

MULTI-OBJECTIVE OPTIMIZATION OF MIMO CONTROL SYSTEM USING  
SURROGATE MODELING

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*To the people who are crazy enough to think they can change the world.*

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*Mohd Fauzi bin Nor Shah, Jasin*

## ABSTRACT

A multi-objective optimization approach using surrogate modeling is applied to a nonlinear Multi Input Multi Outputs (MIMO) control system model to predict Pareto-front of objective functions which is defined using Integral Square Error (ISE). Typically, practical multi-objective optimization was highly expensive even in computer simulation. To address such a challenge, approximation or surrogate based techniques are adopted to reduce the computational cost. The surrogate modeling developed as surrogates of the expensive simulation process in order to improve the overall computation efficiency in multi-objective optimization problem. By using surrogate modeling, the location of the actual Pareto-front is predicted by Radial Basis Function Neural Network (RBFNN) using only a small fraction of the design space. Some case studies show that the surrogate modeling manages to predict most of the Pareto-front of the design space. The best compromise of ISE obtained from predicted Pareto-front produces optimum response for MIMO control system. The result indicates that the procedure to construct the 'model of the model' totally compensates the computational expense. This thesis also demonstrates that there are a number of techniques which can be used to tackle difficult multi-objective problems.

## ABSTRAK

Sebuah pendekatan pengoptimalan multi-objektif menggunakan pemodelan pengganti diaplikasikan kepada sebuah sistem kawalan Multi Masukan Multi Keluaran (MMMCK) tidak linear untuk menganggar fungsi objektif Pareto-hadapan di mana ianya didefinisikan menggunakan Ralat Integral Persegi (RIP). Kebiasaanya, pengoptimalan multi-objektif yang praktikal adalah sangat mahal walaupun dalam simulasi komputer. Untuk mengatasi cabaran ini, penganggaran atau teknik berasaskan pengganti diadaptasi untuk mengurangkan kos pengiraan. Pemodelan pengganti dibangunkan sebagai pengganti kepada proses simulasi yang membebankan demi meningkatkan keefisienan pengiraan secara keseluruhan dalam permasalahan pengoptimalan multi-objektif. Dengan menggunakan pemodelan pengganti lokasi Pareto-hadapan sebenar diramal oleh Fungsi Saraf Rangkaian Asas Jejarian menggunakan hanya sedikit pecahan dari ruang reka bentuk. Kes-kes kajian menunjukkan pemodelan pengganti berupaya menganggar kebanyakan Pareto-hadapan dari ruang reka bentuk. Kompromi RIP terbaik diperolehi dari Pareto-hadapan yang dianggar menghasilkan respons optimum untuk sistem kawalan MMMCK. Hasil keputusan menunjukkan prosedur membangunkan 'model kepada model' secara keseluruhan mengkompensasikan pengiraan berkomputer. Tesis ini juga mendemonstrasikan dimana terdapat pelbagai teknik yang boleh diguna bagi menyelesaikan masalah multi-objektif yang sukar.



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## LIST OF ABBREVIATIONS

DoE	–	Design of Experiment
FFNN	–	Feed Forward Neural Network
GUI	–	Graphic User Interface
GUIDE	–	Graphic User Interface Development Environment
ISE	–	Integral Square Error
LH	–	Latin Hypercube
LHD	–	Latin Hypercube Design
LHS	–	Latin Hypercube Sampling
MIMO	–	Multi Input Multi Outputs
MOSMO	–	multi-objective optimization using surrogate modeling
NSGA-II	–	Non-dominated Sorting Genetic Algorithm II
PD	–	Proportional Derivative
PID	–	Proportional Integral Derivative
RBFNN	–	Radial Basis Function Neural Network
ROV	–	Remote Underwater Vehicle
SPEA2	–	Strength Pareto Evolutionary Algorithm 2



## LIST OF SYMBOLS

$D$	–	Input parameter
$D_E$	–	Euclidean distance
$E_x$	–	Error
$\bar{E}_x$	–	Estimated error
$l_x$	–	Lower bound
$u_x$	–	Upper bound
$\ \cdot\ $	–	Euclidean Norm
$\phi_k$	–	Basis function
$x \in \Re^{R \times 1}$	–	Input vector
$\phi$	–	Pseudo
$W_{ij}$	–	Weight for network from neuron $i$ to $j$
$w_{lk}$	–	Weight in the output layer
$K_p$	–	PID proportional gain
$K_i$	–	PID integral gain
$K_d$	–	PID derivative gain

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## **CHAPTER 1**

### **INTRODUCTION**

In the world of control engineering design, there are often multi-input multi-output (MIMO) non-linear systems with complicated mathematical model. The system usually consists of controlled variables and manipulated variables and in practice, it is normally desired to find the controlled values that would give optimal responds of the system. For example, a MIMO control system for a fluid mixing system which consists of a mixing tank and two auxiliary tanks. The first auxiliary tank contains colored water, while the second one contains clear water. The input flow to the mixing tank is controlled by two valves, which regulate the output flows from the auxiliary tanks.

The control system is used to control the level of the liquid in mixing tank and the coloration of the resulting mix at the desired set point. Common practice usually needs to find the optimum controller parameter values that minimize both liquid level and coloration. However there are certain cases engineer emphasis to find the optimal value by selecting one of the controllers. To increase the responsiveness for coloration of the mixing result, the respond on liquid level need to be decreased or vice versa. The process of finding parameters of different respond in MIMO control system is known as a multi-objective problem.

There are mainly two ways to optimize multiple variables in MIMO system. First by aggregating the objectives to a single objective and second by solving a multi-objective optimization problem. Multi-objective optimization is a tool that aids engineers in choosing the best design in a world where many targets need to be satisfied. Unlike conventional optimization, multi-objective optimization will not produce single solution, but rather a set of solutions, commonly referred to as Pareto-front [1]. By definition it will contain only non-dominated solutions. It is up to engineers to select the final design by examining this front. Hence the main purpose

of multi-objective problem is to find this Pareto-front points.

## 1.1 Problem Statement

In MIMO control system problem user usually find an optimum respond for all controller. The optimum response can be obtained by aggregating the objective functions to a single objective function. However in real world not every objective function weight the of same of each other. By aggregating the objective function, only one solution can be achieve in a simulation. User need to re-simulate the problem when the weight in one of the objective function changed. This is why multi-objective optimization is needed to let engineer to have a set of solution or Pareto-front using only a single simulation.

The simulations needed when applying multi-objective optimization for non-linear MIMO control system might be very expensive computationally due to the complexity of the actual model. Despite the continuous advances in computer technology, the long simulation time is still unavoidable. This is due to the fact that the control system to be simulated also keeps getting more complex everyday. Thus it becomes impractical to rely exclusively on simulation for the purpose of multi-objective control system optimization. Here, surrogate modeling is proposed to adopt with multi-objective optimization to produce the Pareto-front. Surrogate modeling requires simple computational algorithm to provide multi set of controller parameters.

This thesis is concerned with how this simulation problem is often tackled in engineering design: simpler approximation models are created to predict the Pareto-front by developing a relationship between the system inputs and outputs. When properly constructed, these approximated Pareto-front models mimic the behavior of the simulation code while being computationally cheap(er) to evaluate.

## 1.2 Objective of Research

1. To develop the **Multi-objective Optimization using Surrogate Modeling (MOSMO)** algorithm for optimizing Multi Input Multi Output (MIMO) controller system.

2. To apply the MOSMO algorithm on different model of the PID controller system as a case study to verify the effectiveness of MOSMO.
3. To compare the performance of MOSMO with brute force search approach and other type of multi-objective optimization approach.
4. To compare the effectiveness of RBF with other approximation approach in searching actual Pareto-front.
5. To develop and integrated a user friendly MOSMO tool using MATLAB® Graphical User Interface Development Environment (GUIDE).

### 1.3 Scope of Research

The emphasis of this project will be on the aspect of developing the MOSMO algorithm model for the MIMO control system which can perform exactly as the Simulink® performs. This algorithm then will be used to find the parameters of the controller that gives non-dominated error.

MOSMO is then applied to different type of controllers and MIMO model as a case study to verify the effectiveness of MOSMO in tuning the Pareto-front parameters. Two case studies presented, forced circulation evaporator and remotely operated vehicle using PID controller.

The most common characterizations to be compared are Pareto-front point obtained by surrogate modeling and actual Pareto-front obtained by using brute force search approach. The MOSMO use RBF to approximate the actual Pareto-front of input design space. The performance of RBF also will be evaluated by comparing with Feed Forward (FF) back propagation neural network.

Two other well known types of optimization approach: Non-dominated Sorting Genetic Algorithm II (NSGA-II) and Strength Pareto Evolutionary Algorithm 2 (SPEA2) are used to compare MOSMO as an optimization algorithm. The performance evaluated based on Pareto-front performance and best compromise value.

The final scope is to develop an integrated and user friendly MOSMO tool using MATLAB® Graphical User Interface Development Environment (GUIDE) to aid designer in producing an accurate model of the original system for the control

system optimization purpose. The software package is intended for use with any Simulink® model. User will also enter the parameters to be optimized through GUI.

## **1.4 Thesis Outline**

This thesis consists of six chapters. This chapter gives a brief description of the objectives and scopes of the project. Chapter 2 consists of a literature review of surrogate modeling, multi-objective optimization and related works on multi-objective optimization using surrogate modeling. Chapter 3 presents the methodology and details of the MOSMO algorithm development process. In Chapter 4 and 5, the MOSMO is demonstrated to an evaporator and a ROV. Chapter 6 describes the development, user interface and usage of the MOSMO GUI Toolbox. Chapter 7 concludes this research.

## REFERENCES

1. Keane, A. and Nair, P. *Computational Approaches for Aerospace Design. The Pursuit of Excellence.* 2005.
2. Obayashi, S., Takahashi, S. and Takeguchi, Y. Niching and Elitist Models for MOGAs. *Springer*, 1998. *Lecture Notes in Computer Science*: pp. 260–269.
3. Fonseca, C. and Fleming, P. J. Genetic Algorithms for Multiobjective Optimization: Formulation, Discussion and Generalization. *Proc. 5th Int. Conf. Genetic Algorithms, S. Forrest, Ed. San Mateo, CA:Morgan Kaufmann*, 1993: pp. 416–423.
4. Fabian, T., Fisher, J. L., Sasieni, M. W. and Yardeni, A. *Purchasing Raw Material on a Fluctuating Market.* vol. vol. 7. 1959.
5. Kleijnen, J. P. A Comment on Blannings Metamodel for Sensitivity Analysis: The Regression Metamodel in Simulation. *Interfaces*, 1975. vol. 5, no. 3: pp. 2123.
6. Davis, P. K. and Bigelow, J. H. *Motivated Metamodels: Synthesis of Cause-Effect Reasoning and Statistical Metamodeling.* 2003. The Rand Corporation.
7. Ma, L., Xin, K. and Liu, S. Using Radial Basis Function Neural Networks to Calibrate Water Quality Model. *International Journal of Intelligent Systems and Technologies*, 2008. 3;2.
8. Santos, I. R. and Santos, P. R. Simulation Metamodels for Modeling Output Distribution Parameters. *Proceedings of the 2007 Winter Simulation Conference.* 2007.
9. Gu, L. A Comparison of Polynomial Based Regression Models in Vehicle Safety Analysis. *ASME Design Engineering Technical Conferences - Design Automation Conference, ASME, Pittsburgh, PA, September 9-12, 2001.* DAC-21063.
10. Mohaghegh, S. Quantifying Uncertainties Associated With Reservoir Simulation Studies Using Surrogate Reservoir Models. *SPE Annual Technical Conference and Exhibition (ATCE)*, 2006.

11. Ghoreyshi, M., Post, M. L. and Cummings, R. M. Transonic Aerodynamic Loads Modeling of X-31 Aircraft. *30th AIAA Applied Aerodynamics Conference, Louisiana*, 2012.
12. Tsuga, T. *Multi-Objective Optimization of Blast Simulation Using Surrogate Model*. Master's Thesis. George Mason University, Fairfax, VA. 2007.
13. Queipo, N., Haftka, R., Shyy, W., Goel, T., Vaidyanathan, R. and Tucker, P. Surrogate-based Analysis and Optimization. *Progress in Aerospace Sciences*, 2005. Vol. 41, No. 1, pp. 128.
14. Wang, G. and Shan, S. Review of Metamodeling Techniques in Support of Engineering Design Optimization. *Journal of Mechanical Design*, 2007. Vol. 129, No. 4, pp. 370380.
15. Amorim, T., Petrobras and Denis, J. S. Risk Analysis Speed-up with Surrogate Models. *SPE Latin American and Caribbean Petroleum Engineering Conference, Mexico*, 1618 April 2012.
16. Braconnier, T., Ferrier, M., Jouhaud, J. C., Montagnac, M. and Sagaut, P. Towards an Adaptive POD/SVD Surrogate Model for Aeronautic Design. *Institut Jean Le Rond d'Alembert, Universite Pierre et Marie Curie, UPMC*, August 25, 2010.
17. Kumaran, K., Mustafizur, M. R., Abdul, R. I. and Rosli, A. B. Surrogate Modelling to Predict Surface Roughness and Surface Texture When Grinding. *AISI 1042 Carbon Steel Scientific Research and Essay*: 7 (5) pp. 598–608.
18. Tommasi, L. D., Gorissen, D., Croon, J. and Dhaene, T. Surrogate Modeling of Low Noise Amplifiers based on Transistor Level Simulations. *The 7th International Conference on Scientific Computing in Electrical Engineering (SCEE 2008), Helsinki, Finland*, September 28 - October 3, 2008.
19. Zhang, J. *Hybrid and Uncertainty-Based Surrogate Modeling With Applications to Wind Energy*. Ph.D. Thesis. Faculty of Rensselaer Polytechnic Institute, Rensselaer Polytechnic Institute Troy, New York. July 2012.
20. Shi, L., Yang, R. J. and Zhu, P. A Method for Selecting Surrogate Models in Crashworthiness Optimization. *Structural and Multidisciplinary Optimization*. Springer, 2012.
21. Anand, K., Ra, Y., Reitz, R. D. and Bunting, B. Surrogate Model Development for Fuels for Advanced Combustion Engines. *Energy Fuels*, 2011. 25 (4), pp 14741484.
22. Gupta, A. and Bhakta, S. An Integrated Surrogate Model for Screening



- of Drugs Against Mycobacterium Tuberculosis. *Juornal of Antimicrob Chemother*, 2012. 67(6):1380-91.
23. Patra, A. K., Dalbey, K., Pitman, E., Stefanescu, E. R., Bursik, M. I., Sheridan, M. F., Calder, E. S. and Jones, M. D. Surrogate Models and Uncertainty Quantification for Hazard Map Construction, . *American Geophysical Union*, 2010.
  24. Koziel, S. and Ogurtsov, S. Rapid Optimization of Dielectric Rresonator Antennas Using Surrogate Models. *Antennas and Propagation Conference (LAPC), Loughborough*, 2011.
  25. Kleijnen, J. P. C. and Sargent, R. G. A Methodology for Fitting and Validating Metamodels in Simulation. *European Journal of Operational Research*, 2000. vol 120: pp. 14–29.
  26. Meckesheimer, M. *A Framework for Metamodel-based Design: Subsystem Metamodel Assessment and Implementation Issues*. Ph.D. Thesis. 2001.
  27. Abdullah, S. S. and Allwright, J. C. An Active Learning Approach For Radial Basis Function Neural Networks. *Jurnal Teknologi, Universiti Teknologi Malaysia*, 2006. 45(D): 77–96.
  28. Sacks, J., Welch, W. J., Mitchell, T. J. and Wynn, H. P. Design and Analysis of Computer Experiments. *Statistical Science*, 1989. 4(4): 409–435.
  29. Cressie, N. Spatial Prediction and Ordinary Kriging. *Mathematical Geology*, 1988. 20(4),: 405–421.
  30. Papadrakakis, M., Lagaros, M. and Tsompanakis, Y. Structural Optimization Using Evolution Strategies and Neural Networks. *Computer Methods in Applied Mechanics and Engineering*, 1998. 156(1-4): 309–333.
  31. Dyn, N., Levin, D. and Rippa, S. Numerical Procedures for Surface Fitting of Scattered Data by Radial Basis Functions. *SIAM Journal of Scientific and Statistical Computing*, 1986. 7(2): 639–659.
  32. Friedman, J. H. Multivariate Adaptive Regressive Splines. *The Annals of Statistics*, 1991. 19(1): 1–67.
  33. De Boor, C. and Ron, A. On Multivariate Polynomial Interpolation. *Constructive Approximation*, 1990. 6: 287–302.
  34. Varadarajan, S., Chen, W. and Pelka, C. J. Robust Concept Exploration of Propulsion Systems with Enhanced Model Approximation Capabilities. *Engineering Optimization*, 2000. 32(3): 309–334.
  35. Langley, P. and Simon, H. A. Applications of Machine Learning and Rule

- Induction. *Communications of the ACM*, 1995. 38(11): 55–64.
36. Wang, L., Beeson, D., Akkaram, S. and Wiggs, G. Gaussian Process Metamodels for Efficient Probabilistic Design in Complex Engineering Design Spaces. *ASME 2005 International Design Engineering Technical Conferences and Computers and Information in Engineering Conference*, ASME, Long Beach, California USA, 2005: DETC2005–85406.
  37. Girosi, F. and Poggio, T. Networks and the Best Approximation Property. *Biological Cybernetics*, 1990. 63: 169–176.
  38. Jin, R., Chen, W., and Simpson, T. W. Comparative Studies of Metamodeling Techniques Under Multiple Modeling Criteria. *Struct. Multidiscip. Optim.*, 2001. 23(1): pp. 1–13.
  39. Samsudin, S. I. *Modern and Intelligent Control of Active Magnetic Bearing*. Master's Thesis. Faculty of Electrical Engineering Universiti Teknologi Malaysia. 2006.
  40. Tsa, H., Wang, Y. and Itoh, T. An Unconditionally Stable Extended (USE) Finite-Element Time-Domain Solution of Active Non-linear Microwave Circuits Using Perfectly Matches Layer,. *IEEE Transaction on Microwave Theory and Technique*, 2002. Vol. 50, No. 10: 2226–2232.
  41. Rashid, K. *Optimization in Electromagnetic Using Computational Intelligence*. Ph.D. Thesis. Imperial College of Science, Technology and Medicine, Department of Electrical and Electronics Engineering. 2000.
  42. Sultan, M. M. A., Abdullah, S. S. and Osman, D. Optimization of PID Controllers for a Fluid Mixing System Using Metamodeling Approach. *3rd IEEE Conference on Industrial Electronics and Applications, ICIEA*, 2008: 1282–1286.
  43. Sultan, M. M. A. *Optimization of the Controller Parameters for a Fluid Mixing System Using Metamodeling Technique*. Master's Thesis. Faculty of Electrical Engineering, Universiti Teknologi Malaysia. 2008.
  44. Sultan, M. M. A., Abdullah, S. S., Mohamed, Z. and Ahmad, M. A. Optimization of PID Controllers for a Flexible Robot Manipulator Using Metamodeling Approach. *10th International Conference on Control, Automation, Robotics and Vision, ICARCV 2008*, 2008: 555–559.
  45. Ab Malek, M. N. and Sultan, M. M. A. Evolutionary Tuning Method for PID Controller Parameters of a Cruise Control System Using Metamodeling. *Modelling and Simulation in Engineering*, 2009. Volume 2009, Article ID 234529.

46. Sultan, M. M. A., Abdullah, S. S., Ahmad, M. A. and Hambali, N. Optimization of PID controllers for Cartesian Coordinates Control of Hovercraft System Using Metamodeling Approach,. 18-20, July 2008.
47. Gary Wang, G. and Shan, S. Review of Metamodeling Techniques in Support of Engineering Design Optimization. *ASME Transactions, Journal of Mechanical Design*, 2006. R3T 5V6.
48. Simpson, T. W., Peplinski, J. D., Koch, P. N., and Allen, J. K. Metamodels for Computer-based Engineering Design: Survey and Recommendations. *Engineering with Computers*, 2001. No. 2, Vol. 17: pp. 129150.
49. Forrester, A. I. J. and Keane, A. J. Recent Advances in Surrogate-based Optimization. *Progress in Aerospace Sciences*, 2009. Vol. 45: pp. 5079.
50. Jones, D., Schonlau, M., and Welch, W. Efficient Global Optimization of Expensive Black-Box Functions. *ournal of Global Optimization*, 1998. Vol. 13, No. 4: pp. 455 – 492.
51. Huang, D., Allen, T. T., Notz, W. I. and Zeng, N. Global Optimization of Stochastic Black-Box Systems via Sequential Kriging Meta-Models. *Journal of Global Optimization*, 2006. Vol. 34, No. 3: pp. 441–466.
52. Viana, F. A. C., Haftka, R. T., and Watson, L. T. Why Not Run The Efficient Global Optimization Algorithm with Multiple Surrogates. April 12-15 2010.
53. Shan, S. and Wang, G. G. An Efficient Pareto Set Identification Approach for Multi-objective Optimization on Black-box Functions. *Transactions of the ASME, Journal of Mechanical Design*, 2005. 127,: 866–874.
54. Shan, S. and Wang, G. Reliable Design Space and Complete Single-loop Reliability-based Design optimization. :. *Reliab Eng Sys Safety*, 2008. 93(8): 12181230.
55. Kumano, T. Multidisciplinary Design Optimization of Wing Shape for a Small Jet Aircraft Using Kriging Model. *44th AIAA Aerospace Sciences Meeting and Exhibit*, Jannuary 2006: pp. 1–13.
56. Loshchilov, I., Schoenauer, M. and Sebag, M. A Pareto-Compliant Surrogate Approach for MultiobjectiveOptimization. *Genetic and Evolutionary Computation Conference 2010 (GECCO-2010), Portland, OR: United States*, 2012.
57. Ahmed, M. and Qin, N. Surrogate-Based Multi-Objective Aerothermodynamic Design Optimization of Hypersonic Spiked Bodies. *AIAA Journal*, 2012. Vol. 50, No. 4.

58. Ricardo, M. P., Andr, R. D. C., Curran, C. and Afzal, S. Comparison of Surrogate Models in a Multidisciplinary Optimization Framework for Wing Design. *AIAA Journal*, May 2010. Vol. 48, No. 5.
59. Giunta, A. A., Balabanov, V., Haim, D., Grossman, B., Mason, W. H., Watson, L. T. and T., H. R. Multidisciplinary Optimization of a Supersonic Transport Using Design of Experiments theory and Response Surface Modeling. *Aeronautical Journal*, 1997. 101(1008): pp. 347–356.
60. Sacks, J., Welch, W. J., Mitchell, T. J. and Wynn, H. P. Design and Analysis of Computer Experiments. *Statistical Science*, 1989. 4(4): pp. 409–435.
61. Simpson, T. W., Peplinski, J., Koch, P. and Allen, J. Meta-models for Computer Based Engineering Design: Survey and Recommendations. *Engineering with Computers*, 2001. Vol. 17, No. 2: pp. 129–150.
62. McKay, M. D., Beckman, R. and Conover, W. A Comparison of Three Methods for Selecting Values of Input Variables from a Computer Code. *Technometrics*, 1979. Vol. 21: pp. 239–245.
63. Iman, R. and Conover, W. Small Sample Sensitivity Analysis Techniques for Computer Models with an Application to Risk Assessment. *Communications in Statistics, Part A. Theory and Methods*, 1980. Vol. 17: pp. 1749–1842.
64. Kleijnen, J., Sanchez, S., Lucas, T. and Cioppa, T. A Users Guide to the Brave New World of Designing Simulation Experiments. *INFORMS Journal on Computing*, 2005. Vol. 17, No. 3: pp. 263–289.
65. Broomhead, D. S. and Lowe, D. Multivariable Functional Interpolation and Adaptive Networks. *Complex Systems*, 1988. 2: pp. 321–355.
66. Lee, C. C. Fuzzy Logic in Control Systems: Fuzzy Logic Controller Part 1. *IEEE Transactions on Systems, Man & Cybernetics*, 1990. Vol.20, No. 2,: pp. 404–419.
67. Ham, F. M. and Kostanic, I. *Principles of Neurocomputing for Science and Engineering*. Singapore: McGraw-Hill. 2001.
68. Newell, R. B. and Lee, P. L. *Applied Process Control: A Case Study, Process Control Group Department of Chemical Engineering University of Queensland*. Prentice Hall, Australia. 1989.
69. Koh, T. H., Lau, M. W. S., Seet, G. and Low, E. Control Module Scheme for an Underactuated Underwater Robotic Vehicle. *Intell Robot Syst.*, 2006. 46: pp. 43–58.
70. Fossen, T. I. Guidance and Control of Ocean Vehicles. *John Wiley and Sons*

*Ltd, England, 1994.*

71. Koh, T., Lau, M., Low, E. S. G., Swei, S. and Cheng, P. Development and Improvement of an Underactuated Remotely Operated Vehicle (ROV). *Proc. MTS/IEEE Int. Conf. Oceans*, 2002. Biloxi, MS: pp. 2039–2044.
72. Fossen, T. I. *Guidance and Control of Ocean Vehicles*. John Wiley and Sons Ltd. England, 1994.