengths and classifier performance using benchmark medical datasets. Therefore, this thesis has shown GA-based fuzzy granular neural networks, and GA-based fuzzy artificial neural networks are capable of reasoning based on granules for both crisp and uncertain data in artificial neural networks.

ABSTRAK

Tesis ini menyelidik taakulan bagi rangkaian neural buatan berdasarkan granul untuk kedua-dua data jelas dan tidak jelas. Kaedah pemahaman data melalui cara ini adalah sukar apabila kandungan data adalah kompleks. Untuk mengurangkan kekompleksan masalah yang cuba dipelajari oleh rangkaian ini dan juga mengurangkan kos proses pembelajarannya, teknik ramalan yang lebih baik adalah diperlukan. Ramalan yang sesuai dalam rangkaian neural buatan bergantung kepada kebolehan untuk memahami isi kandungan data dengan mendalam dan juga kebolehan untuk mengenal pasti hubungan antara data. Ketakpastian dan kepelbagaian jenis data juga akan menjadikan hasil ramalan yang tidak tepat. Ketakpastian terhadap jenis data disebabkan oleh kekompleksan jenis data tersebut dan juga set data yang mengandungi tahap ketakpastian yang kompleks. Ketakpastian boleh diwakili dengan granul dan taakulan yang dikenali sebagai pengkomputeran granular. Tesis ini menggunakan rangkaian neural granular untuk mencapai hasil daripada data yang tidak pasti dan jelas. Dua kaedah telah diperkembangkan berdasarkan algoritma genetik. Rangkaian granular kabur berasaskan algoritma genetik (GA) telah diperkembangkan menggunakan rangkaian neural buatan kabur berasaskan GA. Rangkaian neural granular kabur berasaskan GA mengandungi dua bahagian: granulasi menggunakan pengelompokan min-c kabur, dan taakulan oleh rangkaian neural buatan kabur berasaskan GA. Untuk mengekstrak peraturan granular kaedah granulasi yang diterokai mengandungi tiga peringkat, iaitu pembinaan semua peraturan granular yang mungkin, pemangkasan data yang berulang dalam set data dan pengurangan peraturan granular yang telah digunakan. Rangkaian neural buatan kabur berasaskan GA berfasa dua telah direka bentuk dalam dua fasa. Dalam keadaan ini peningkatannya berdasarkan kepada nilai *alfa-cut* dalam rangkaian neural. Dalam fasa pertama nilai optimum *alfa-cut* adalah sifar dan boleh diperolehi bagi menentukan pemberat set kabur kepada rangkaian neural. Dalam fasa kedua nilai optimum untuk *alfa-cut* tengah diperolehi untuk menentukan bentuk set kabur. Uji kaji untuk dua rangkaian neural yang telah dipertingkatkan telah dijalankan berdasarkan kepada jumlah ralat yang dihasilkan dan masa yang diambil bagi melaksanakan uji kaji tersebut. Hasil uji kaji berdasarkan set data mesin pembelajaran repositori di University of California Irvine (UCI). Set data yang digunakan untuk rangkaian neural granular kabur berasaskan GA dan set peraturan digunakan untuk rangkaian neural buatan kabur. Set peraturan yang digunakan adalah kepuasan pelanggan dan uranium manakala set data yang digunakan ialah arak, iris, servo, kekuatan mampat konkrit dan uranium. Hasil untuk rangkaian dua fasa mendedahkan keunggulan kaedah ini berbanding dengan rangkaian konvensional satu fasa. Rangkaian dua fasa telah meningkat sebanyak 35% dan 98% untuk masa pelaksanaan dan 27% dan 26% untuk ralat umum. Hasil untuk rangkaian neural berasaskan GA didedahkan berbanding dengan rangkaian neural buatan jelas berasaskan GA. Sementara itu perbandingan dengan kaedah pengkomputeran granular yang lain yang berkaitan dijalankan menggunakan set data penanda aras iris. Hasil untuk rangkaian ini menunjukkan prestasi purata sebanyak 82.1%. Hasil daripada kaedah yang disarankan telah dianalisis dari segi statistik, kekuatan aturan dan pengelasan tenaga menggunakan penanda aras set data perubatan. Oleh itu tesis ini menunjukkan bahawa rangkaian neural granular kabur berasaskan GA dan rangkaian neural buatan kabur berasaskan GA mampu sebagai taakulan bagi rangkaian neural buatan berdasarkan granul untuk kedua-dua data jelas dan tidak jelas.

TABLE OF CONTENTS

CHAPTER	TITLE	PAGE
	DECLARATION	ii
	DEDICATION	iii
	ACKNOWLEDGEMENT	iv
	ABSTRACT	v
	ABSTRAK	vi
	TABLE OF CONTENTS	vii
	LIST OF TABLES	xi
	LIST OF FIGURES	xvi
	LIST OF ABBREVIATION	xxiv
	LIST OF APPENDICES	xxv
1	INTRODUCTION	1
	1.1 Introduction	1
	1.2 Problem background	3
	1.3 Problem statement	12
	1.4 Thesis aim	13
	1.5 Thesis objectives	14
	1.6 Thesis scope	14
	1.7 Significance of thesis	15
	1.8 Contribution of thesis	15
	1.9 Thesis plan	16
	1.10 Organization of thesis	16
	1.11 Summary	18
2	LITERATURE REVIEW	19
	2.1 Introduction	19

2.2	Soft computing techniques	21
2.2.1	Fuzzy sets theory	21
2.2.2	Genetic algorithms (GAs)	30
2.3	Granular computing	37
2.3.1	Structure of granular computing	38
2.3.2	Fuzzy information granulation (FIG)	44
2.3.3	Granular neural networks (GNNs)	48
2.4	Hybrid approaches	61
2.4.1	GA-based fuzzy artificial neural networks (GA-FANNs)	61
2.4.2	GA-based fuzzy granular neural networks (GA-FGNNs)	65
2.5	Data sets	69
2.5.1	Liu rule set (Liu, et al., 2005)	71
2.5.2	Aliev rule set (Aliev, et al., 2001)	72
2.5.3	Customer satisfactory rule set (Fasanghari, et al., 2008)	73
2.5.4	Uranium data set (Staudenrausch, et al., 2005)	74
2.5.5	Uranium data set (Houston, et al., 1987)	75
2.5.6	Wine data set	75
2.5.7	Servo data set	76
2.5.8	Iris data set	76
2.5.9	Concrete compressive strength data set	77
2.5.10	Hepatitis data set	77
2.5.11	Pima Indian diabetes data set	77
2.5.12	Liver disorder data set	78
2.6	Summary	78
3	METHODOLOGY	80
3.1	Introduction	81
3.2	General research framework	81
3.3	Data preparation	82
3.4	Data division	83
3.5	Proposed GA-based fuzzy granular neural networks	83
3.5.1	Proposed granulation	85
3.5.2	Integration and reasoning	96
3.6	GA-based fuzzy artificial neural networks	98

3.6.1	One-phase GA-based fuzzy artificial neural networks	102
3.6.2	Proposed two-phase GA-based fuzzy artificial neural networks	103
3.7	Validation and measurements	106
3.7.1	K-fold validation	106
3.7.2	Error and time	107
3.7.3	Rule strength measurements	107
3.7.4	Goodness-of-fit measurements	108
3.7.4.1	Lilliefors test	108
3.7.4.2	Pearson test	109
3.7.5	Classifier performance measurements	109
3.8	Summary	112
4	RESULTS OF THE PROPOSED METHODS	114
4.1	Introduction	115
4.1.1	General framework	115
4.2	Proposed GA-based fuzzy granular neural networks	116
4.2.1	Granulation	119
4.2.2	Integration and reasoning	121
4.3	Improved two-phase GA-based fuzzy artificial neural networks	124
4.3.1	Testing on Aliev and Liu data sets	125
4.3.1.1	Phase definitions	126
4.3.1.2	Superiority of the improved method	127
4.3.1.3	Accuracy of the improved method	130
4.3.1.4	Testing and prediction	133
4.3.1.5	Comparison with earlier works	135
4.4	Testing on a uranium data set	137
4.5	Testing on e-commerce data set	140
4.5.1	Testing the designed evaluator systems	143
4.5.2	Accuracy of designed evaluator systems	147
4.6	Discussion	150
4.7	Summary	153
5	TATISTICAL ANALYSIS OF THE PROPOSED METHODS	155
5.1	General framework	155
5.2	Phase I: distribution analysis	156

5.2.1	Statistical results of one-phase method	158
5.2.2	Statistical results of proposed two-phase method	166
5.3	Phase II: Rule strength analysis	179
5.4	Phase III: Classifier performance analysis	185
5.5	Discussion	189
5.6	Summary	190
6	CONCLUSION	191
6.1	Introduction	191
6.2	Summary of work	193
6.3	Research findings and contributions	194
6.4	Limitations of work	195
6.5	Conclusion	196
6.6	Future works	196
	REFERENCES	198
	Appendices A-D	205-212

LIST OF TABLES

TABLE NO	TITLE	PAGE
1.1	Related researches on granular computing and descriptions of each from the soft computing perspective.	4
1.2	List of a few proposed learning methods for fuzzy artificial neural networks.	10
1.3	Learning convergences of the methods in Table 1.2.	11
1.4	Speed of convergences of the methods in Table 1.2.	12
2.1	Major studies on granular computing streaming to granular neural networks.	42
2.2	Different studies using the notion of information granulation.	47
2.3	Some studies on granular classification models.	48
2.4	List of proposed learning methods for fuzzy artificial neural networks (FANNs).	59
2.5	The major studies for GA-based fuzzy artificial neural networks (FANNs).	64
2.6	The data sets are used here based on their nature; inexact data sets are used for fuzzy artificial neural networks and exact data sets are used for granular neural networks.	70
2.7	Liu data set (Liu, et al., 2005) with inputs X_1 and X_2 and outcome $f(X_2; X_2)$.	71
3.1	Calculating the weights for the G-rules and eliminating repeated G-rules.	94

3.2	Pruning the multi-out G-rules based on the example of Table 3.1.	96
3.3	Eight possible granular rule bases that can be obtained based on Table 3.2.	96
4.1	Data sets used in this chapter.	116
4.2	Obtained fuzzy clusters for each data set.	120
4.3	Number of all constructed granular rules before pruning for each data set.	121
4.4	Number of final granular rules after pruning for each data set.	121
4.5	Final granular rules, abbreviated as G-rules, for each data set after pruning; they are given in linguistic forms of low and high, abbreviated as L and H.	121
4.6	The results of GA-based fuzzy granular neural networks compared to GA-based crisp artificial neural networks, where error and time are listed based on improvement obtained from GA-based fuzzy granular neural networks.	122
4.7	Comparison of one- and two-phase GA-based methods using the fitness function F_p given in equation (10).	129
4.8	Comparison results for two-phase GA-based methods using four methods of fitness functions FA , FP .	130
4.9	Comparison results of training for one and two-phase GA-based methods using the data set of Table A1 in Appendix A.	131
4.10	Comparison results of training for one- and two-phase GA-based methods using the data set of Table A2 in Appendix A.	131
4.11	Inputs to the trained network based on a two-phase method using data set Table A1 from Appendix A.	134
4.12	Predicted outcomes from the trained network based on a two-phase GA-based method for input values of Table 4.11.	134

4.13	Explanations on comparing the proposed method with the earlier work (Mashinchi, 2007).	137
4.14	Summary of comparisons between proposed method and other methods.	137
4.15	Estimation of GA-based fuzzy artificial neural networks based on C1 of Appendix C.	140
4.16	Estimation of GA-based fuzzy artificial neural networks based on C4 in Appendix C.	140
4.17	The data to validate the use of GA-based fuzzy artificial neural networks for a customer satisfactory evaluator system.	143
4.18	The training result of one-phase and two-phase evaluator systems based on data set Table 4.17.	144
4.19	Two new customers' opinions to test the trained evaluator systems.	144
4.20	The results of training based on Table B1 of Appendix B.	148
4.21	The testing results of trained one- and two-phase evaluator systems based on three new customers.	148
4.22	The performance of GA-based fuzzy granular neural networks on iris data set compared to other methods addressed in a work (Daniel, et al., 2009).	151
4.23	The comparison results of one- and two-phase GA-based methods, where the error and time are given in percentages based on the two-phase method.	152
5.1	Statistical values of Figures 5.3 and 5.4.	160
5.2	Lilliefors test, at 5% significance level, for one-phase method based on Liu rule set.	160
5.3	Pearson test (Nakagawa, et al., 2012) for one-phase method based on Liu rule set (Li, et al., 2005).	161
5.4	Statistical values of Figure 5.5 and Figure 5.6.	163
5.5	Lilliefors test (Liu, et al., 2005) for one-phase method based on Aliev rule set (Aliev, et al., 2001).	163
5.6	Pearson test (Nakagawa, et al., 2012) for one-phase method based on Aliev rule set.	164

5.7	Overall testing results of one-phase method.	165
5.8	Overall testing results of statistical test for one-phase method (✓ indicates for normal distribution).	165
5.9	Statistical values of training and testing results from first and second phases shown in Figure 5.7, 5.8, 5.9 and 5.10.	168
5.10	Lilliefors test (Lilliefors, 1967) on training results of first and second phases on Liu rule set (Liu, et al., 2005).	169
5.11	Pearson test (Nakagawa, et al., 2012) on training results of first and second phase on Liu rule set (Liu, et al., 2005).	169
5.12	Statistical values of Figures 5.11, 5.12, 5.13 and 5.14.	174
5.13	Lilliefors test (Lilliefors, 1967) for two-phase method based on Aliev rule set (Aliev, et al., 2001).	175
5.14	Pearson test (Nakagawa, et al., 2012) for two-phase method based on Aliev rule set (Aliev, et al., 2001).	176
5.15	Overall testing results of statistical test for two-phase method (✓ indicates for normal distribution).	177
5.16	Overall testing results of two-phase method.	178
5.17	The strengths of extracted granular rules from wine data set.	181
5.18	The strengths of extracted granular rules from servo data set.	182
5.19	The strengths of extracted granular rules from iris data set.	182
5.20	Comparison of results based on the mean of values for extracted granular rules.	183
5.21	Fuzzy clustering on data sets variables into high and low.	186
5.22	Extracting the granular rules from based on clusters in Table 5.21.	187
5.23	Classification rates on each benchmark data set.	187
5.24	Overall results of distribution analysis.	189
5.25	Overall classification rates.	190
A 1	Liu dataset (Li, et al., 2005).	205
A 2	Aliev dataset (Aliev, et al., 2001).	206
B 1	The dataset to validate the using GA-based fuzzy artificial neural networks for the evaluator systems.	207

B 2	The dataset to find the capability of using GA-based fuzzy artificial neural networks for the evaluator systems.	208
C 1	Unsure dataset (Staudenrausch, et al., 2005) modeled in the form of fuzzy values.	209
C 2	Crisp dataset before granulation (Houston, et al., 1987).	210
C 3	Clusters definition into low and high for each chemical element of dataset of (Houston, et al., 1987) in the form of fuzzy numbers (a_1, a_2, a_3).	210
C4	Linguistic rules correspondent with dataset of (Houston, et al., 1987), which is obtained after granulations and rule pruning.	211

LIST OF FIGURES

FIGURE NO	TITLE	PAGE
1.1	Granular neural networks and fuzzy neural networks in conjunction with soft computing and granular computing areas.	4
1.2	An example of crisp modeling in dealing with a function.	5
1.3	An example of fuzzy modeling in dealing with a function.	6
1.4	Different optimum explorations for fitness landscape (Weise, 2007).	7
1.5	A well-shaped fuzzy value represented with eleven α -cuts.	8
1.6	A triangular fuzzy value with two α -cuts.	8
1.7	Different types of fuzzy numbers, triangular and trapezoidal in symmetrical and asymmetrical representation.	9
2.1	An overall view of the involved approaches to derive the combined approaches.	19
2.2	An overall view of the basic and combined models used in this thesis. The symbol \oplus indicates the combination of two models (note: FIG-CANN is denoted for fuzzy information granulation based crisp artificial neural networks, and, CIG-FANN is denoted for crisp information granulation based fuzzy artificial neural networks).	20
2.3	The role of fuzzy sets with respect to the future and past in collaboration with genetic algorithms (GAs) and granular neural networks (GNNs).	24
2.4	Simple fuzzy numbers in respect to the normality and convexity, where D and E are triangular fuzzy numbers.	26

2.5	Well-shaped fuzzy numbers in respect to the normality and convexity.	26
2.6	Nested intervals in a normal and convex fuzzy number.	27
2.7	Computation of $C = A + B$, based on equation (2.5).	28
2.8	Computation of $C = A \times B$, based on equation (2.9).	29
2.9	General schema of genetic algorithms.	33
2.10	An example of a roulette wheel selection operator in genetic algorithms.	34
2.11	A typical crossover.	35
2.12	A uniform crossover.	35
2.13	An example of the mutation function.	36
2.14	An example of the idea of granular computing by drawing different approaches under one computational unit, which is given by this thesis based on the studies in the literature.	39
2.15	The procedures of emerging an approach under the model of granular computing, which is modified by this thesis based on studies in the literature.	40
2.16	A general model of information granulation.	45
2.17	Crisp artificial neural networks as the conventional class, which is able to process crisp numerical values.	50
2.18	Granular neural networks as a new class for artificial neural networks, which is able to process the non-numeric values formed in granules.	50
2.19	An example of a descriptive neural network in three-layer feed-forward architecture.	52
2.20	An example of a higher-level of granular neural networks under the model of granular computing.	52
2.21	Conventional artificial neural networks contrast to the corresponding ones in the hybrid with the fuzzy model.	54
2.22	Classification of neuro-fuzzy systems (Liu, et al., 2004).	54
2.23	Regular fuzzy neuron (Liu, et al., 2004).	55
2.24	Topological structure of fuzzy artificial neural network (Liu, et al., 2004).	57

2.25	General scheme of GA-based fuzzy artificial neural networks.	62
2.26	A three-layer, feed-forward fuzzy artificial neural network, where each fuzzy value can be obtained by genetic algorithms.	62
2.27	Involved techniques to improve the granular neural networks based on genetic algorithms.	66
2.28	Structure of GA-based fuzzy granular neural networks.	67
2.29	The structure of granulation, in Figure 2.25, for a granular neural network.	68
2.30	Linguistic variables of the Liu rule set (Li, et al., 2005) represented in alpha cuts.	72
2.31	Customer evaluation system.	73
2.32	Customer service satisfaction index (Fasanghari, et al., 2008).	74
3.1	General research framework for methodology.	82
3.2	General methodology of GA-based crisp artificial neural networks.	83
3.3	General methodology of GA-based fuzzy granular neural networks.	84
3.4	Granulation of crisp data to extract the granular rule base.	85
3.5	Extraction of the granular rules.	86
3.6	The steps of extracting the granular-rules.	87
3.7	The steps of granulation to extract the granular rules from a crisp data set.	88
3.8	Detail of step 2 of Figure 3.7 to find the intersected parts of two clusters.	89
3.9	An example for intersecting parts of two granules in a data set.	90
3.10	Detail of Step 3 of Figure 3.7 to find all possible granular rules.	91
3.11	Finding all possible rules based on Figure 3.10, following the example in Figure 3.9.	92
3.12	Detail of Step 4 of Figure 3.7, to prune the repeated granular rules.	93

3.13	Details of Step 5 in Figure 3.7, to prune multi-output granular rules.	95
3.14	The methodology of integration and reasoning in GA-based fuzzy granular neural networks.	97
3.15	Different types of fuzzy neural networks vary based on the values of biases and weights.	99
3.16	Three-layer fuzzy neural network architecture.	100
3.17	The steps of one-phase GA-based fuzzy artificial neural networks	102
3.18	Algorithm of one-phase GA-based fuzzy artificial neural networks.	103
3.19	Schema of two-phase GA-based learning method.	104
3.20	Flowchart of two-phase GA-based learning method.	105
3.21	K-fold cross validation.	106
3.22	Framework to study GA-based granular neural networks.	112
3.23	Framework to study GA-based fuzzy artificial neural networks.	113
4.1	General framework to conduct the results.	115
4.2	Preparation of the test data for GA-based fuzzy granular neural networks.	116
4.3	Steps used in implementing GA-based artificial neural networks and GA-based fuzzy granular neural networks.	118
4.4	The steps of granulation to extract the granular rules from a crisp data set.	119
4.5	The flowchart of defuzzifier.	122
4.6	Results of phase definitions (shown in the form of first phase% - second phase%) using the data set of Table A(1), where the overall error is computed based on errors from the first and second phases.	126
4.7	Results of phase definitions (shown in the form of: first phase% - second phase%) using the data set of Table A2, where the overall error is computed based on errors from the first and second phases.	127

4.8	Membership functions for Small, Medium and Large, where vector X indicates real numbers and μ_x indicates the membership function.	128
4.9	Training results of one- and two-phase GA-based methods using the data sets of Table A1 of Appendix A.	128
4.10	Training results of one- and two-phase GA-based methods using the data sets of Table A2 of Appendix A.	129
4.11	Training convergence of the two-phase GA-based method using the data set of Table A1 in Appendix A.	132
4.12	Training convergence of the two-phase GA-based method using the data set of Table A2 in Appendix A.	132
4.13	The outcomes from a trained network based on data set of Tables A1 in Appendix A.	133
4.14	An example of a multimodal error function (Weise, 2007).	136
4.15	Learning behavior of designed GA-based fuzzy artificial neural networks in terms of generated error by increasing the training data.	138
4.16	Learning time behavior of designed GA-based fuzzy artificial neural networks by increasing the training data.	138
4.17	Learning behavior of designed GA-based fuzzy artificial neural networks in terms of generated error using different populations.	139
4.18	General structure of the one-phase evaluator system.	141
4.19	General structure of the two-phase evaluator system.	141
4.20	The steps of the one-phase evaluator system.	142
4.21	The steps of the two-phase evaluator system.	142
4.22	Two customers' opinions depicted equivalent to Table 4.19.	143
4.23	Predicted gap for the first test customer using the trained one-phase evaluator system.	145
4.24	Predicted gap for the second test customer using the trained one-phase GA-based evaluator system.	145
4.25	Different assignments to the first and second phases of the two-phase evaluator system using the data set of Table B1 in Appendix B.	146

4.26	Predicted gap for the first test customer using the trained two-phase GA-based evaluator system.	146
4.27	Predicted gap for the second test customer using the trained two-phase GA-based evaluator system.	147
4.28	The variation of generated error in different populations using the one-phase GA-based evaluator system.	148
4.29	Different cases of allotments for the first and second phases of the two-phase GA-based evaluator system using the Table B1 data set.	149
4.30	The variation of generated error using the two-phase GA-based evaluator system.	150
5.1	General framework to conduct the analysis results.	156
5.2	The framework for distribution analysis (phase I).	157
5.3	Results of one-leave-out training for one-phase GA-based method using Liu rule set.	158
5.4	Results of one-leave-out testing for one-phase GA-based method using Liu rule set using.	159
5.5	Results of one-leave-out training for one-phase GA-based method base on Aliev rule set (Aliev, et al., 2001).	161
5.6	Results of one-leave-out testing for one-phase method based on Aliev rule set (Aliev, et al., 2001).	162
5.7	Results of one-leave-out training for first phase of two-phase GA-based method using Liu rule set (Liu, et al., 2005).	166
5.8	Results of one-leave-out training for second phase of two-phase GA-based method using Liu rule set (Liu, et al., 2005).	167
5.9	Results of one-leave-out testing for first phase of two-phase GA-based method using Liu rule set (Li, et al., 2005).	167
5.10	Results of one-leave-out testing for second phase of two-phase GA-based method using Liu rule set (Li, et al., 2005).	168
5.11	Results of one-leave-out training for first phase of two-phase GA-based method using Aliev rule set (Aliev, et al., 2001).	170
5.12	Results of one-leave-out training for second phase of two-phase GA-based method using Aliev rule set (Aliev, et al., 2001).	171

5.13	Results of one-leave-out testing for first phase of two-phase GA-based method using Aliev rule set (Aliev, et al., 2001).	172
5.14	Results of one-leave-out testing for second phase of two-phase GA-based method using Aliev rule set (Aliev, et al., 2001).	173
5.15	Comparison of results of normality and β -distribution for one-phase and two-phase methods.	178
5.16	Overall test results of normality and β -distribution for one-phase and two-phase methods.	178
5.17	The framework for rule strength analysis (Phase II).	180
5.18	Comparison of results based on Table 5.20.	184
5.19	Comparison of results for confidence constraint referred in Table 4.	184
5.20	Framework to obtain the results for imbalanced analysis.	185
5.21	Obtained classification rates in comparison.	188
5.22	Obtained positive predictive values in comparison.	188
5.23	Obtained negative predictive values in comparison.	188

LIST OF SYMBOLS

\tilde{w}	-	Fuzzy weights of fuzzy artificial neural networks
$\bigcup_{i=0}^n i$	-	Union i , where $i = 0$ to n
$\sum_{i=0}^n i$	-	Summation i , where $i = 0$ to n
α_l^L	-	Left boundary of α -cut at level l
α_l^R	-	Right boundary of α -cut at level l
\tilde{b}	-	Fuzzy valued bias
\tilde{X}_n	-	Fuzzy valued input
\tilde{O}_q	-	q^{th} fuzzy outcome
\widetilde{Inter}	-	Intersection of edges in FANNs
\widetilde{agg}	-	Aggregation of edges in FANNs
F_P	-	Proposed fitness function
F_A	-	Aliev fitness function
D_l^L	-	Left boundaries of α -cuts target values
D_l^R	-	Right boundaries of α -cuts for target values
O_l^L	-	Left boundaries of α -cuts outcome values
O_l^R	-	Right boundaries of α -cuts outcome values
$f_{net}(\tilde{X}_1; \tilde{X}_2)$	-	Actual outcome from input \tilde{X}_1, \tilde{X}_2

LIST OF ABBREVIATION

ANN	-	Artificial Neural Network
CANN	-	Crisp Artificial Neural Network
PR	-	Probabilistic Reasoning
EC	-	Evolutionary Computing
NC	-	Neuro Computing
FL	-	Fuzzy Logic
FANN	-	Fuzzy Artificial Neural Network
FIG	-	Fuzzy Information Granulation
GC	-	Genetic Computing
GA	-	Genetic Algorithm
GrC	-	Granular Computing
CGNN	-	Crisp Granular Neural Network
FGNN	-	Fuzzy Granular Neural Network
GNN	-	Granular Neural Network
GBLM	-	Genetic Based Learning Method
2P-GBLM	-	2 Phase Genetic Based Learning Method
H	-	High
L	-	Low
TFIG	-	Theory of Fuzzy Information Granulation
TIG	-	Theory of Information Granulation
MSE	-	Mean of Squared Error
SE	-	Squared Error
SC	-	Soft Computing

LIST OF APPENDICES

APPENDIX	TITLE	PAGE
A	Standard fuzzy rule sets Liu (Liu, et al., 2005) and Aliev (Aliev, et al., 2001)	205
B	Customer satisfactory dataset (Fasanghari, et al., 2008)	207
C	Uranium datasets (Staudenrausch, et al., 2005)(Houston, et al., 1987)	209
D	List of Publication and Recognition	212

CHAPTER 1

INTRODUCTION

1.1 Introduction

This chapter presents a brief introduction to the notions that are used to achieve the aim of this thesis. The aim is to use granular computing for problems solving. The introduced notions are granular computing, granular neural networks, fuzzy artificial neural networks, fuzzy information granulation, generic algorithms and fuzzy sets theory. The reason for this study is to investigate the aim of artificial computations that is to solve a problem with the least amount of cost and the best accuracy. Problems become more difficult to be solved when their corresponding data sets are large or contain uncertain information. In the literature of artificial computations, there are many nature inspired computations such as evolutionary computations, artificial neural networks, artificial immune systems, swarm intelligence, etc. (Zomaya, 2006) (Kari, et al., 2008). However, there are two issues behind the proposed algorithms; which are the ability of each algorithm to solve only a particular type of problem; and their performance in solving the problem. To overcome these two issues, this thesis uses granular computing with the aid of learning and optimization mechanisms for an optimal learning from granular rules. Therefore, granular neural networks have been used for learning mechanism; meanwhile fuzzy artificial neural networks are centered in the granular neural networks. Also, the genetic algorithms (GA) are used to increase the performance of fuzzy artificial neural networks. Therefore, GA-based fuzzy artificial neural networks are used in the main part for granular neural networks.

In order to have better performance and wide applicability of computational methods, different individual models need to be unified. This has emerged in granular computing as an inspiration from the human mind. Among natural

computations as the source of inspiration for artificial computations, the human mind is known to be superior in problem solving, for example processing large and also uncertain information. The superiority of mind is spotted when an attempt is made to solve a complex problem. A problem is called complex when its components or their relations are difficult to understand. Since uncertainties are considered complexity, a problem consisting of uncertainties becomes complex. Solving complex problems is promised by the granular computing model, which has been inspired from the way that the human mind solves such problems. A major key in granular computing is granulation, which is similar to abstraction in the human mind (Zadeh, 1997). Granulation and granular computing are two similar meanings to information granulations. Historically, the notion of granular computing emerged from the theory of information granulation, which initially was proposed based on fuzziness. Similar to granular computing, the theory of fuzzy information granulation is inspired from how the human mind reacts to solve problems (Zadeh, 1997). It is known as a key in the mind-processing mechanism; a system must consider it in solving a complex problem (Zadeh, 1997).

Therefore, in this thesis, fuzzy modeling has been used for granular computation to solve complex problems. Fuzzy artificial neural networks, which are used in the center of improved granular neural networks, are the combination of fuzzy modeling and artificial neural networks. Fuzzy artificial neural networks are able to predict based on learned instances (Liu, et al., 2004) (Arotaritei, 2011). Their accuracy is highly dependent on tuned weights of network connections, and thus, the connection weights need to be optimally adjusted. This has been done in GA-based fuzzy artificial neural networks, where a genetic algorithm is used to adjust the weights (Aliev, et al., 2001). The genetic algorithms are combined with fuzzy artificial neural networks due to their strong appeal as an optimization technique (Liu, et al., 2004). The optimizations in genetic algorithms are based on the evolutionary process of generations. From an overall view, genetic algorithms are used to identify the best outcome of the results based on the optimization of the fuzzy artificial neural networks.

1.2 Problem background

Artificial neural networks have already been positioned as an important class of non-linear systems. They are highly adaptable systems that have been used for many areas of applications. Crisp artificial neural networks are primarily geared toward the intensive processing of numerical data. However, as the dimensionality of the problems increases, the computational complexity becomes visible because the sizes of the data sets grow up rapidly (Pedrycz, et al., 2001). Therefore, the weak points of crisp artificial neural networks are identified as follows:

- (i) Inability to tackle large-scale data, which causes inefficient learning within these networks, and thus predicts unsuitable outcomes.
- (ii) Inability to process non-numeric data, such as uncertainties and linguistic variables.

Regarding issue (i), there are a few ways to solve the problem. One solution is modular architectures of neural networks, which helps to break down the problem into a series of simpler subtasks and each of the subtasks is handled independently. The modularization of problems is a viable way of exploring neural architectures in the long run. Breaking down the problem for modulation is a method of simplification, which is similar to the granulation of data. Therefore, granulation is another way to solve issue (i) instead of using the concept of modularization. The granulation in the computation process can be used to solve also issue (ii). There are few granulation approaches; however, fuzzy modeling is the most appealing. The use of fuzzy models in conjunction with artificial neural networks creates granular neural networks, which can solve either issue (i) or (ii). See Figure 1.1 for the location of granular neural networks.

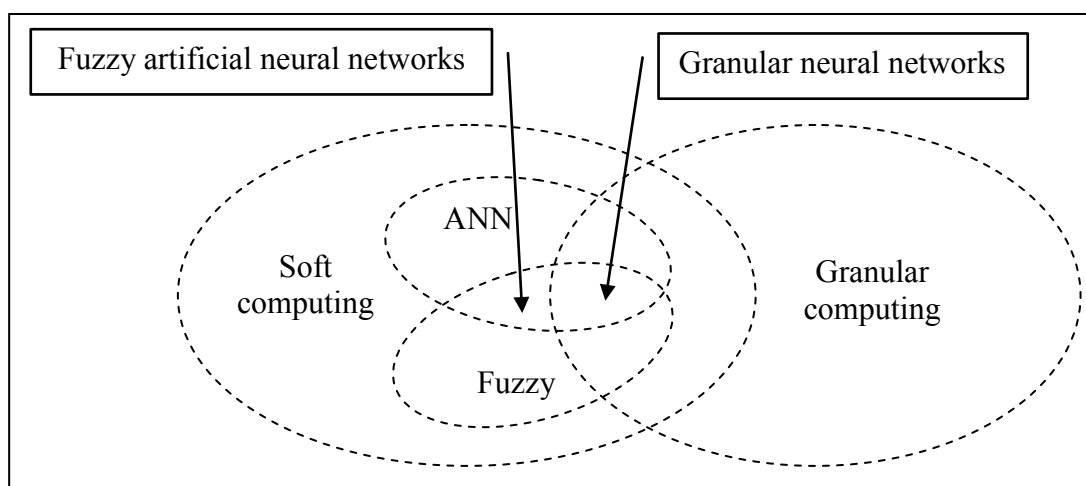


Figure 1.1: Granular neural networks and fuzzy neural networks in conjunction with soft computing and granular computing areas.

A potential solution for solving complex problems is granular computing. Since 1997, the proposal by L.A Zadeh that described granular computing, this method has become an attractive research area. However, most of the studies in this field are theoretic which needs to be studied in actual applications. Table 1.1 presents a few studies on granular computing, and the remaining issues.

Table 1.1: Related researches on granular computing and descriptions of each from the soft computing perspective.

Study	Proposed method	The problems remained unsolved
Information granulation	Proposing the idea of generalizing the information (Zadeh, 1979).	The research remained as an idea.
Reconstruction of information granulation concept	Formalization of information granulation (Zadeh, 1997).	The research does not present implementation of information granulation concept.
Labeling granular computing	Formalization of information granulation (Lin, 1997).	The research does not present implementation of granular computing.
Foundation of granular neural networks	Joint the concepts of information granulation and neural networks (Lin, 1997).	Remained as an idea.
GA-based fuzzy granular neural networks (this study)	Improves the idea of granular neural networks proposed in (Pedrycz, et al., 2001) by this study.	Decreasing the complexity of granulation when dataset is very huge.

Based on Table 1.1, this study improves the granular neural based on GA-based fuzzy artificial neural networks. Furthermore, an information granulation has been investigated to extract the fuzzy granules from the crisp data sets. Therefore, in this thesis, fuzzy sets theory has been used for granular neural networks due to the following reasons:

- (i) Fuzzy sets support the modeling of the concepts that exhibit continuous boundaries (Pedrycz, et al., 2001) (Hans-Jurgen, et al., 2012). Continuous boundaries are used to represent fuzzy values on real numbers. Fuzzy values are used to tune fuzzy artificial neural networks by genetic algorithms.
- (ii) Fuzzy sets exhibit well-defined semantics and fully meaningful conceptual entities from building modules that are identified in problem solving (Pedrycz, et al., 2001) (Hans-Jurgen, et al., 2012). The originality of the source problem is preserved after modeling it in the fuzzy concept. Meanwhile, it is possible to simplify the fuzzy modeled problem using the concept of granulation. This has been illustrated by two examples in Figure 1.2 and Figure 1.3, respectively with the illustrated modeling of a function in crisp and fuzzy representations. An advantage to fuzzy modeling, as shown in Figure 1.3, is that it does not have the crispness when moving from one segment as a concept to another. This can benefit a rule-based system to decrease the effects from a noisy data.

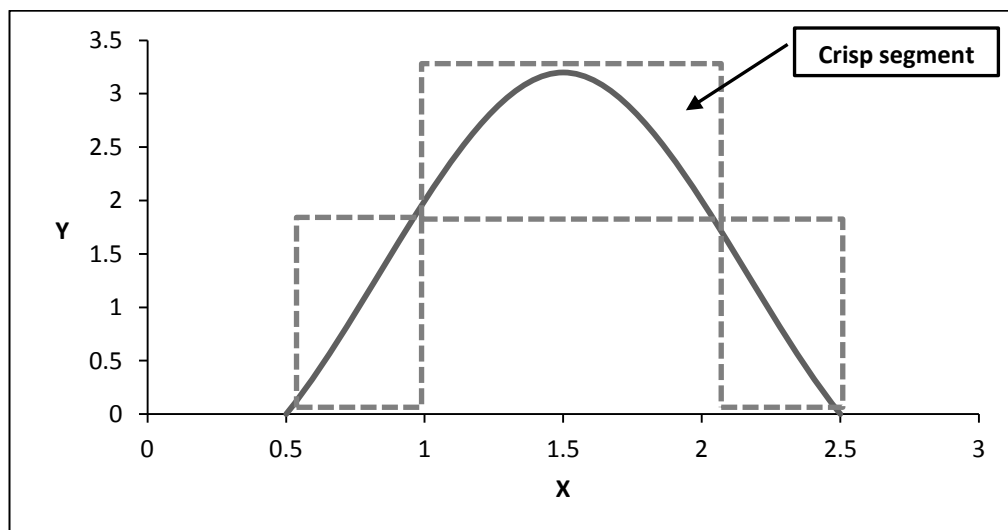


Figure 1.2: An example of crisp modeling in dealing with a function.

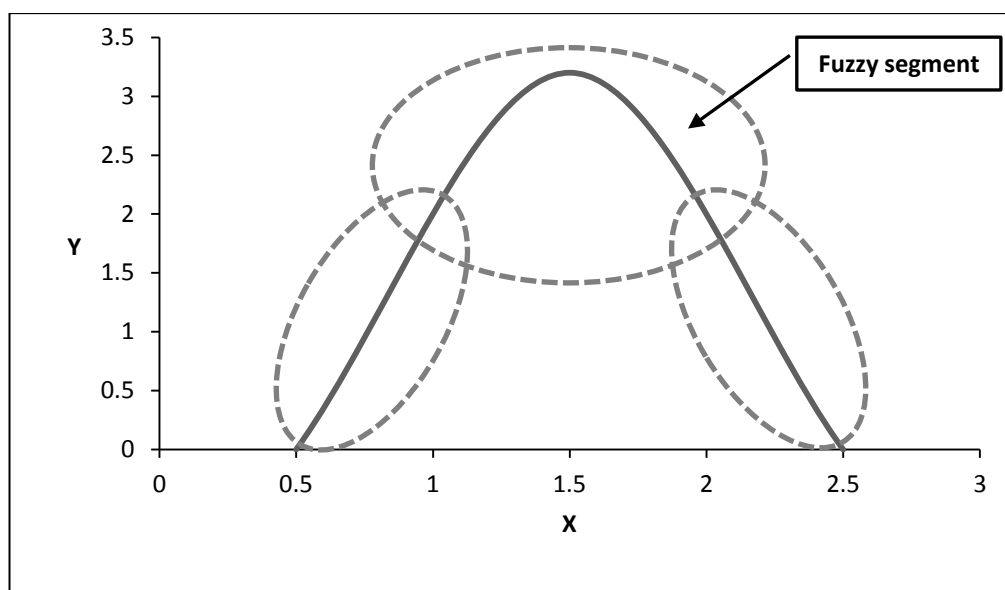


Figure 1.3: An example of fuzzy modeling in dealing with a function.

Due to the above advantages, (i) and (ii), fuzzy modeling has been combined with artificial neural networks to improve the learning mechanism (Zomaya, 2006). This is called as fuzzy artificial neural networks, which are used in this thesis as the main part of granular neural networks. As the fuzzy artificial neural networks are successfully used in learning and approximate reasoning, improvements are still required to increase their performance. There are some issues that need to be considered as follows:

- (i) Finding the global solution: The existing methods are usually being trapped into local minima when searching for the optimal network as shown in Figure 1.4. An accurate learning method is needed to avoid local minima and to find an optimal network similar to what is ideal (Arotaritei, 2011). This becomes more notable when the number of alpha cuts is increased to shape the fuzzy numbers. Having more alpha cuts increases the possibility of trapping in the local minima.

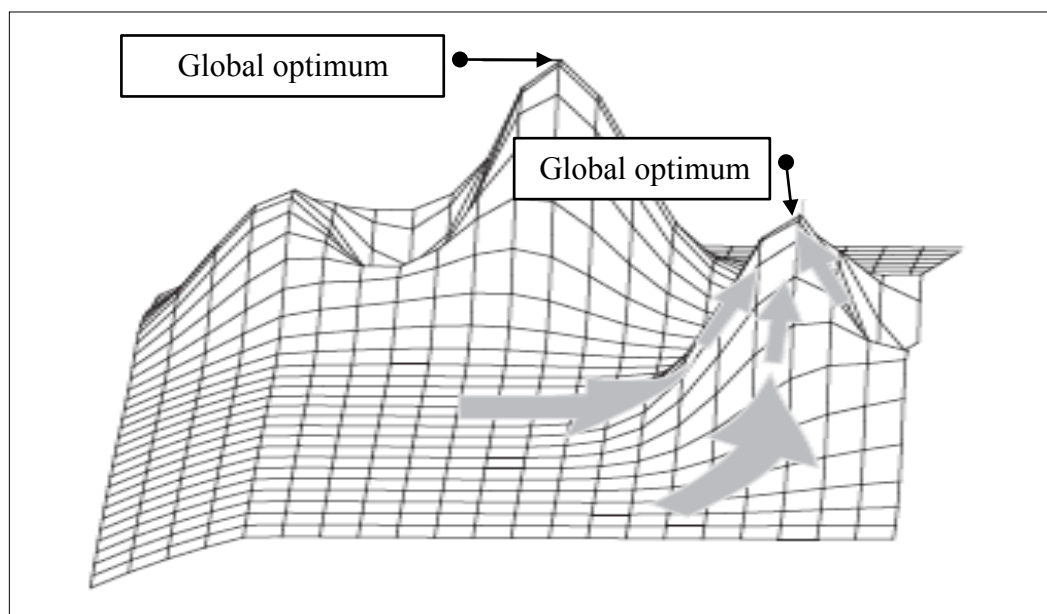


Figure 1.4: Different optimum explorations for fitness landscape (Weise, 2007).

- (ii) Increasing the convergence speed: The execution time in finding the optimal network needs to be considered in two cases. First, when learning and reasoning the outcome for an online application. Second, when a well-shaped fuzzy number is needed for a better outcome. Figures 1.5 and 1.6 shows well-shaped fuzzy value with several alpha-cuts and a triangular fuzzy value in two alpha cuts (Lee, 2005) (Hans-Jurgen, et al., 2012). The processing of a well-shaped fuzzy value is more time consuming due to two consequent reasons. First, numerous alpha cuts need to be optimized. Then, they must be optimized within an unconstrained searching space; because the optimal value for each boundary of each alpha-cut can be any real number.

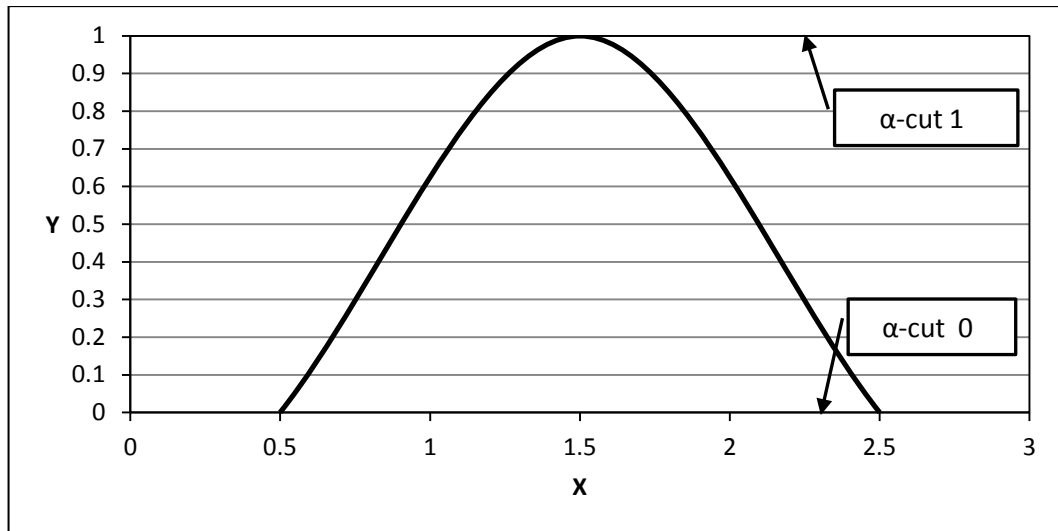


Figure 1.5: A well-shaped fuzzy value represented with eleven α -cuts.

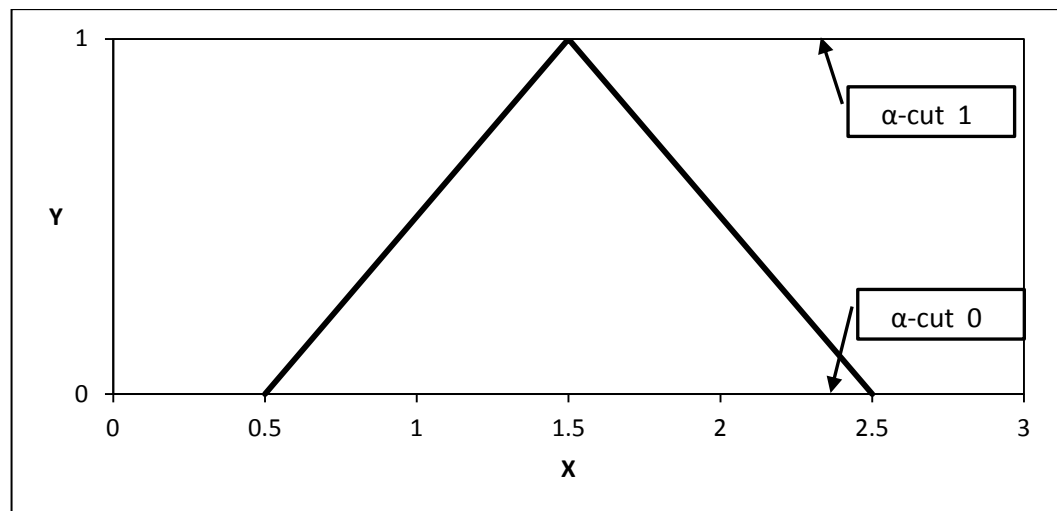


Figure 1.6: A triangular fuzzy value with two α -cuts.

- (iv) Dealing with all types of fuzzy values: Most of the existing learning methods for fuzzy artificial neural networks are unable to deal with all kinds of fuzzy numbers (Arotaritei, 2011). This would result in a lack of these networks being applicable to different applications. Therefore, a suitable fuzzy artificial neural network is required to deal with all types of fuzzy numbers as shown in Figure 1.7 (Lee, 2005).

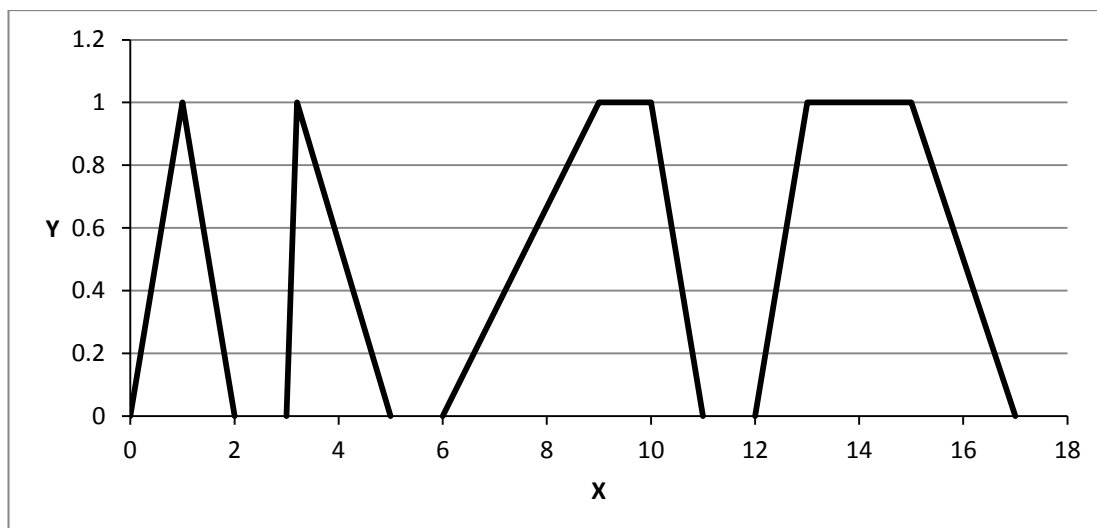


Figure 1.7: Different types of fuzzy numbers, triangular and trapezoidal in symmetrical and asymmetrical representation.

Based on the above-mentioned issues for fuzzy artificial neural networks, there are some major methods that have been proposed in the literatures. First, the direct fuzzification is proposed that fuzzifies the delta rule from the feed-forward artificial neural networks (Buckley, et al., 1992, 1995), (Hayashi, et al., 1993). This method has been rejected from a theoretical point of view (Liu, et al., 2004). Later, some learning approaches for triangular symmetric fuzzy values were proposed (Ishibuchi, et al., 1995, 2001). However, they are not able to deal with other bounded convex types of fuzzy values. Consequently, an approach based on the derivation of the min-max function has been proposed (Zhang, et al., 1996, 1999), (Liu, et al., 2004, 2005) to deal with all types of bounded convex fuzzy values. In all of the above-mentioned methods, avoiding trapping in local minima is not promised. This is due to using the back propagation algorithm, which is a local optimizer.

Another method used in studying fuzzy artificial neural networks is based on genetic algorithms. Buckley et al (Buckley, et al., 1994) introduced the use of genetic algorithms for the first time, and then Aliev et al. (Aliev, et al., 2001) reintroduced it. The reason of these two studies was using the ability of genetic algorithms to improve the fuzzy artificial neural networks. A recent works has been done for these networks by (Arotaritei, 2011). This method has the ability to deal with all types of fuzzy values that are bounded and convexed. However, the speed of learning convergence still needs to be improved. The summary of mentioned methods is given

in Table 1.2; also, a description for each method is given in Table 1.3 and Table 1.4 in terms of learning and the speed of convergences.

Table 1.2: List of a few proposed learning methods for fuzzy artificial neural networks.

Researcher	Learning method		
	Name	Advantages	Disadvantages
Buckley and Hayashi (1993)	Direct fuzzification	It proposes fuzzy artificial neural networks for the first time, which fuzzifies delta rule form feed-forward artificial neural networks.	It has been rejected from mathematical aspect.
Zhang, et al. (1996)	Derivation of min-max function	It improves fuzzy artificial neural networks to deal with all types of fuzzy values.	It does not have an adequate learning ability.
Aliev et al. (2001)	GA-based FANNs	It applies the idea of using genetic algorithms for fuzzy artificial neural networks, which were firstly sparked in 1994. It could successfully deal with all types of fuzzy values.	It does not have an adequate speed of learning convergence to be applicable for real applications.
Mashinchi (2007)	Two-phase FANNs based on BP	Proposing FANNs that learn fuzzy rule set in two phases.	Low learning convergence due to using local optimizer in the first stage.
Mashinchi, et al. (2009)	Three-term fuzzy back-propagation	The proposed method enhances the speed of back-propagation based FANNs by adding a fuzzy proportional factor.	High possibility of trapping into local minima for learning convergence process.
Arotaritei (2011)	Local crossover GA-based FANNs	Improves according to feed-forward (FFNR) and fuzzy recurrent networks (FRNN).	Needs to be compared with other methods.
This study	Two-phase GA-based FANNs	It improves the conventional GA-based method by Aliev in terms of generated error and execution time.	It does not have the ability of learning from well-shaped fuzzy values in less time.

Table 1.3: Learning convergences of the methods in Table 1.2.

Method	Learning convergence
Buckley and Hayashi (1993)	It is remained as an idea without implementation.
Derivation of min-max function (Zhang, et al., 1996)	It has an acceptable convergence for triangular fuzzy values; however, it is less promising since it is based on back propagation as a local optimizer. Main studies on this method are done by: (Zhang, et al., 1996, 1999), (Liu, et al., 2004, 2005). The remain issues to be done are as follows: <ul style="list-style-type: none"> • To guarantee the convergence • To keep the accuracy for well-shaped fuzzy values
GA-based FANNs (Aliev, et al., 2001)	It has acceptable convergence for triangular fuzzy values with more promising since it is based on GA as a global optimizer. Main studies on this method are done by: (Buckley, et al., 1994), (Aliev, et al., 2001). The remain issue to be done is as follows: <ul style="list-style-type: none"> • To keep the accuracy for well-shaped fuzzy values
Two-phase FANNs based on back-propagation (Mashinchi, 2007)	It has acceptable convergence in compared with its based method, BP; however, it is less promising since it is based on back propagation as a local optimizer. The remain issue to be done is as follows: <ul style="list-style-type: none"> • To guarantee the convergence • To keep the accuracy for well-shaped fuzzy values
Three-term fuzzy back-propagation (Mashinchi, et al., 2009)	It has acceptable convergence in compared with its based method, BP; however, there is more possibility of trapping into local minima for learning process as BP is a local optimizer. The remain issue to be done is as follows: <ul style="list-style-type: none"> • To guarantee the convergence To keep the accuracy for well-shaped fuzzy values
Local crossover GA-based FANNs (Arotaritei, 2011)	It has acceptable convergence for triangular fuzzy values with more promising since it is based on GA as a global optimizer. The remain issue to be done is as follows: <ul style="list-style-type: none"> • To keep the accuracy for well-shaped fuzzy values
Two-phase GA-based FANNs (this study)	It has better convergence with promising results, since it benefits from the optimization features of genetic algorithms. In addition, it keeps the convergence accuracy for well-shaped fuzzy values.

Table 1.4: Speed of convergences of the methods in Table 1.2.

Method	Speed of convergence
Buckley and Hayashi (1993)	It is remained as an idea without implementation.
Derivation of min-max function (Zhang, et al., 1996)	It has acceptable speed of convergence in learning triangular fuzzy values, however, there is a remained issue to be done as follows: <ul style="list-style-type: none"> • To keep the speed of convergence for well-shaped fuzzy values
GA-based FANNs (Aliev, et al., 2001)	It has acceptable convergence for triangular fuzzy values, however, there is a remained to be done as follows: <ul style="list-style-type: none"> • To keep the accuracy for well-shaped fuzzy values
Two-phase FANNs based on back-propagation (Mashinchi, 2007)	It has better speed of convergence in learning well-shaped fuzzy values in compared with its base method back-propagation. The remained to be done as follows: <ul style="list-style-type: none"> • To keep the accuracy for well-shaped fuzzy values
Three-term fuzzy back-propagation (Mashinchi and Shamsuddin, 2009)	It has better speed of convergence in compared with its base method back-propagation due to adding a fuzzy proportional factor. The remained to be done is as follows: <ul style="list-style-type: none"> • To keep the accuracy for well-shaped fuzzy values
Local crossover GA-based FANNs (Arotaritei, 2011)	It has acceptable convergence for triangular fuzzy values, however, there is a remained to be done as follows: <ul style="list-style-type: none"> • To keep the accuracy for well-shaped fuzzy values
Two-phase GA-based FANNs (this study)	It has better speed of convergence in learning well-shaped fuzzy values.

In order to improve the performance of fuzzy artificial neural networks, this thesis proposes an improved GA-based fuzzy artificial neural network to overcome the speed and the learning convergence when dealing with well-shaped fuzzy values.

1.3 Problem statement

Complex problems are known to be difficult to solve since understanding them is not easy. An example of complex problems is the unsteadiness of things such as linguistic variables. Involving uncertainties and enlargement of the problems to be

tackled cause the problems to be complex. To solve complex problems, simplification of the problems and learning mechanisms can be taken. Respectively, fuzzy granulation and fuzzy artificial neural networks can be used. The combination of these two has emerged in granular neural networks, where fuzzy artificial neural networks can play an important role. If the performance of fuzzy artificial neural networks is increased, therefore, the performance of granular neural networks can be improved. Meanwhile, the complex problem needs to be simplified in the form of a fuzzy rule base to be fed to fuzzy artificial neural networks.

Therefore, the hypothesis of this thesis is stated as follows:

“How a complex problem can be solved by granular neural networks and how fuzzy artificial neural networks can collaborate to increase the performance of granular neural networks in solving complex problems.”

1.4 Thesis aim

The aim of this thesis is to solve the complexity and uncertainty of data sets using GA-based fuzzy artificial neural networks, where reasoning based on crisp data sets is considered in granularity. In this regard, granular neural networks aim to be improved by GA-based fuzzy artificial neural networks. In addition, a rule extraction is used to transform the crisp data set into a fuzzy granular rules base. Due to the impact of GA-based fuzzy artificial neural network in learning from the granules, the efficiency of these networks on GA-based fuzzy granular neural networks are investigated. Consequently, enhancing GA-based fuzzy artificial neural networks is considered to improve the performance of granular neural networks. The improvement of GA-based fuzzy artificial neural networks is due to two reasons: the low accuracy of these networks and their centrality in GA-based fuzzy granular neural networks.

1.5 Thesis objectives

The objectives of the thesis are defined as follows:

- (i) To propose the reasoning on crisp data sets in fuzzy artificial neural networks using genetic algorithms.
- (ii) To propose the transformation of crisp data sets into fuzzy granular rule bases to train fuzzy artificial neural networks.
- (iii) To evaluate the performance of proposed fuzzy artificial neural networks based on genetic algorithms with their conventional method and crisp artificial neural networks.

1.6 Thesis scope

The scope of this thesis is defined as follows:

- (i) Three standard fuzzy rule sets and six crisp data sets are used to test the improved methods. The rule sets, and also uncertain data sets, are used to test the two-phase GA-based fuzzy artificial neural networks, and the data sets are used to test the fuzzy granular neural networks.
- (ii) The rules/data sets are available in University of California Irvine (UCI) machine learning repository, and literatures. Aliev (Aliev, et al., 2001), Liu (Liu, et al., 2005) and customer satisfaction fuzzy rule sets (Fasanghari, et al., 2008), and also a uranium data set with uncertain values (Staudenrausch, et al., 2005), are used to test two-phase GA-based fuzzy artificial neural networks. Meanwhile, the crisp data sets to test GA-based fuzzy granular neural networks are chosen based on size. Wine, servo and iris data sets from UCI repository as well as a uranium data set (Houston, et al., 1987) from the literature are used as small sizes, and concrete compressive strength data set from UCI repository is used as medium size.

- (iii) Comparisons for the improved methods are done in terms of generated error, execution time, and distribution. To this end, improved two-phase GA-based fuzzy artificial neural networks are compared with corresponding conventional method, and improved GA-based fuzzy granular neural networks are compared with GA-based crisp artificial neural networks.
- (iv) Implementations for GA-based fuzzy artificial neural networks are done using Matlab, and the implementations for GA-based fuzzy granular neural networks and GA-based artificial neural networks are done using Microsoft C++.

1.7 Significance of thesis

The significance of this thesis is as follows:

- (i) Fuzzy artificial neural networks based on genetic algorithms have been studied and improved using the notion of granular neural networks.
- (ii) Fuzzy artificial neural networks can be studied using available data sets for application, and they have been improved in terms of generated error and execution time.
- (iii) A granular rule extraction is proposed to simplify a crisp data set and represent it in fuzzy form.

1.8 Contribution of thesis

This thesis contributes to problem solving via soft computing by granulation. A granular rule extraction is given to simplify the problems, and granular learning approaches are improved for reasoning based on these granules. More specifically, three methods have been proposed in this thesis as follows:

- (i) Fuzzy artificial neural networks are able to learn from crisp data sets, and conversely, crisp data sets can be processed by fuzzy artificial neural networks.

- (ii) GA-based fuzzy artificial neural networks are improved in terms of generated error and execution time. The improved method can learn well-shaped fuzzy values represented in alpha-cuts.
- (iii) A granulation method is improved to extract fuzzy granular rules from a crisp data set. It prepares the collaboration of crisp data sets with fuzzy artificial neural networks.

1.9 Thesis plan

The direction of the thesis is taken from research background of the author on solving complex problems by human cognition. Here, granular computing and soft computing are chosen due to their similarities with human cognition. Reasoning based on granules is considered for a crisp data set, and thus a granulation method has been presented. The granulation method uses fuzzy representation, and reasoning is based on fuzzy granules. Respectively, fuzzy granulation and fuzzy artificial neural networks are used, and genetic algorithms aid in improving the learning performance. Drawing these three methods under the model of granular computing constructs GA-based granular neural networks as the main idea. The constructed method is presented to achieve the aim and objectives of this thesis. In addition, GA-based fuzzy artificial neural networks are improved due to their impact on enhancing the GA-based fuzzy granular neural networks. Eventually, contribution of this thesis is carried out for improved methods by comparison.

1.10 Organization of thesis

This chapter presents the framework of this thesis. It introduces the research field and explains the reasons for the study by reviewing the problem background. Five chapters are organized to meet the scopes and objectives. These are the introduction, a literature review, methodology, the results of the proposed fuzzy artificial neural networks, an analysis of the proposed fuzzy granular neural networks and a conclusion.

The organization of individual chapters is as follows:

- (i) Chapter 1 presents an overview of the thesis. The problem under study is introduced and the reasons for such study are described. The reasoning process by using granules for crisp data sets is highlighted. The background to the problem is given, and previously utilized approaches published in available literature are reviewed. The objectives and scope of the study are defined along with the aim of thesis. Finally, a synopsis of the likely contribution of the study is given according to the defined aims and objectives.
- (ii) Chapter 2 introduces the data sets that are used for the experiments. It also provides a review of soft computing, granular computing and the hybrid techniques that have arisen between them. Fuzzy sets theory and genetic algorithms are discussed with respect to soft computing, and fuzzy information granulation and granular neural networks are discussed with respect to granular computing.
- (iii) Chapter 3 discusses the methodology of improved methods that is used to carry out this study. Improved GA-based granular neural networks are presented, including the concepts of granulation and GA-based fuzzy artificial neural networks. The granulation method is presented in order to extract the fuzzy granular rules. The general architecture of fuzzy artificial neural networks and the schema of improved GA-based fuzzy artificial neural networks are also presented.
- (iv) Chapter 4 presents the detailed implementation and results of the improved granular neural networks. The constructed algorithms of granulation are detailed, including the fuzzy C-mean, granular rules extraction, granular rule contraction, pruning the granular rules and the defuzzifier.
- (iv) The improved method is tested using four standard crisp data sets, which are the wine, servo, iris and concrete compressive strength data sets. The results of improved GA-based granular neural networks are compared with those of other methods in the literature using the benchmarked iris data set. Using the rest of the data sets, they are compared with the results of corresponding GA-based crisp artificial neural networks to contrast granular reasoning against crisp reasoning. This chapter also presents the detailed implantation and results of

improved GA-based fuzzy artificial neural networks that are given in Chapter 4.

- (v) Chapter 5 reveals the analysis results for distribution, rule strength, and classifier performance. The results are obtained from the proposed methods: two-phase GA-based fuzzy artificial neural networks, granulation, and GA-based fuzzy granular neural networks. The results are carried out in compared with one-phase GA-based fuzzy artificial neural networks and GA-based crisp artificial neural networks, which are based on three data sets: Liver disorder, hepatitis, and diabetes.
- (vi) Chapter 6 discusses the work that has been done to complete this study. The proposed approaches are discussed and the work is summarized to conclude the results and analysis of Chapter 4. Finally, the future work is addressed in this chapter.

1.11 Summary

This chapter introduces the thesis by presenting the framework of the study. six chapters are defined to obtain the aims and objectives. Some notions are reviewed, such as granular computing, granular neural networks, fuzzy information granulation, fuzzy artificial neural networks, fuzzy sets theory and genetic algorithms. These notions are discussed according to their relation to the three improved methods of this thesis. The improved methods are two-phase GA-based fuzzy artificial neural networks, GA-based fuzzy granular neural networks and granulation. Particularly, the major studies in the literature for granular neural networks and GA-based fuzzy artificial neural networks are reviewed. Finally, the contributions of this thesis are given according to the aims and objectives, and the organization of the thesis has been presented.

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