

PLASTIC BEHAVIOUR OF STRENGTHENED COLD-FORMED STEEL
SECTION

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To my God, Allah *'azza wa jalla*
Then to my beloved parents, parents in law, wife and children

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ABSTRACT

To date, the use of cold-formed steel on single storey industrial buildings particularly as structural element of a portal frame is restricted. Mostly, its application is as roof and wall framing, cladding, purlins and rails. Compared with hot-rolled steel, the use of cold-formed steel on a building has advantages such as light self-weight and corrosion-free problems, even though these are weaknesses to be overcome. The main problems are local buckling and low connection capacity. From the previous study, it was shown that cold-formed rectangular hollow portal frame using thick section indicated the plastic behaviour. This section is uneasy to be derived at site. Besides, some connection methods have also been suggested by previous researchers using bolts, rivets, press and weld but such the connections cannot reach rigid connection as needed for plastic design of portal frame. This research intends to study strengthening methods of cold-formed steel section and the connection performance improvement using cover plate. From this study, it is expected that cold-formed steel section can achieve plastic section and the rigid connection can be reached. The study was performed in two stages. In the first stage, the study on small cold-formed steel beams was done, while in the second stage, the study investigated a full scale of cold-formed steel beams and the connections. Specimens of this research consist of strengthened cold-formed closed beams and the moment connections. The beams are strengthened using a splice of hot rolled plate attached to the original section by screws and weld. The beams are in various design strength, thickness, screw spacing and number of web screw rows. Three types of connection i.e. welded, unbraced cover and braced cover connections were constructed for the specimens. Self-drilling screws for the section strengthening were applied on the connected members outside the cover plate. The experimental results were compared to the theoretical one. From this study, it can be concluded that the applied strengthening method significantly increase the moment capacity of the cold-formed steel sections. Similarly, the braced cover connection improves the connection to be rigid connection.

ABSTRAK

Sehingga kini, penggunaan keluli terbentuk sejuk pada binaan-binaan perindustrian satu tingkat khasnya sebagai elemen struktur kerangka portal belum banyak dibuat. Penggunaannya pada binaan majoriti digunakan sebagai kekuda, kerangka bumbung, dinding dan bahagian-bahagian penyokong binaan lain. Dibandingkan dengan keluli tergelek panas, penggunaan keluli terbentuk sejuk pada struktur binaan mempunyai kelebihan-kelebihan antara lain berat diri kecil dan tak ada soalan kakisan, namun ada kelemahan yang perlu dibaiki agar boleh digunakan secara lebih luas lagi. Permasalahan utama yang menghalang adalah terjadinya lengkukan tempatan dan keupayaan sambungannya yang rendah. Penyelidik sebelumnya menyatakan bahawa kerangka portal yang menggunakan keratan segiempat tepat geronggang yang tebal dapat menunjukkan kelakuan plastik. Keratan seperti ini tidak mudah diperolehi di lapangan. Disamping itu pelbagai kaedah penyambungan yang dicadangkan penyelidik sebelumnya dengan menggunakan bolt, rivet, tekanan mahupun kimpal, bagaimanapun tidak boleh berkelakuan sebagai sambungan tegar seperti yang diperlukan pada reka bentuk plastik kerangka portal. Penyelidikan ini bermaksud menyiasat perkuatan keratan keluli terbentuk sejuk dengan cara menambah ketebalan elemen-elemen keratan yang tertekan serta meningkatkan keupayaan sambungannya dengan penambahan plat penutup. Dari hasil kajian ini diharapkan keratan-keratan keluli terbentuk sejuk dapat mencapai kategori keratan plastik serta sambungan tegar anggota-anggota keluli terbentuk sejuk dapat dicapai. Penyelidikan ini dilakukan dua tahap iaitu kajian berskala pada rasuk-rasuk keluli terbentuk sejuk dan penyelidikan dengan spesimen skala penuh rasuk-rasuk keluli terbentuk sejuk yang diperkuat serta sambungan momennya. Keratan rasuk diperkuat dengan menambah keluli tergelek panas yang dikimpal dan diperkuat dengan skru gerudi-diri dengan pengaturan yang berbeza. Tiga jenis sambungan iaitu sambungan kimpal, sambungan penutup tanpa penguat dan sambungan penutup dengan penguat dibuat sebagai spesimen. Skru gerudi-diri dipasang pada batang-batang sambungan diluar kawasan plat penutup. Hasil penyelidikan tersebut kemudian dibanding dengan hasil pengiraan teori. Dari penyelidikan ini dapat disimpulkan bahawa kaedah perkuatan yang dilakukan dapat meningkatkan keupayaan keratan keluli terbentuk sejuk secara nyata meskipun belum mencapai keratan plastik. Begitu juga dengan kaedah penyambungan yang dicadangkan dapat menambah ketegaran sambungan sehingga mencapai kriteria sambungan tegar.

2.2.1.2	Behaviour of a Portal Frame at Failure	13
2.2.1.3	Types of Connection of Portal Frame Structure	15
2.2.1.4	Analysis Diagrams of Portal Frame Structure	16
2.2.2	Cold-Formed Steel Members Subject to Bending	19
2.2.2.1	Classification of Sections	20
2.2.2.2	Material Properties	21
2.2.2.3	Effect of Local Buckling	22
2.2.2.4	Capacity of CFS Sections Subject to Bending	23
2.2.2.5	Stability of CFS Sections Subject to Bending	26
2.2.3	Strengthening of Steel Sections	30
2.2.3.1	Types of Strengthening	30
2.2.3.2	Classification of Strengthened Steel Sections	32
2.2.3.3	Properties of Strengthened Steel Sections	35
2.2.3.4	Capacity of Strengthened Steel Sections	37
2.2.4	Moment Connection on Steel Portal Frame Structure	37
2.2.4.1	Types of Moment Connection	38
2.2.4.2	Classification of Moment Connections	38
2.2.4.3	Rigidity of Moment Connection	40
2.2.4.4	Capacity of Moment Connection	43
2.3	Previous Studies	45
2.3.1	Application of CFS Sections in Frame Structure	45

	2.3.2	Behaviour of CFS Sections Subject to Bending	51
	2.3.3	Strengthening of Cold-Formed Steel Sections	58
	2.3.4	Connections on CFS Structures	62
	2.4	Conclusion Remarks	77
3		ANALYTICAL STUDY OF STRUCTURE AND ELEMENTS OF COLD-FORMED STEEL PORTAL FRAME	80
	3.1	Introduction	80
	3.2	Analysis Curves of Pinned Base Portal Frame	80
	3.3	Analysis of Portal Frame Based on Elastic and Simple Plastic Theory	87
	3.4	Stability of Cold-Formed Open and Closed Sections Rafter in PF Design	93
	3.5	Effect of Section Thickness to the Plastic Section Classified of Cold-Formed Rectangular Hollow Sections in Various Width to Depth Ratios	112
	3.6	Properties of Cold-Formed Rectangular Hollow Members in Bending	116
	3.7	Capacity of Cold-Formed Rectangular Hollow Members in Bending	118
	3.8	Performance of Welded Cover Connections	120
	3.9	Conclusion Remarks	128
4		STRENGTHENING OF COLD-FORMED STEEL SECTION AT PLASTIC BEHAVIOUR	130
	4.1	Introduction	130
	4.2	Material and Geometrical Properties of Specimens	131
	4.3	Types of Section Strengthening	132
	4.4	Plastic Section Classification	133
	4.5	Section Properties	135
	4.6	Design Capacity	141

4.7	Experimental Program	143
4.7.1.	Objective	143
4.7.2.	Specimen	143
4.7.3.	Test Procedure	147
4.7.4.	Result	148
4.8	Discussion	154
4.8.1	Plastic Section Classification	154
4.8.2	Properties of Section	155
4.8.3	Moment Capacity	157
4.8.4	Mode of Failure	158
4.8.5	Failure Location	159
4.8.6	Effect of Screw Spacing	161
4.8.7	Effect of Numbers of Flange Screws Row	161
4.9	Conclusion Remarks	162
5	FLEXURAL BEHAVIOUR OF STRENGTHENED COLD-FORMED STEEL CLOSED SECTIONS	163
5.1	Introduction	163
5.2	Tensile Test of Cold-Formed/Hot-Rolled Steel Plates	164
5.2.1	Objective	164
5.2.2	Specimens	164
5.2.3	Test Procedure	166
5.2.4	Test Result	167
5.3	Section Plasticity	168
5.4	Properties of Section	180
5.5	Moment Capacity	182
5.6	Experimental Program	184
5.6.1	Objective	184
5.6.2	Specimen	185
5.6.3	Test Procedure	187
5.6.4	Test Result	188
5.7	Discussion	194
5.7.1	Plasticity of Section	194
5.7.2	Section Properties	196

	5.7.3	Moment Capacity	199
	5.7.4	Mode of Failure	204
	5.7.5	Failure Location	206
	5.8	Conclusion Remarks	208
6		PERFORMANCE OF WELDED COVER CONNECTION	209
	6.1	Introduction	209
	6.2	Theoretical Analysis of Connection	210
	6.2.1	Material and Geometrical Properties	210
	6.2.2	Members of Connection	212
	6.2.3	Properties of Connection Members	215
	6.2.4	Capacity of Connection Members	216
	6.2.5	Limit Slope of Connection Rigidity	218
	6.2.6	Design Capacity of Connection	222
	6.3	Experimental Work	228
	6.3.1	Objective	228
	6.3.2	Specimen	228
	6.3.3	Test Procedure	231
	6.3.4	Test Result	232
	6.4	Discussion	234
	6.4.1	Mode of Failure	234
	6.4.2	Location of Failure	236
	6.4.3	Rigidity of Connection	237
	6.4.4	Capacity of Connection	239
	6.5	Conclusion Remarks	241
7		RESULTS AND DISCUSSION	242
	7.1	Introduction	242
	7.2	Plasticity of Strengthened Cold-Formed Steel Sections	243
	7.3	Bending Stiffness of Strengthened Cold-Formed Steel Sections	245

7.4	Moment Capacity of Strengthened Cold-Formed Steel Sections in Bending	246
7.5	Capacity of Connection	247
7.6	Rigidity of Connection	248
7.7	Predominant Parameters in the Strengthening of Cold-Formed Beam	249
7.8	Dominant Parameters Influencing the Connection Capacity	255
7.9	Conclusion Remarks	258
8	CONCLUSIONS	259
8.1	Introduction	259
8.2	Conclusions	259
8.3	Further Study	260
	REFERENCES	262
	Appendices A-L	267-335

LIST OF TABLES

TABLE NO.	TITLE	PAGE
2.1	Limiting width to thickness ratios for sections other than CHS and RHS	33
2.2	Components of the connection capacity check	44
3.1	Types of the portal frame	87
3.2	Material and section properties of the rafter	94
3.3	Types and dimensions of the portal frame	94
3.4a	Reactions and moments for various span of portal frame PF-1	95
3.4b	Reactions and moments for various span of portal frame PF-2	96
3.4c	Reactions and moments for various span of portal frame PF-3	96
3.4d	Reactions and moments for various span of portal frame PF-4	96
3.4e	Reactions and moments for various span of portal frame PF-5	97
3.5a	Stability check of open section rafter of portal frame PF-1	106
3.5b	Stability check of open section rafter of portal frame PF-2	107
3.5c	Stability check of open section rafter of portal frame PF-3	107
3.5d	Stability check of open section rafter of portal frame PF-4	108
3.5e	Stability check of open section rafter of portal frame PF-5	108
3.6a	Stability check of closed section rafter of portal frame PF-1	109
3.6b	Stability check of closed section rafter of portal frame PF-1	109
3.6c	Stability check of closed section rafter of portal frame PF-1	110
3.6d	Stability check of closed section rafter of portal frame PF-1	110

3.6e	Stability check of closed section rafter of portal frame PF-1	111
3.7	Maximum. span and critical parameter of stability of the portal frames	111
3.8	Plastic section classification of rectangular hollow sections	114
3.9	Data of the connection models	122
3.10	Theoretical capacity of connection models	127
4.1	Properties of the beam specimen	131
4.2	Types of beam specimens	132
4.3	Plastic section classification of the specimens	134
4.4	Calculation of section area	137
4.5	Calculation of moment of inertia of the idealized section	137
4.6	Calculation of moment inertia of the effective section	145
4.7	Calculation of the effective plastic modulus	139
4.8	Section properties of the beam sections	140
4.9	Moment capacity of the beam specimens	142
4.10	Types of beam specimen	145
4.11	Experimental moment of inertia	156
4.12	Ratios of moment capacity	157
5.1	Coupon specimens	165
5.2	Tensile test results	167
5.3	Types of specimen used	170
5.4a	Assumed thickness, t of the strengthened sections	174
5.4b	Assumed width, B and effective width, B' of the compression flange	174
5.4c	Assumed depth, D and effective depth, D' of the web	174

5.5a	Theoretical plastic section classification of the specimen CRBS-T1.5 ($f_y = 450$ MPa)	176
5.5b	Theoretical plastic section classification of the specimen CRBS-T1.9 ($f_y = 550$ MPa)	177
5.5c	Theoretical plastic section classification of the specimen CRBS-T2.4 ($f_y = 400$ MPa)	178
5.6	Plastic section classification of the specimens	179
5.7a	Section properties of the specimen CRBS-T1.5	181
5.7b	Section properties of specimen CRBS-T1.9	181
5.7c	Section properties of specimen CRBS-T2.4	182
5.8a	Moment capacities of the specimen CRBS-T1.5	183
5.8b	Moment capacities of the specimen CRBS-T1.9	183
5.8c	Moment capacities of the specimen CRBS-T2.4	184
5.9	Details of the beam specimens	187
5.10	Maximum moment and corresponding deflection and rotation	189
5.11	Maximum moment and theoretical plastic moments	195
5.12	Experimental second moment of inertia	196
5.13a	Ratios of second moment of inertia ($t = t_s$)	197
5.13b	Ratios of second moment of inertia ($t = t_p$)	197
5.13c	Ratios of second moment of inertia ($t = t_s + t_p$)	197
5.14	Second moment of inertia of the equivalent sections	198
5.15	Experimental moment capacity	199
5.16a	Ratios of moment capacity ($t = t_s$)	200
5.16b	Ratios of moment capacity ($t = t_p$)	200
5.16c	Ratios of moment capacity ($t = t_s + t_p$)	200
5.17	Ratios of the equivalent to total thicknesses	201

5.18a	Experimental moment capacity to plastic moment ratios ($t = t_s$)	202
5.18b	Experimental moment capacity to plastic moment ratios ($t = t_p$)	202
5.18c	Experimental moment capacity to plastic moment ratios ($t = t_s + t_p$)	202
5.19	Ratios of the equivalent to total thicknesses	203
6.1	Material properties of the specimens	210
6.2	Detail of connection members	214
6.3	Approached moment of inertia of the connected members	216
6.4	Approached moment capacity of the connected members	218
6.5	Slopes of the dividing line refer to Steel Construction Institute (1995)	220
6.6	Slopes of the dividing line refer to Steel Construction Institute (1995)	221
6.7	Theoretical connection capacity	225
6.8	Theoretical maximum force	227
6.9	Ratios of theoretical connection capacity	228
6.10	Detail of the connection specimens	229
6.11	Rotation at maximum moment	233
6.12	Experimental slope of the dividing line	238
6.13	Theoretical and experimental rigidity of the specimens	239
6.14	Maximum moment of the connections	239
6.15	Experimental maximum forces	240
6.16	Maximum force ratio	240
7.1	Moment ratio of the beams	246
7.2	Moment ratio of the connections	247
7.3	Slope ratio of connections	249

7.4	Ratios of strengthening moment	250
7.5	Ratios of section thickness and strengthening moment	251
7.6	Ratios of $\frac{D}{n+1}$ and strengthening moment	252
7.7	Ratios of screw spacing and strengthening moment	253
7.8	Ratios of the design strength and the strengthening moment	254
7.9	Ratios of cover plate thickness and moment	256
7.10	Ratios of cover plate length and moment	257

LIST OF FIGURES

FIGURE NO.	TITLE	PAGE
2.1	Pinned base portal frame	8
2.2	Bending moment and shear force diagrams of pinned base portal frame	9
2.3	Determination of plastic moment of pinned base portal frame	11
2.4	Determination of plastic hinge locations	12
2.5	Plastic hinge locations at haunched portal frame	13
2.6	Portal frame with uniformly distributed load	14
2.7	Types of eaves connection	15
2.8	Types of apex connection	16
2.9	Diagrams of plastic analysis for pinned base portal frame (Righniotis, 1996)	18
2.10	Diagrams of plastic analysis for pinned base portal frame (Joannides and Weller, 2002)	19
2.11	Typical compound beams	31
2.12	Typical sections of plate girder	31
2.13	Stiffener plate of cold-formed steel C section	32
2.14	Cold-formed combined sections	32
2.15	Dimension of compound flanges(BSI, 2000)	34
2.16	Dimension for section classification of plate girders	34
2.17	Typical strengthened sections with welding	35
2.18	Connector holes on I section	36

2.19	Combined section of cold-formed steel and gypsum board	36
2.20	Dimension of equivalent combined sections	37
2.21	The moment-rotation of connection	39
2.22	Connections classification curves	40
2.23	Classification of joints by stiffness (BS EN 1993: 1-8: 2005)	42
2.24	Classification of joints by stiffness (Bjorhovde, 1990)	42
2.25	Connection checking zones	43
2.26	Components of the connection capacity check	44
2.27	Truss structure subject to point load panel	45
2.28	Lipped channel and hat sections	46
2.29	Section geometry	47
2.30	Bending test set-up	47
2.31	Failure mode of truss elements	48
2.32	A typical of cold-formed steel portal frame	49
2.33	Dimension and section geometry of the proposed section	49
2.34	Schematic drawing of portal frame test by Kwon <i>et. al.</i> (2006)	50
2.35	Schematic drawing of the portal frame test (Wilkinson, 2006)	50
2.36	Variables involved in design of hat, I and Z beams	52
2.37	Sections of beam specimens	53
2.38	Schema of end loading test	54
2.39	Dimension of Z and C sections	55
2.40	Simple, inside angled and outside angled returns lips of Z sections	55
2.41	Beam model and cold-formed steel sections	56
2.42	Built-up column using batten plate	58
2.43	Box beam edge loading	59

2.44	Schematic drawing of section, screw spacing and test of built up stud	60
2.45	Built-up closed column	61
2.46	Typical joint using press join method	62
2.47	Moment-rotation connection model of press joining method	62
2.48	Types of screw fastener	63
2.49	Dimensions of screwed connection specimens	64
2.50	Schematic drawing of column-base connection test	65
2.51	Setup of beam-column connection tests	66
2.52	Schematic drawing of portal frame test	66
2.53	Schema of single bolt specimens	67
2.54	Schema of double bolt specimens	68
2.55	Typical failure of bolted connections	68
2.56	Bearing failure of single shear single bolt connection	69
2.57	Double-lap fillet connections specimens	70
2.58	Single-lap fillet welded connection specimens	70
2.59	Double-lap flare-bevel welded connection specimens	71
2.60	Stiffened welded connection specimen	72
2.61	Unstiffened welded connection specimen	72
2.62	Screw patterns	73
2.63	Flexural failure of external beam-column sub-frame	74
2.64	Typical purlin arrangement	74
2.65	Lateral-torsional buckling of purlin	75
2.66	Setup of eaves connection test	76
3.1	Pinned base portal frame with uniform load	81
3.2	Dimension of purlin section (C 40030)	81

3.3	Elastic analysis curves	84
3.4	Plastic analysis curves	85
3.5	Configuration of the portal frames	88
3.6	Horizontal force at the base	88
3.7	Moment in the rafter	89
3.8	Moment in the column	90
3.9	Horizontal force and moments ratios	92
3.10	Typical configuration of portal frame suitable for the plastic design	93
3.11	Typical double C-sections	93
3.12	Types of portal frame used in the study	95
3.13	Portal Frame PF-5	98
3.14	Typical rectangular hollow section	112
3.15	Relation of B/D ratio and section thickness	115
3.16	Typical rectangular hollow section	116
3.17	Moment of inertia	117
3.18	Elastic modulus	117
3.19	Plastic modulus	117
3.20	Moment capacity	119
3.21	Plastic moment capacity	119
3.22	Types and details of the connection models	121
3.23	Tension and compression force in beam flange	123
3.24	Resistance of column flange in tension	124
3.25	Resistance of column web in tension	124
3.26	Force dispersion for web crushing	125
3.27	Length for web buckling	126

3.28	Column web panel in shear	126
4.1	Dimension of the beam sections	131
4.2	Screw arrangements of the beam section	132
4.3	Dimension of the C channel section	136
4.4	Dimension of effective section	138
4.5	Schematic drawing of the strengthened beam	143
4.6	Photos of the beam specimen	145
4.7	Types of screw arrangement on flange and web of the stiffener	146
4.8	Drawing sketch of the beam-bending test	147
4.9	Determination of beam rotation	148
4.10	Determination of moment maximum	149
4.11	Load-deflection diagram of the specimens	151
4.12	Moment-rotation diagram of the specimens	154
4.13	Deflection of simply supported beam	155
4.14	Experimental load-deflection curve	156
4.15	Local deformation at mid span of specimens C1, C2 and CRS	159
4.16	Local deformation of specimens CRS-S1, S2 and S3	159
4.17	Failure location of specimens	160
5.1	Dimension of coupon specimen	164
5.2	Photos of some coupon specimens	165
5.3	Test of the coupon specimen	166
5.4	Assumed thickness for strengthened cold-formed sections	169
5.5	Assumed width and depth of the strengthened sections	169
5.6	Numbers of screw rows of specimen CRBS-T1.5	171
5.7	Numbers of screw rows of specimen CRBS-T1.9	171

5.8	Numbers of screw rows of specimen CRBS-T2.4	172
5.9	Specimen CRBS-T1.5	185
5.10	Specimen CRBS-T1.9	186
5.11	Specimen CRBS-T2.4	187
5.12	Schematic drawing of bending test	188
5.13	Determination of moment maximum	190
5.14	Test results of the specimen CRBS-T1.5	191
5.15	Test results of the specimen CRBS-T1.9	192
5.16	Test results of the specimen CRBS-T2.4	193
5.17	Test results of the specimens	194
5.18	Determination of experimental moment capacity	199
5.19	Failure of specimen CRBS-T1.5	205
5.20	Failure of specimen CRBS-T1.9	205
5.21	Failure of specimen CRBS-T2.4	206
5.22	Failure location of specimen CRBS-T1.5	207
5.23	Failure location of specimen CRBS-T1.9	207
5.24	Failure location of specimen CRBS-T2.4	207
6.1	Eaves location in portal frame	209
6.2	Schematic drawing of welded moment connection	210
6.3	Dimension of single C channel section	211
6.4	Hot-rolled stiffener plates	211
6.5	Cover plate of connection	212
6.6	Welded connection of single C section	212
6.7	Internal sleeve	213
6.8	Internal stiffeners	213

6.9	Stiffener attachment with self-drilling screws	214
6.10	Screws arrangement of connected members	215
6.11	Classification of moment connection based on the rotational stiffness (BS EN 1993: 1-8: 2005)	219
6.12	Determination of the connection length	219
6.13	Classification of moment connection based on the rotational stiffness (Bjorhovde, 1990)	221
6.14	Distribution of force in connection members	226
6.15	Specimen CRBC-T1.5	230
6.16	Specimen CRBC-T1.9	230
6.17	Specimen CRBC-T2.4	231
6.18	Schematic diagram of connection tests	232
6.19	Moment-rotation curves of specimen CRBC-T1.5	233
6.20	Moment-rotation curves of specimen CRBC-T1.9	233
6.21	Moment-rotation curves of specimen CRBC-T2.4	234
6.22	Failure mode of specimen CRBC-T1.5	234
6.23	Failure mode of specimen CRBC-T1.9	235
6.24	Failure mode of specimen CRBC-T2.4	235
6.25	Failure location of specimens	237
6.26	Slope of moment-rotation diagram of the specimen CRBC-T1.5	238
7.1	Thickness limit of plastic section classification of assumption D2	245
7.2	Relation of strengthening moment and thickness ratios	251
7.3	Relation of strengthening moment and number of web screw rows ratios	252
7.4	Relation of strengthening moments and screw spacing ratios	253
7.5	Relation of strengthening moment and design strength ratios	254

7.6	Moment ratios of connection	255
7.7	Relation of moment and cover plate thickness ratios	256
7.8	Relation of cover plate length to moment ratios	257

LIST OF SYMBOLS

A	-	section area
b	-	flange or section width; haunch length; flat width of the compression element
b_p	-	internal width of web plate
b_o	-	outstand of plate width
b_1	-	stiff bearing length
B	-	overall section width; constant of elastic analysis of portal frame; flange width for unstiffened or edge stiffened flanges, or half the overall flange width for stiffened flanges
B_b	-	beam flange width
B_c	-	column flange width
B_1	-	section width
B_2	-	section depth
B_{eff}	-	effective section width
c	-	distance from the end of the beam to the load or the reaction
C	-	constant of elastic analysis of portal frame; compression force
C_b	-	coefficient which may be conservatively assumed to be unity
C_{exp}	-	experimental compression force
C_{th}	-	theoretical compression force
C_3	-	constant
C_4	-	constant
C_{12}	-	constant
d	-	section or web depth; haunch depth; deflection at mid-span
D	-	overall section depth; overall web depth
D_e	-	equivalent depth of an intermediately stiffened web
D_2	-	distance between the centre line of the intermediate stiffener web and the tension element

e	-	height to hinge location at the bottom of haunch
E	-	modulus of elasticity
E_s	-	modulus of elasticity of steel
E_g	-	modulus of elasticity of gypsum board
f	-	rise of portal frame roof
f_a	-	average stress
f_{av}	-	average shear stress
f_v	-	shear stress
f_c	-	compressive stress of effective element
F_v	-	shear force
$F_{v\text{ exp}}$	-	experimental shear force
$F_{v\text{ th}}$	-	theoretical shear force
F_w	-	concentrated web load or reaction
g	-	roof height from base
G	-	shear modulus
h	-	eaves height of portal frame; constant which is equal to B_2/B_1
H	-	horizontal force at base
H_e	-	elastic horizontal force at base
H_p	-	plastic horizontal force at base
I_{app}	-	approach moment of inertia
I_g	-	moment of inertia of gypsum board section
I_s	-	moment of inertia of steel section
I_{th}	-	theoretical moment of inertia
I_x	-	moment of inertia
I_{xr}	-	moment of inertia of reduced section
I_{xx}	-	moment of inertia referring to X axis
I_1	-	moment of inertia of column
I_2	-	moment of inertia of rafter
k	-	constant of elastic analysis of portal frame; constant which is equal to $p_y / 228$
K	-	local buckling coefficient; buckling coefficient of the compression flange
l	-	length of lip of C-section

L	-	span length; connection length
L_c	-	cover plate length
L_E	-	effective length
m	-	constant of elastic analysis of portal frame
M	-	bending moment for a loading system; bending moment acting at the action as F_v
M_b	-	buckling resistance moment
M_c	-	moment capacity of section
M'_c	-	actual moment capacity
M_{cr}	-	critical bending moment
M_{exp}	-	experimental moment
M_{th}	-	theoretical moment
M_E	-	elastic lateral buckling resistance moment
M_r	-	moment in portal frame rafter
M_{re}	-	elastic moment in portal frame rafter
M_{rp}	-	plastic moment in portal frame rafter
M_l	-	moment in portal frame column
M_{le}	-	elastic moment in portal frame column
M_{lp}	-	plastic moment in portal frame column
M_p	-	plastic moment
M_x	-	moment at point X
M_c	-	moment capacity of section
M_{cr}	-	critical bending moment
n_1	-	length obtained by a 45° dispersion through half the depth of column
n_2	-	length obtained by a 1:2.5 dispersion through the column flange and root radius
N	-	constant of elastic analysis of portal frame; actual length of bearing; axial force
N_{exp}	-	experimental axial force
N_{th}	-	theoretical axial force
p_{cr}	-	local buckling stress of element
p_y	-	design strength

p_o	-	limiting compressive stress in a flat web
p_v	-	design strength
p_{vc}	-	design strength of column
P_c	-	resistance of column web in compression zone
P	-	applied point load
P_c	-	column web capacity in crushing/ bearing; column web capacity in buckling
P_{cf}	-	beam flange capacity in compression
P_{exp}	-	experimental ultimate load
P_{th}	-	theoretical ultimate load
P_{th}	-	theoretical ultimate load
P_{max}	-	ultimate load
P_s	-	theoretical ultimate load
P_t	-	tension capacity of unstiffened column web
P_{tc}	-	column web capacity in bending
P_{tf}	-	beam flange capacity in tension
P_{th}	-	ultimate load
P_v	-	shear capacity or shear buckling resistance
P_w	-	concentrated load resistance of a single web
q	-	constant generally 0.6 – 0.7
q_{cr}	-	shear buckling stress of a web
r	-	inside bend radius
r_c	-	column root radius
r_y	-	radius of gyration of section about Y axis
R_{mb}	-	moment ratio of beam
R_{mc}	-	moment ratio of connection
R_{ms}	-	ratio of strengthening moment
R_s	-	ratio of slope
R_t	-	ratio of section thickness
s	-	rafter length
sf	-	fillet weld leg length to beam flange
S	-	plastic modulus of section
S_{exp}	-	experimental curve slope

S_x	-	experimental curve slope about X-axis
S_{xr}	-	experimental curve slope
t	-	flange or web thickness; material thickness; compression element thickness
t_b	-	beam web thickness
t_{br}	-	thickness of bracing plate
t_c	-	thickness of cover plate; column web thickness
t_{eq}	-	equivalent thickness of section
t_p	-	thickness of stiffener plate
t_s	-	thickness of original section
T	-	flange thickness; tension force
T_b	-	beam flange thickness
T_c	-	column flange thickness
T_{exp}	-	experimental tension force
T_{th}	-	theoretical tension force
u	-	deflection of the centre of the flange towards the neutral axis
U_s	-	minimum ultimate tensile strength
V	-	vertical reaction of support; shear force
w	-	uniformly distributed load
x	-	points distance
\bar{y}	-	distance of flange from neutral axis
Y_s	-	minimum yield strength
Z	-	section modulus
Z_c	-	bending compression modulus for full cross section
Z_x	-	elastic modulus to X axis
α	-	coefficient of linear thermal expansion
β	-	ratio of the smaller end moment to the larger end moment M in the unbraced length of a beam
Δ	-	deflection for given loading system
Δ_c	-	deflection corresponding to M_c
Δ_{cr}	-	deflection of beam corresponding to M_{cr}
ε	-	constant
\emptyset	-	constant of elastic analysis of portal frame; rotation

- η - Perry coefficient
- θ - angle (in degrees) between plane of web and plane of bearing surface
- ν - Poisson's ratio

LIST OF APPENDICES

APPENDIX	TITLE	PAGE
A	Table 11 and Table 12 of BS 5950 Part 1: 2000	267
B	Minimum yield strength of CFS sections, Y_s	269
C	Local buckling coefficient, K	270
D	Ratio of moment coefficient, β	272
E	Calculation of w	273
F	Calculation example of H , M_r and M_1	276
G	Section properties of section 2LL25430	281
H1	Stability check of open rafter	283
H2	Stability check of closed rafter	294
I	Test results of the small beam specimens	304
J	Tensile test results	307
K	Calculation example of M_c and M_p	320
L	Test results of the strengthened beams (CRBS)	329
M	Test results of the welded cover connections (CRBC)	333

CHAPTER 1

INTRODUCTION

1.1 Overview

To date, the majority use of cold-formed steel on buildings is for roof and wall framing, cladding, purlins and railing with C channel, Z and I are the frequently used sections. As cold-formed steel sections are composed of thin elements, usually such sections are categorized as slender section due to the width to thickness b/T of the flange and depth to thickness d/t of the web ratios are relatively large. Thus, generally the sections are vulnerable to local buckling particularly on those compression elements subjected to bending or in axial compression.

In single storey industrial buildings, portal frames are a widely used typical structure because of their cleanliness, good overhead clearance and relatively low cost. Commonly, such frames are designed using plastic method to obtain an economical structure although the detailed stability check is required. So far, hot-rolled steel is the material which satisfies the requirement for such structures because of having ability to yield perfectly in tension as well as in compression. In addition, the hot-rolled connections have a sufficient rotational stiffness to form plastic hinge.

To expand the application of cold-formed steel in buildings, its use as portal frame members for replacing the hot-rolled needs to be considered. This is because cold-formed steel sections have advantages such as its light self-weight and corrosion-free problems. Otherwise, these are some weaknesses needed to be solved

mainly due to the local buckling and low rotational stiffness connection.

1.1 Background of Research

The use of cold-formed steel sections as portal frame members of single storey industrial buildings is very rare. This mainly is due to their insufficient stability to withstand the large forces (i.e. horizontal force at the base, moment in the rafter and moment in the column) normally induced in portal frame structure. Previous studies (Vos and Rensburg, 1977; Lim and Nethercot, 2004; Kwon *et al.*, 2006; Wilkinson, 2006) on this matter have not been performed extensively. Most existing research studied the cold-formed open sections subjected to bending or in compression of C channel, Z, L or I section (Adeli and Karim, 1997; Schafer and Pekoz, 1999; Pan and Yu, 2001; Corte *et al.*, 2003; Young and Hancock, 2003; Yu and Schafer, 2003; Nguyen *et al.*, 2006; Madry and Ignatowicz, 2008). In addition, some researchers (LaBoube and Yu, 1998; Nuttayasakul and Easterling, 2006; Wood and Dawe, 2006; Dawe *et al.*, 2009) have conducted researches on cold-formed steel sections for roof truss structure using a cold-formed lipped channel open section. In addition, a hat section was also used in the study by another researcher (Tahir *et al.*, 2006).

The use of cold-formed closed section is an alternative to derive a better stability of section. A study on stability of the closed section had been performed by previous researchers but it was limited to the members subjected to bending (Serrette, 2004; Young and Chen, 2008; Xu *et al.*, 2009). The only investigation on behaviour of cold-formed closed sections in portal frame had been carried-out. The study used cold-formed rectangular hollow sections with a relatively large thickness (Wilkinson, 2006). In fact, this type of section cannot be easily found in market. Therefore, it is a need to consider constructing a closed section by combining the existing and common sections.

A main weakness of applying cold-formed steel sections as portal frame members is the local buckling problem. This is because such sections are composed of thin elements in which the width to thickness b/T of the flange and depth to thickness d/t of the web ratios are relatively large. Consequently, in general cold-formed steel sections are categorized as slender section which causes buckling on the compression elements of the section at a stress level lower than the material yield strength. In order to prevent the local buckling, adding the thickness of the compression elements may be required.

In addition, another problem of applying cold-formed steel sections in portal frame besides the local buckling is low rotational stiffness of the connection. Although, all the types of the connections commonly used in hot-rolled steel structure can be applied to cold-formed steel, bolted connection is the type often used for the cold-formed moment connection. However, such connections can not be classified as rigid connection.

1.2 Problem Statement

This study is performed in order to enhance the use of cold-formed steel sections in buildings particularly for portal frame members. The main problems of applying such sections as portal frame members to be designed plastically are the local buckling and low rotational stiffness of the connection due to the local buckling.

Therefore, this research emphasize on how to prevent the local buckling of cold-formed steel sections so increasing the section capacity and how to improve the rotational stiffness of the connection. Thus, the problems to be solved of this study are the suitable section strengthening and connection methods of cold-formed steel particularly for portal frames have not been found.

The idea to strengthen cold-formed steel sections by adding the thickness of compression elements of the section in order to increase the section capacity is a relatively original concept. Likewise, the rigid connection of cold-formed members proposed by using cover plate is. Thus, this research is expected to increase the capacity of cold-formed steel sections. In addition, it is also expected that the proposed rigid connection can be achieved.

1.3 Objectives of Study

The objective of this study is to investigate the possibility of applying cold-formed steel sections in portal frame to be designed plastically. In detail, the objectives of this study are as follows:

- (i) To generate design charts of pinned base portal frames;
- (ii) To investigate analytically behaviour of cold-formed steel sections and its stability in portal frame;
- (iii) To investigate experimentally effect of section strengthening and screw arrangements to the properties and capacity of small cold-formed steel beams;
- (iv) To derive the design strength Y_s of the cold-formed and hot-rolled steel coupons;
- (v) To investigate experimentally effect of the section strengthening method to the plastic section classification, section properties and capacity of strengthened cold-formed steel beams;
- (vi) To investigate experimentally effect of the connection method to rigidity and capacity of the strengthened cold-formed steel connections.

1.4 Scope of Study

The scope of this research includes theoretical analysis and experimental test,

which encompasses the following items:

- (i) Elastic and plastic analysis diagrams of pinned base portal frame;
Portal frames with simply supported at the base, single storey and subjected to a uniformly distributed load were analyzed base on the elastic and plastic methods. The horizontal force at the base, moment in the rafter and moment in the column curves for elastic and same parameters for plastic with respect to rise/span and span/eaves height were generated.
- (ii) Plasticity behaviour of cold-formed steel sections;
Six analytical studies were performed to investigate behaviour of cold-formed steel sections applied as portal frame members which were elastically and plastically analyzed. Stability of the rafter of open and closed sections was also checked. Effect of the B/D ratio to the plastic section classification of the cold-formed rectangular hollow section was determined. Properties and capacities of the cold-formed steel section and connections were calculated based on BS 5950 Part 5: 1998.
- (iii) Capacity of strengthened cold-formed beams;
Three section types were used which are C channel, rectangular hollow and strengthened rectangular hollow sections. Plastic section classification, section properties and design capacity of the sections were calculated based on the design standard, BS 5950 Part 1: 2000 and BS 5950 Part 5: 1998. The experiment on six beams on C channel, rectangular hollow without strengthening and strengthened with hot-rolled plate was also performed. Form six beams, three rectangular hollow sections were strengthened by increasing the thickness of the web and compression flange using a splice of hot-rolled plate of 1 mm thickness. The plates were attached to the original section using self-driven screws. And the different number of screw and screw spacing were adopted. The results from theory and experimental were compared.
- (iv) Performance of moment connection of the strengthened cold-formed members;

Three moment connections had been tested in this study i.e. welded, unbraced cover and braced cover connections. All the connections were strengthened by internal sleeve made of hot-rolled steel of 5 mm thickness. The connection members were closed sections formed of two channel sections which were face-to-face welded. The members were strengthened referring to the result of the strengthened cold-formed steel beam test. The connections were tested by applying horizontal point load on the rolled point on the connections edge. Maximum load, deflection and rotation adjacent to the observed point of the connection were recorded. Moment-rotation diagrams, rigidity and capacity of the connections were obtained. The experimental and theoretical results were compared.

1.5 Organization of Thesis

This thesis is structured as follows: Chapter 2 contains a literature review which covers basic theory and previous studies on portal frame analysis, cold-formed steel stability, strengthening of cold-formed steel sections and portal frame connections. The chapter provides the basis to draw the portal frame analysis diagrams and overall review of cold-formed steel members subjected to bending. In addition, some methods of steel section strengthening and rigid connection concept are described. Chapter 3 discusses the analytical study on structure and elements of cold-formed steel portal frame. Chapter 4 outlines the experimental study using model while Chapter 5 and Chapter 6 explain the full-scale study has been performed. Results obtained from this research and the discussion is presented in Chapter 7. Finally, Chapter 8 provides some conclusions and suggestions for further study.

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