

# Application of Microwave Moisture Sensor for Determination of Oil Palm Fruit Ripeness

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This paper describes the development of a low cost coaxial moisture sensor for the determination of moisture content (30 % to 80 % wet-weight basis) of the oil palm fruits of various degree of fruit ripeness. The sensor operating between 1 GHz and 5 GHz was fabricated from an inexpensive 4.1 mm outer diameter SMA coaxial stub contact panel which is suitable for single fruit measurement. The measurement system consists of the sensor and a PC-controlled vector network analyzer (VNA). The actual moisture content was determined by standard oven drying method and compared with predicted value of fruit moisture content obtained using the studied sensor. The sensor was used to monitor fruit ripeness based on the measurement of the phase or magnitude of reflection coefficient and the dielectric measurement software was developed to control and acquire data from the VNA using Agilent VEE. This software was used to calculate the complex relative permittivity from the measured reflection coefficient between 1GHz and 5 GHz.

**Keywords:** Vector network analyzer, moisture content, reflection coefficient, oil palm fruits, microwave sensors, dielectric constant

## 1. INTRODUCTION

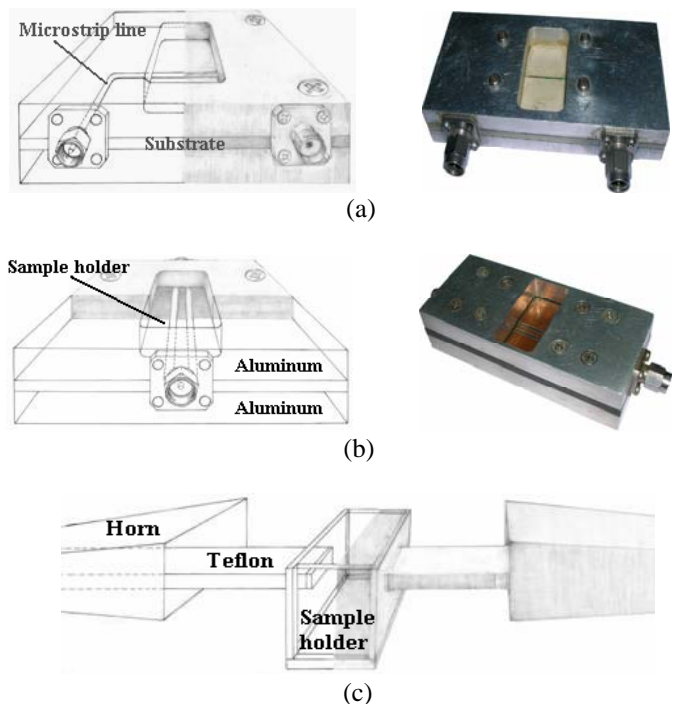
PALM OIL has become increasingly popular as it provides rich sources of  $\alpha$  and  $\beta$ -carotene and vitamin E, which play important roles in blood coagulation, suppression of cholesterol production and cancer inhibition. Nutrition as well as environment protection will have a prominent role in consumer's choice of edible oil consumption. Besides its nutritional value, it is a well-known raw material for oleo chemical industry and bio-fuel for automobiles.

Palm oil is obtained from the mesocarp of the oil palm fruits. Researchers [1], [2] found that the quality of palm oil is closely related to the moisture content  $m.c$  in the fruits, as well as the fruit ripeness. When the oil palm fruit is ripening, the oil content reaches the maximum, but the moisture content  $m.c$  reaches the minimum (~30%  $m.c$ ) in the fruit [1], [2]. Therefore, the close relationship between the moisture and oil contents in the mesocarp gives a possibility of using percentage of moisture content  $m.c$  as a parameter to gauge the mesocarp ripeness and the harvesting time.

Various microwave sensors have been utilized to estimate the ripeness of oil palm fruits, such as microstrip sensor (MWG) [12], coplanar sensor (CBCPW) [13], rectangular dielectric waveguide (RDWG) [15], monopole [16] and open-ended rectangular waveguide (OERWG) [17] as shown in Fig.1. Microstrip and coplanar sensors based on attenuation measurement were the first to have been successfully used to estimate the amount of moisture content  $m.c$  in the oil palm fruits. Unfortunately, the sensors require laborious sample preparation as the fresh mesocarp of the oil palm fruit has to be separated from the nut and crumbled to form a semi-solid sample. The preparation of the fruit sample is very time consuming. The comparison of previous work features for oil palm

fruit measurements using microwave sensors was tabulated in Tab.1.

In this study, the open-ended coaxial probe is used as a moisture sensor to determine the moisture content  $m.c$  of oil palm fruits of various degrees of fruit ripeness at room temperature by using reflection techniques. Furthermore, a model is developed to describe the relation between reflection coefficient and moisture content  $m.c$  of the oil palm mesocarp for frequency range 1 GHz to 5 GHz.



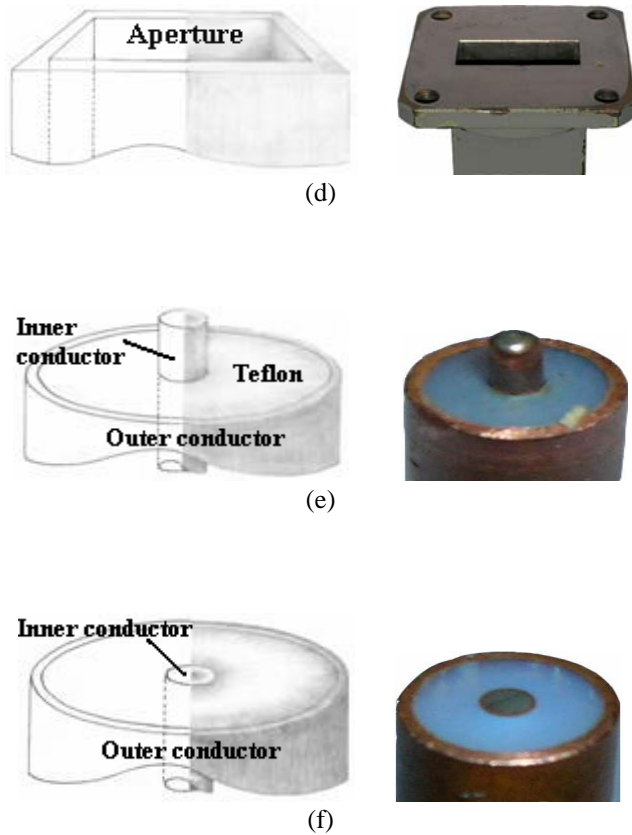


Fig.1 (a) Microstrip sensor (MWG) [12] (b) Coplanar sensor (CBCPW) [13] (c) Rectangular dielectric waveguide (RDWG) [15] (d) Rectangular waveguide (OERWG) [17] (e) Monopole [16] (f) coaxial waveguide (OECWG) (This work).

## 2. EXPERIMENT AND METHODS

Experimentation planning includes fabrication and construction of open-ended coaxial sensor, oil palm sample preparation, sensor calibration, reflection measurements and moisture content  $m.c$  measurements in this study.

### A. Fabrication of sensor

The probe was fabricated from a 12.7 mm by 12.7 mm square flange, SMA stub contact panel. The stub was machined flat and polished. The diameter of the inner and outer conductors was 1.3 mm and 4.1 mm, respectively. The dielectric material separating the inner and outer conductor was Teflon (PTFE), as shown in Fig.2.

### B. Sensor calibration

For this measurement calibration, no loss was assumed for the electromagnetic wave when it is transmitted in offset coaxial line (see Fig.2 (a)). Thus, the error network calibration parameters of  $S_{11}$  and  $S_{22}$  in Fig.2 (b) are equal to zero. Finally, the concept of Fig.2 (b) was simplified as in Fig.2 (c), where the  $S_{12}$  and  $S_{21}$  are replaced by transmission factor,  $\exp(-jk_c d_c)$  [18].

$$\Gamma_{Actual} = \Gamma_{AA'} \exp(2jk_c d_c) \quad (1)$$

where  $d_c$  and  $k_c$  are the physical length (in meter) and propagation constant of coaxial line, respectively.

Table 1 Comparison of previous work features for oil palm fruit measurements using microwave sensors

Type of sensor	Comparison features of microwave sensor for oil palm fruits measurements							
	Operating frequency	Nondestructive test	Set-up speed	Cost of sensor	One-port measurements	Single fruit measurements	Sensitivity	Precision
MWG, [12]	10.7 GHz	No	Slow	Low	No	No	Good	Good
CBCPW, [13]	2.2 GHz	No	Slow	Low	No	No	Good	Good
Commercial HP 85070B OECWG, [14]	0.13 – 20 GHz	No	Slow	Expensive	Yes	No	Good	Good
RDWG, [15]	8 – 12 GHz	No	Slow	Low	No	No	Good	Good
Monopole, [16]	0.5 GHz	Yes	Very fast	Very low	Yes	Yes	Very good	Poor
OERWG, [17]	8 – 12 GHz	No	Fast	Very low	Yes	No	Good	Good
OECWG (This work)	1 – 5 GHz	Yes	Very fast	Very low	Yes	Yes	Good	Good

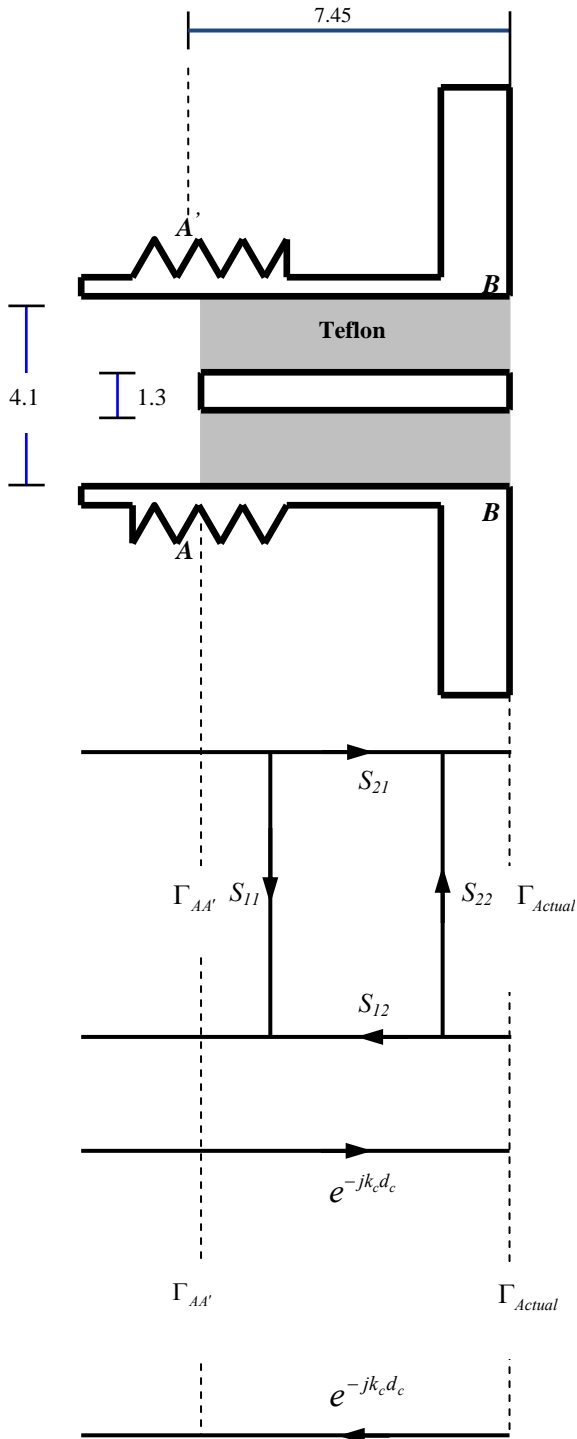


Fig.2 (a) Open-ended coaxial sensor with physical length,  $d_c$  equal to 7.45 mm. (b) Error network calibration. (c) Alternative transmission line calibration.

### C. Reflection measurements

The measurement consists of a computer controlled HP 8720B vector network analyzer (VNA) that operates between 1 GHz and 5 GHz. The moisture sensor was connected to VNA port by coaxial cable as shown in Fig.3. All reflection measurements of fruit samples were carried out at room temperature ( $25 \pm 1$ ) °C.

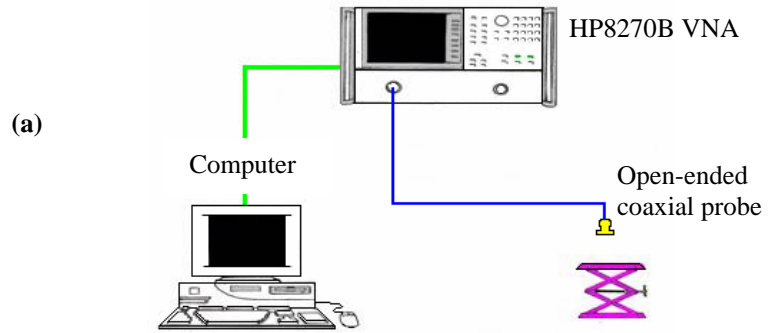


Fig.3 Experimental set-up

### D. Sample preparation

Twenty bunches of tenera variety from different oil palms were selected from the university farm for this study. The surface of the fruit was wiped dry to free excess surface moisture. Part of the fresh mesocarp of each fruit was sliced in the longitudinal direction to ensure good contact between the surface of the mesocarp and the open-ended coaxial probe as illustrated in Fig.4.

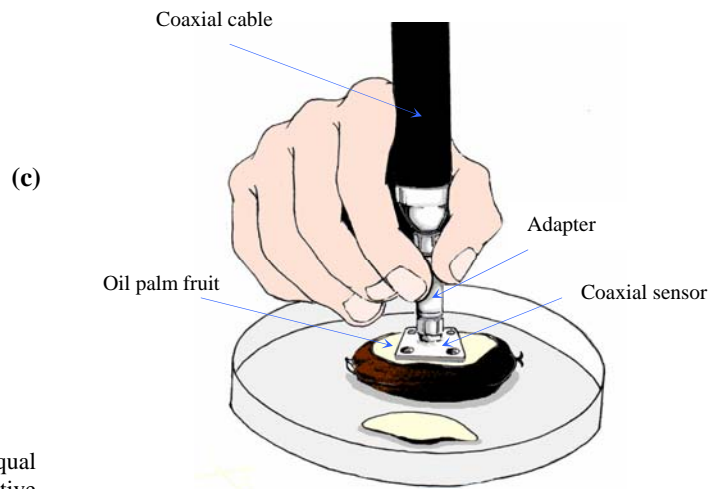


Fig.4 Part of the experimental set-up

### E. Moisture content *m.c* measurements

The actual moisture content of the fruit sample was determined by PORIM test method or standard oven drying method [7]. Before drying, the single fruit sample was weighted by digital scale and the value was recorded. Next, the fruit sample was dried at  $(103 \pm 2)^\circ\text{C}$  in the oven for two to three days. During the drying time, the fruit was taken out and cooled off, then re-weighed once every day to ensure the weight of the fruit reached a constant level. The relative moisture content *m.c* of oil palm fruit, in percentage (wet basis), was calculated from:

$$\% m.c = \frac{m_{\text{Before\_Dry}} - m_{\text{After\_Dry}}}{m_{\text{Before\_Dry}}} \times 100\% \quad (2)$$

where  $m_{\text{Before\_Dry}}$  and  $m_{\text{After\_Dry}}$  are the weight of fruit sample before and after drying in the oven, respectively. It is important to emphasize that the weight of the fruit nut is accounted for in the calculation.

### 3. RELATIVE PERMITTIVITY CALCULATION

In this study, the measured reflection coefficient  $\Gamma_{\text{Actual}}$  of oil palm mesocarp was converted to relative permittivity  $\epsilon_r$  via [8]:

$$\epsilon_r = \frac{Y_o}{j\omega C_T} \left( \frac{1 - \Gamma_{\text{Actual}}}{1 + \Gamma_{\text{Actual}}} \right) \quad (3)$$

where  $\omega$  is the angular frequency. The  $Y_o$  and  $C_T$  are the characteristic admittance and the total aperture capacitance of the coaxial sensor, respectively. The characteristic admittance  $Y_o$  is expressed as:

$$Y_o = \frac{2\pi\sqrt{\epsilon_o\epsilon_c}}{\sqrt{\mu_o} \ln(b/a)} \quad (4)$$

where  $\epsilon_o$  and  $\mu_o$  are the free space permittivity and permeability, respectively.  $\epsilon_c$  is the dielectric constant of the Teflon filling the coaxial line. The  $a$  and  $b$  are the inner and outer radius of the coaxial conductors, respectively. The total capacitance  $C_T$  is calculated from [9]:

$$C_T = 2.38\epsilon_o\epsilon_r(b-a) \quad (5)$$

For this design sensor, the values of  $Y_o$  and  $C_T$  are equal to 0.0203 S and 0.03 pF.

## 4. RESULTS AND DISCUSSION

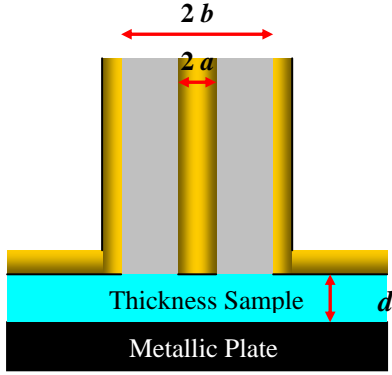
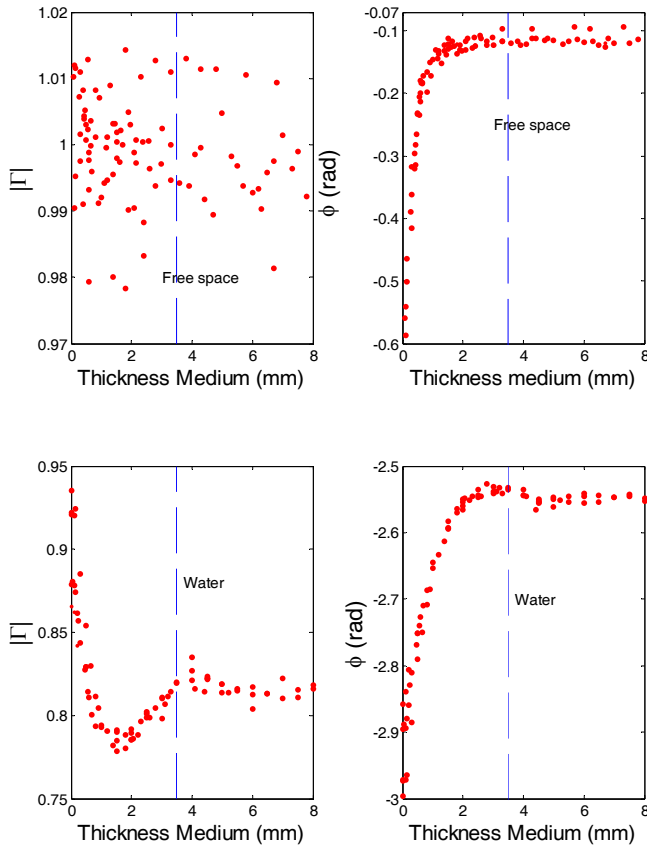
The measurement results were presented in terms of reflection coefficient  $\Gamma$  and the comparison with the analytical [19] and numerical calculations was carried out. Subsequently, the estimation of complex relative permittivity  $\epsilon_r$  of the oil palm mesocarp based on measured reflection coefficient  $\Gamma_{\text{Actual}}$  was calculated using (3).

### A. Calibration at the aperture of the coaxial sensor

The conventional one-port calibration normally involves measuring an open, a short and a reference material (water) of which the properties are known. The calibration procedures are implemented using the basic error-correction method as is shown in Fig.2(b) [10]. However, we have learned that the measuring of standard short is quite difficult to determine accurately and precisely, since it depends on how dense the coaxial probe is pressed to a metal material. In addition, a small air gap between aperture probe and metal material will cause significant measuring errors. To solve this problem, a perfect standard of short calibration must be designed to suite the probe which is used. Even if the perfect short standard has been designed, the calibration using the basic error-correction method gives more repeatable and precise measurement results than the transmission method, which only inputs the physical length of the probe. Nevertheless, by using the transmission line approach, the cost and measuring time will be reduced. In addition, the measurement uncertainties will not contribute to the calibration procedures, since the calibration transmission model [Eq (1)] is based on the theoretical principle.

### B. Significant sensing area of the coaxial sensor

The significant sample thickness is estimated based on distance  $d$  at which the measured reflection coefficient  $\Gamma_{\text{Actual}}$  becomes constant when the metallic plate is moved away from the probe surface in a sample as shown in Fig.5. Fig.6 shows that when the sample thickness exceeds 3.5 mm, the measured magnitude and phase of reflection coefficient  $\Gamma$  at 4 GHz remains unchanged for half-infinite free space and water, respectively. It can be concluded that the minimum significant thickness of sample under test is assumed to be 3.5 mm for this study probe below 4 GHz.

Fig.5 Finite thickness sample,  $d$  backed by metallic plateFig.6 Variation in magnitude and phase of reflection coefficient  $\Gamma$  with medium thickness (free space and water) for 4 GHz

### C. Variation in reflection coefficient $\Gamma$ with frequency for different moisture content $m.c$

The variations in magnitude  $|\Gamma|$  and phase  $\phi$  of the reflection coefficient with moisture content  $m.c$  for different frequencies were shown in Fig.7 and Fig.8, respectively. The measured magnitude  $|\Gamma|$  and phase  $\phi$  were in good agreement with Finite Element (FEM) simulation and analytical calculation results. The relative complex permittivity  $\epsilon_r$  of the oil palm mesocarp, used in simulations and calculation, was obtained from measurements using commercial HP 85070B probe. The figures suggested that  $\phi$  vary linearly with the amount of moisture content  $m.c$  in the oil palm mesocarp, but not  $|\Gamma|$ , since  $|\Gamma|$  illustrates a quadratic plotted shape with respect to moisture content  $m.c$  at frequency up to 3 GHz. Besides, the measured data of  $|\Gamma|$  were less precise than phase  $\phi$ . It was also observed that the data for  $|\Gamma|$  was less sensitive to moisture content up to 4 GHz. Obviously, magnitude of reflection coefficient  $|\Gamma|$  was less suitable in monitoring the fruit ripeness based on bandwidth measurements. In contrast, the sensitivity in  $\phi$  with respect to moisture content  $m.c$  is quite constant for all frequencies. Therefore, it was suggested that the phase of reflection coefficient  $\phi$  was the most flexible parameter to relate the moisture content  $m.c$  of mesocarp. Finally, the empirical formulation of moisture content  $m.c$  as a function of phase reflection coefficient  $\phi$  was created by using Gaussian Elimination Method as:

$$\% m.c = \left\{ \begin{aligned} & (1.625f^4 - 14.6265f^3 + 40.672f^2 - 25.4363f - 53.4792)\phi + \\ & (-0.0564f^3 + 0.5604f^2 - 5.3215f + 33.377) \end{aligned} \right\} \quad (6)$$

where  $\phi$  and  $f$  are the phase reflection coefficient (in rad) and operating frequency (in Hz), respectively.

### D. Variation in relative complex permittivity, $\epsilon_r$ with frequency for different moisture content $m.c$ of oil palm mesocarp

The relationship between both dielectric constant  $\epsilon_r'$  and loss factor  $\epsilon_r''$  of oil palm mesocarp and frequency (1 GHz to 5 GHz) for various percentages of water content  $m.c$  was shown in Fig.9 and Fig.10. The dielectric constant  $\epsilon_r'$  is calculated from measured reflection coefficient  $\Gamma_{Actual}$  using (3), as well as the comparison of the measurements using commercial HP85070B coaxial probe. Fig.9 revealed that the predicted and measured dielectric constant  $\epsilon_r'$  overall decreased with the increase in frequency.

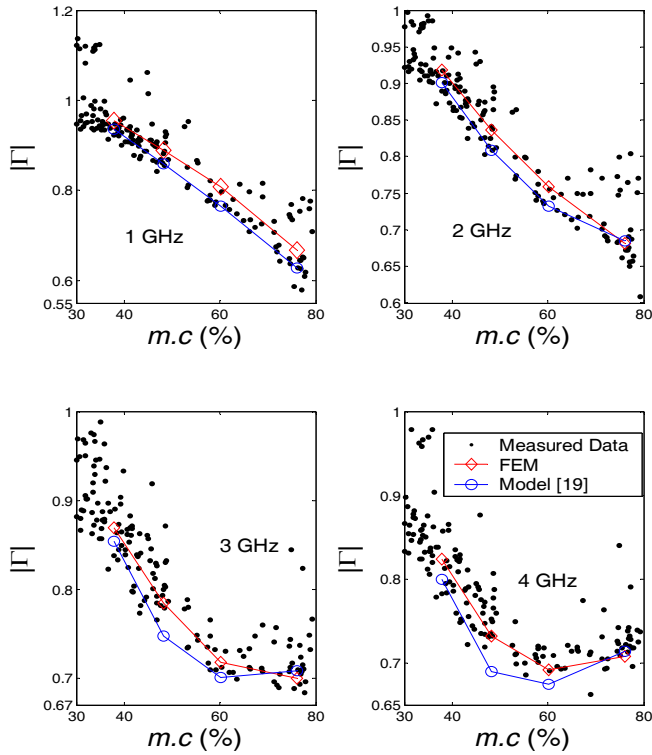


Fig.7 Variation in reflection coefficient magnitude,  $|\Gamma|$  with percentage moisture content  $m.c$

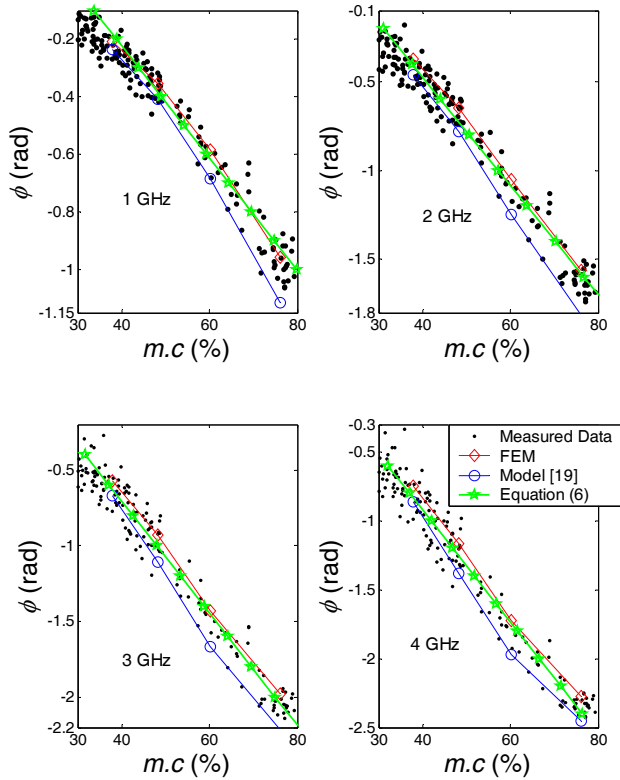


Fig.8 Variation in phase shift  $\phi$  with percentage moisture content  $m.c$

In all measured fruits, the loss factor  $\epsilon_r''$  decreased at low frequency, reached a broad minimum between 1 and 3 GHz, then increased again as shown in Fig.10. This behavior is influenced by ionic conductivity at lower frequencies, since dielectric properties in agriculture are believed to be primary dependant on water activity and ionic conductivity of fluids contained in their cellular structure. Overall, the estimated relative permittivity  $\epsilon_r$  of oil palm mesocarp using (3) corresponded well with measurements using commercial HP85070B coaxial probe. Based on this study, the relationship between dielectric constant  $\epsilon_r'$  and percentage of moisture content in mesocarp, for example at 3 GHz, is obtained and listed in Tab.2. The decrease in relative dielectric constant  $\epsilon_r'$  of the oil palm mesocarp is presumably caused by the displacement of water by oil and fibers contents. The water content  $m.c$  is the main contributor to the value of the dielectric constant of the oil palm mesocarp, since the dielectric constant of water ( $\epsilon_r' = 80$  at DC) is far greater than that of other substances in the oil palm mesocarp (such as oil and fiber). In addition, the orientation of water molecules is sensitive to the microwave frequencies, especially at 2.45 GHz.

Table 2 Relationship between % water content  $m.c$  and dielectric constant  $\epsilon_r'$  of oil palm mesocarp for 3 GHz at  $(25 \pm 1)^\circ\text{C}$

Water Content, $m.c$ (%)	Dielectric Constant, $\epsilon_r'$
30 – 40	10 – 15
40 – 50	15 – 25
50 – 60	25 – 35
60 – 70	35 – 52
70 – 80	52 – 62

In this work, the relative permittivity  $\epsilon_r$  of oil palm mesocarp, ranging from 30 % to 80 % of water content at  $(25 \pm 1)^\circ\text{C}$ , can be represented by a sum of the two relaxation processes dielectric model as:

$$\epsilon_r = \epsilon_\infty + \frac{\epsilon_s - \epsilon_1}{[1 + (j\omega a_1 \tau_1)^{a_2}]^{a_3}} + \frac{\epsilon_1 - \epsilon_\infty}{1 + (j\omega \tau_2)^{a_4}} - \frac{j\sigma}{\omega \epsilon_o} \quad (7)$$

where  $\tau_1$  and  $\tau_2$  are the relaxation time for low and high-



frequency processes, respectively. The  $\epsilon_s$  and  $\epsilon_1$  are the static permittivity for first and second relaxation processes, as well as  $\epsilon_\infty$  is the optical permittivity. The  $\omega$  is the angular frequency and  $\sigma$  is the conductivity of oil palm mesocarp at lower frequencies. The  $a_1$ ,  $a_2$ ,  $a_3$  and  $a_4$  are the empirical constants, which are determined by optimized, up to 120 set measured data using commercial HP85070B probe. The parameters in (7) as a function of water content  $m.c$  (%) are listed in Appendix. Equation (7) is quite in agreement with random selected measured data using the study coaxial probe. At moisture above 70 %, the higher measurement uncertainty appeared due to the water accumulated at the surface between the sensor and the fruit when the sensor is pressed firmly to the sample fruits.

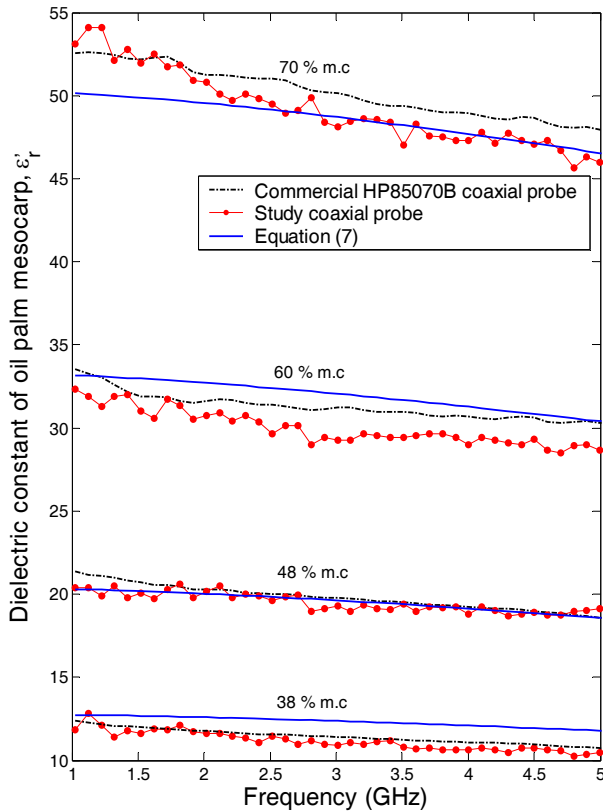


Fig.9 The variations in dielectric constant,  $\epsilon'_r$  of oil palm mesocarp with frequency for various % moisture content at  $(25 \pm 1)^\circ\text{C}$

#### 4. CONCLUSION

For this study, the coaxial sensor is suitable to determine the fruit quality based on measured phase of the reflection coefficient  $\phi$  alone for medium fruit up to 5 GHz. The estimated relative permittivity  $\epsilon_r$  of oil palm mesocarp from directly inverse solutions corresponded well with

measurements using commercial HP85070B coaxial probe. The microwave sensor can be also applied to other fields such as soil moisture determination and quality control of latex.

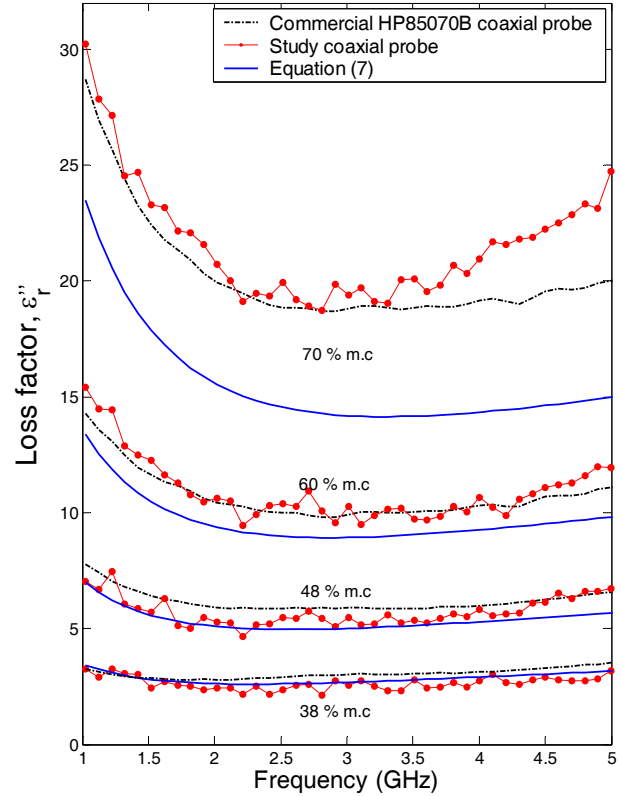


Fig.10 The variations in loss factor  $\epsilon''_r$  of oil palm mesocarp with frequency for various % moisture content at  $(25 \pm 1)^\circ\text{C}$

#### APPENDIX

The parameters in (7) as a function of water content  $m.c$  (%) are listed below:

$$\epsilon_s = \left[ \begin{array}{l} -3.9899 \times 10^{-4} (m.c)^3 + 8.0046 \times 10^{-2} (m.c)^2 \\ -3.8988 (m.c) + 67.258 \end{array} \right] \pm 0.9792$$

$$\epsilon_1 = \left[ \begin{array}{l} -1.8394 \times 10^{-5} (m.c)^4 + 3.8076 \times 10^{-3} (m.c)^3 \\ -0.27371 (m.c)^2 + 8.7394 (m.c) - 98.783 \end{array} \right] \pm 0.5093$$

$$\epsilon_\infty = v_{\text{water}} \epsilon_\infty^{\text{Water}} + (0.84 - v_{\text{water}}) \epsilon_\infty^{\text{Oil}} + 0.16 \epsilon_\infty^{\text{Fiber}}$$

$$v_{\text{water}} = \frac{0.01m.c(0.16\rho_{\text{Fiber}} - 0.16\rho_{\text{Oil}} + \rho_{\text{Oil}})}{\rho_{\text{Water}} - 0.01\rho_{\text{Water}} + 0.01\rho_{\text{Oil}}}$$

where  $\varepsilon_{\infty}^{\text{Water}} = 4.9$ ,  $\varepsilon_{\infty}^{\text{Oil}} = 2.5$ ,  $\varepsilon_{\infty}^{\text{Fiber}} = 2.2$ ,  $\omega = 2\pi f$   
 $\rho_{\text{water}} = 0.9959 \text{ gml}^{-1}$ ,  $\rho_{\text{Oil}} = 0.9073 \text{ gml}^{-1}$  and  
 $\rho_{\text{Fiber}} = 0.9200 \text{ gcm}^{-3}$

$$\sigma = 6.2861 \times 10^{-4} (m.c)^2 - 3.6521 \times 10^{-2} (m.c) + 6.3931 \times 10^{-1} \pm 0.02482 \Omega^{-1} \text{m}^{-1}$$

$$a_1 = -2.2890 \times 10^{-4} (m.c)^2 + 3.6771 \times 10^{-2} (m.c) + 1.4734 \times 10^{-1} \pm 0.0008234$$

$$a_2 = -3.5634 \times 10^{-6} (m.c)^2 - 4.5790 \times 10^{-4} (m.c) + 1.0124 \pm 0.00002904$$

$$a_3 = 4.0888 \times 10^{-5} (m.c)^2 - 8.7443 \times 10^{-3} (m.c) + 1.1543 \pm 0.0008381$$

$$a_4 = 3.5374 \times 10^{-5} (m.c)^2 - 2.5052 \times 10^{-3} (m.c) + 8.7535 \times 10^{-1} \pm 0.004263$$

#### ACKNOWLEDGMENT

This work was supported in part by the Ministry of Science, and Environment of Malaysia under project IRPA 09-02-04-0460-EA001.

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Received November 10, 2009.

Accepted February 3, 2010.