

MODELLING OF TRAFFIC DELAYS AT ROUNDABOUT USING VISSIM
MICROSIMULATION MODEL

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ABSTRACT

Delay is one of the significant parameters used for the operational performance evaluation of roundabouts. Even though there are various methods for estimating delays at the roundabout, the results can differ from actual delays on the field for Malaysian traffic conditions. Most of the existing models, such as HCM 2010, do not consider the impact of the geometric parameters on delays, besides the driver behaviour is different. Therefore, this study used the VISSIM microsimulation model to assess the impacts of traffic and geometric characteristics on delays at roundabouts. Video recording technique was used to collect data at Senai roundabout such as the entry flow rate, circulating flow rate, critical gap, follow-up headway, vehicle desired speed, and delay. The data collected were used to develop the base model scenario in VISSIM. The calibration and validation of the base model were then conducted using entry traffic flow, circulating traffic flow, and delays measured in the field. In VISSIM, three basic scenarios are defined, namely, the central island diameter ($D_i = 60\text{m}, 70\text{m},$ and 80m), entry width ($W_e = 5\text{m}, 9\text{m},$ and 12m), and the circulating roadway width ($W_c = 6\text{m}, 9\text{m},$ and 12m). For each scenario case, additional scenarios were created utilizing different traffic flow rates (350-2000 veh/hr), representing low, medium, and high traffic flow rates; as a result, 351 scenarios are developed in all. Based on the outcomes of the 351 scenarios, an exponential mathematical model is developed for estimating roundabout delay using the regression analysis technique. The entry flow rate and the circulating flow rate are found to have a strong positive correlation with delay. This implies that an increase in the entry flow rate or the circulating flow rate increases the delay. In terms of geometric parameters influence on the delay, the entry width and circulating roadway width exhibit a strong negative correlation with delay ($p\text{-value} < 0.05$). In other words, increasing the width of the entry or circulating roadway leads to delay reduction. In contrast, the central island diameter has no significant impact on the delay ($p\text{-value} > 0.05$); thus, this parameter is omitted from the final model. With an R^2 of 0.79, the derived model is statistically significant at a 95% confidence level, which implies that traffic flow and the geometric parameters account for an approximate of 79% variation in the delay. Moreover, the value of the coefficient of multiple correlations ($R = 0.89$) affirmed that the relationship between delay and the combined influence of the independent variables is significantly strong. Therefore, this study would serve as a more accurate guide for determining the acceptable degree of service for Malaysian roundabouts to justify related expenditures. It is advised that the proposed model be considered into Malaysia's guidance for performance analysis on at-grade junctions, particularly roundabouts.

ABSTRAK

Kelengahan adalah salah satu parameter penting yang digunakan untuk penilaian prestasi operasi bulatan. Walaupun terdapat pelbagai kaedah untuk menilai kelengahan di bulatan, keputusannya boleh berbeza daripada kelengahan sebenar di tapak untuk keadaan lalulintas Malaysia. Kebanyakan model semasa, seperti HCM2010, tidak mengambilkira kesan parameter geometri terhadap kelengahan, selain itu kelakuan pemandu juga berbeza. Oleh itu, kajian ini menggunakan model mikrosimulasi VISSIM untuk menilai kesan lalulintas dan ciri-ciri geometri terhadap kelengahan di bulatan. Teknik rakaman video telah digunakan untuk mengumpulkan data di bulatan Senai antaranya kadar aliran masuk, kadar aliran berpusing, sela kritikal, jarak kepala susulan, kelajuan dikehendaki kenderaan, dan kelengahan. Data yang dikumpulkan digunakan untuk membangunkan scenario model asas di VISSIM. Proses penentukuran dan pengesahan model asas telah dilakukan menggunakan aliran lalulintas masuk, aliran lalulintas berpusing dan kelengahan yang telah diukur di tapak. Di dalam VISSIM, tiga senario asas telah ditakrifkan, iaitu, diameter pulau tengah ($D_i = 60\text{m}, 70\text{m}, \text{ and } 80\text{ m}$), lebar masuk ($W_e = 5\text{m}, 9\text{m}, \text{ and } 12\text{ m}$), dan lebar jalan pusing ($W_c = 6\text{ m}, 9\text{m}, \text{ and } 12\text{m}$). Bagi setiap kes senario, senario tambahan direka menggunakan kadar aliran lalulintas berbeza (350-2000 veh/hr), mewakili kadar aliran lalulintas rendah, sederhana dan tinggi; hasilnya. sebanyak 351 senario telah dibangunkan secara keseluruhan. Berdasarkan dapatan 351 senario, sebuah model matematik eksponen telah dibangunkan untuk menganggar kelengahan bulatan menggunakan teknik analisa regresi. Kadar aliran masuk dan kadar aliran berpusing telah didapati mempunyai korelasi positif yang kuat dengan kelengahan. Ini menunjukkan bahawa peningkatan kadar aliran masuk atau aliran berpusing meningkatkan kelengahan. Dari segi kesan parameter geometri kepada kelengahan, lebar masuk dan lebar jalan berpusing menunjukkan korelasi negatif yang kuat dengan kelengahan (nilai $p < 0.05$). Dalam kata lain, peningkatan lebar masuk dan jalan berpusing membawa kepada pengurangan kelengahan. Sebaliknya, diameter pulau tengah tidak mempunyai kesan signifikan terhadap kelengahan (nilai $p > 0.05$); dengan demikian, parameter ini telah dibuang daripada model akhir. Dengan R^2 0.79, model yang diterbitkan adalah signifikan secara statistik pada 95% aras keyakinan, yang membawa maksud bahawa aliran lalulintas dan parameter geometri membawa kepada anggaran 79% perubahan di dalam kelengahan. Lebih lagi, nilai pekali korelasi berganda ($R = 0.89$) memperakui bahawa hubungan antara kelengahan dan kesan gabungan dari pembolehubah tak bersandar adalah kuat secara signifikan. Oleh itu, kajian ini akan memberi panduan lebih tepat untuk menentukan tahap perkhidmatan yang boleh diterima bagi bulatan Malaysia untuk mewajarkan perbelanjaan yang berkaitan. Adalah disarankan agar model yang dicadangkan dipertimbangkan di dalam garis panduan Malaysia untuk analisa prestasi persimpangan sama aras, khususnya bulatan.

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LIST OF ABBREVIATIONS

HCM	-	Highway Capacity Manual
MHCM	-	Malaysian Highway Capacity Manual
MOE	-	Measure of Effectiveness
PDF	-	Probability Distribution Function
US	-	United States
UK	-	United Kingdom
GEH	-	Geoffery E.Havers
AD	-	Advantages
LIM	-	Limitations
M/G/1	-	Markovian (random) arrivals/generally distributed service times/one
m	-	Meter
sec	-	Second
min	-	minute
hr	-	Hour
veh/hr	-	Vehicles per hour
sec/veh	-	Seconds per vehicles
pcu/hr	-	Passenger car unit per hour
sec/pcu	-	Seconds per passenger car unit
m/sec	-	Meter per second

LIST OF SYMBOLS

$Fr(t)$	-	Probability function of rejected gap
$Fa(t)$	-	Probability function of accepted gap
$Fc(t)$	-	Probability function of critical gap
t_f	-	Follow-up headway
t_c	-	Critical gap
Q_e	-	Entry traffic flow
Q_c	-	Circulating traffic flow
d	-	delay
$CI_{1-\alpha\%}$	-	Confidence interval for the true mean
S	-	Standard deviation
M	-	Model hourly traffic flow
O	-	Observed hourly traffic flow
a_x	-	Desired distance between two consecutive vehicles in queue
b_{xAdd}	-	A parameter used to determine the desired safety
b_{xmult}	-	A parameter used to determine the desired safety
D_i	-	Roundabout central diameter
D_s	-	Roundabout inscribed diameter
W_e	-	Entry width
W_c	-	Circulating roadway width
N	-	Number of repetitions
v	-	Approach width
l	-	Effective flare length
s	-	Sharpness width
$F(a_i)$	-	Cumulative distribution function for normal distribution for accepted gap
$F(r_i)$	-	Cumulative distribution function for normal distribution for rejected gap
$P_{tc}(t_j)$	-	Frequencies of estimated critical gaps
t_{dj}	-	Class mean of two consecutive time gaps

Q	-	Roundabout capacity
e	-	Average width of the approach
W	-	Width of weaving section
p	-	Proportion of weaving traffic
C	-	Entry capacity
Q_{exit}	-	Exiting traffic volume
x	-	Degree of saturation
d_m	-	Minimum delay
D_s	-	Stopped delay
V_s	-	Subject approach volume
V_c	-	Circulating volume
T_t	-	Travel time
d_{st}	-	Stopped line delay
s_p	-	Speed
V_e	-	Entry volume
Q_l	-	Queue length
HV	-	Heavy vehicle

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CHAPTER 1

INTRODUCTION

1.1 Background of the study

In recent years, roundabouts are becoming very attractive to be used as an un-signalized intersection type (Oketch *et al.*, 2004; Al-madani, 2016; Hossain and Hossain, 2016; Patel and Khode, 2016; Anagnostopoulos and Kehagia, 2019). A roundabout is defined as the type of un-signalized intersection with a circular shape, characterized by the yield on entry and circulation around a central island (TRB, 2010). One of the most significant advantages of the roundabout is reducing the conflict points at an intersection; which leads to a capacity improvement as well as intersection safety (Agyeman *et al.*, 2015; Zubaidi *et al.*, 2020; Mądział *et al.*, 2021). In addition, the total delay is also reduced (Oketch *et al.*, 2004; Sofia *et al.*, 2012; Almukdad *et al.*, 2021; Osei *et al.*, 2021).

Drivers at roundabouts entry are only required to yield for circulating vehicles in the circulating roadway. Consequently, drivers experience less delay at roundabout compared to other types of at-grade intersections; as a result of this, the fuel consumption is reduced, which in turn leads to fewer emissions at the roundabout (Lakouari *et al.*, 2020). A substantial number of studies emphasize that fewer emissions are produced at roundabouts than other types of intersections (Gastaldi *et al.*, 2014; Puan *et al.*, 2014; Chen and Lee, 2016; Lakouari *et al.*, 2020; Ahmed and Easa, 2021; Mądział *et al.*, 2021); thus, a roundabout is considered as an environmentally friendly facility.

For the purpose of designing a new intersection or improvement of an existing one, the operational performance with respect to traffic is a critical element. Capacity and delay are the most important performance measures for intersections. Delay is commonly known as the excess time spent on a transportation facility compared to that

of a reference value. In other words, is the difference between actual travel time experienced by the driver and the ideal travel time at the free-flow condition. From the road users' point of view, one of the essential evaluations of the performance of an intersection is the delay; consequently, it should be precisely taken into consideration to assess an intersection's operational performance.

Several methods for estimating delays at uncontrolled intersections are well documented in the literature (Tanner, 1962; Akcelik and Troutbeck, 1991; Flannery *et al.*, 2000; TRB, 2010; Tanyel *et al.*, 2013; Ali Sahraei *et al.*, 2018; Sahraei and Akbari, 2020b; Ma *et al.*, 2021; Sahraei *et al.*, 2021). These estimation methods are either based on the empirical or analytical approach. The empirical method depends on field observation at varying sites, in which generated data are processed using regression analysis to develop an empirical model to estimating delay. On the other hand, the analytical theory is based on either queuing theory or gap acceptance theory; which considerably depends on the drivers' behaviour. These two (2) approaches were used to develop a delay equation in most countries, depending on the local conditions.

Microsimulation models have been widely used in transportation planning, design, and analysis. There are significant benefits gained from the application of the microsimulation models; such as cost-effectiveness, safety, and fast production of the results (Ciuffo *et al.*, 2008; Yu and Fan, 2017). Microsimulation models such as VISSIM can be used to model roundabout performance precisely. Roundabout simulation differs from other types of intersections, since at the roundabout entry leg, vehicle has to yield and check if there are vehicles at the circulating roadway. In the absence of vehicles, the driver can proceed to enter the circulating roadway without the need for a complete stop. In VISSIM, this process is controlled by parameters of gaps and headways on a link by link basis (Trueblood and Dale, 2003). Many researchers employed VISSIM to model roundabout performance due to its magnificent capability to express the actual traffic conditions, especially at roundabouts (Gallelli and Vaiana, 2008; Vaiana *et al.*, 2012; Wei *et al.*, 2012; Otković, *et al.*, 2013; Mitrovic *et al.*, 2018).

As stated earlier, one of the significant advantages of the roundabout is reducing delay; nevertheless, due to high traffic volume during the rush hours, delays still occur. The roundabout delay is a critical performance measure for evaluating traffic conditions at a roundabout. This study focuses on delay at the entry leg of a roundabout. To present, limited work has been done on the topic, leading to an inaccurate assessment of the impact of the geometric and traffic parameters of roundabouts. Therefore, more studies are needed to examine the effects of geometry and traffic parameters on roundabout delays under the influence of driver behaviour in the field.

Collecting data from roundabouts with various geometric characteristics under different traffic flow conditions is a challenging process. It is required a lot of resources in terms of time and money, besides finding roundabouts under saturation conditions is challenging to find. Thus, the current study attempts to develop a base simulation model in VISSIM. Thereafter, the developed base model was calibrated and validated using field data from a representative roundabout to account for Malaysia's typical drivers' behaviour. Subsequently, different scenarios were generated in VISSIM based on varying ranges of geometric parameters and traffic flow conditions. Finally, the outputs from the VISSIM were used to formulate a relationship among roundabout delay, traffic flow, and roundabout geometric parameters.

1.2 Problem statement

Many researches have been carried out with regard to roundabout capacity (Benhadou, 2020; Almkdad *et al.*, 2021; Hamim *et al.*, 2021); whilst, studies to roundabout delay is yet to receive the most desired attention (Al-Omari *et al.*, 2004; Hossain and Hossain, 2016). Most of the studies carried out on delay estimation at roundabout were based on gap acceptance concept, from which delay prediction models are derived. This technique is theoretically grounded on knowledge of driver and vehicle behaviour. Although this method may extrapolate results to a broad range of cases, its theoretical assumptions (the gap is considered as headway, vehicles arrive stochastically, drivers on the circulating lane have homogeneous behaviour, and

drivers on the entry lane recognize the vehicles going to leave the roundabout) limited its validity to express real-field conditions. Besides driver and vehicle behaviour, geometric features could impact the roundabout delay. However, the gap acceptance-based approach does not consider the impact of the roundabout geometric features in the delay estimation process. Specifically, the geometric parameters are missing from the delay models based on the approach. The use of an empirical approach allows for more insights into driver-traffic behavior in the field as it comprises of driver behaviour influencing factors, which may not be expressed in the theoretical model. Yet, this approach heavily depends on the data used in formulating the model. Therefore, the applications of the derived model could be restricted to the data ranges used in developing the model. Besides, collecting data from different roundabouts with varying geometric features consumes time and financial resources. On the other hand, microsimulation models are similar to theoretical models in terms of assumptions about driver behaviour. However, this method provides more flexibility to account for particular driver behaviour and presents more pragmatic models. However, the microsimulation models such as VISSIM demands sophisticated user knowledge and expertise, which not all engineers possess. Additionally, most research conducted to construct roundabout delay models did not consider the effect of a sufficiently wide range of geometric and traffic features in these models. Furthermore, most of these studies have been accomplished in nations where the driver behaviour, geometry, and traffic characteristics of roundabouts differ from those in Malaysia.

In Malaysia, although in the Arahan Teknik (Jalan) 11/87, a capacity model for roundabout was developed. This model was developed based on weaving theory; which is mainly based on weaving section geometric parameters without considering the impact of the traffic flow parameters (Ministry of Works Malaysia, 1987; Aziz *et al.*, 2004). On the other hand, the procedure followed to estimate roundabout delay is based on the delay model for un-signalized intersections or other roundabout delay models developed in other countries (Puan *et al.*, 2015; Ghani *et al.*, 2019). The delay model used for un-signalized intersection did not consider the influence of the geometric parameters in the estimation process. Simultaneously, using roundabout delay models developed in other countries where intersection geometric features, traffic conditions, rules, and driver behaviour differ significantly from Malaysia would result in inaccurate assessment for design, analysis, and planning roundabouts.

Accordingly, further investigation is required to evaluate the impact of various ranges of geometric and traffic parameters on delays. Using the VISSIM microsimulation model based on actual driver behaviour appears a promising solution to assess the influence of wide ranges of different roundabout's geometric features on delays instead of collecting the data from the field. Finding roundabouts with diverse geometric characteristics with varying traffic flow conditions is challenging and consume time and money. Consequently, the current study attempts to develop a user-friendly and straightforward model for roundabout's delay based on the outputs obtained from VISSIM for different scenarios cases based on Malaysian roadway and traffic conditions and motorists' behaviour. Moreover, simple application graphs could be created based on the mathematical model to estimate delay for roundabouts under different geometric and traffic flow parameters.

1.3 Aim and objectives

This research aims to evaluate the impact of traffic flow and roundabout's geometric features on delays at the subject facility using a VISSIM microsimulation model software. To accomplish this, the following specific objectives are set.

- i. To develop a base model of traffic operations at roundabout using VISSIM microsimulation model;
- ii. To evaluate the impact of roundabout's geometric features (i.e. central island diameter, entry width, and circulating roadway width) on delays at a roundabout;
- iii. To develop a mathematical model for prediction of delay at roundabout as influenced by traffic flow and roundabout's geometric features; and
- iv. To develop application charts for computing delay at roundabouts with varying ranges of traffic flow and geometric parameters.

1.4 Scope and limitation of the study

Essentially, this study's scope consists of field data collection and evaluation and roundabout simulation model development in VISSIM. In terms of data collection and evaluation, the selected site in this study is a two-lane roundabout with a central island diameter of 67 m located in Johor Bahru States, Malaysia. Modelling driver behaviour at a roundabout is a complex process. Because the possibility of vehicular conflicts circulating traffic at the roundabout is high; however, this is also the case in real-life, not only for the simulation model (Trueblood and Dale, 2003). Therefore, modelling this type of behaviour can easily be accommodated in VISSIM microsimulation model with incorporation of further scenarios in the model. The study site was selected such that it is characterized by various traffic flow conditions such that vehicular queues are at times developed at least one or two entry leg(s) of the roundabout. The data was collected during morning peak hours on working weekdays because the traffic volumes at the weekends are low; therefore, finding delayed vehicles is more diminutive. On the other hand, collecting data in the evening peak is complex because the traffic flow stream's visibility is challenging to estimate. Data evaluation involved analyzing all data related to this study, such as estimating the critical gap, follow-up headway, traffic flow parameters, traffic composition, vehicle desired speed, and delays. The evaluated delay in this study is the total delay experienced by drivers at roundabout's entry, it is composed of queuing and service time delays. Moreover, pedestrians and cyclists are not examined in this research due to the scope of the study since their presence was infrequent within the study site proximity. Furthermore, the effects of the upstream signal and the slope on roundabout delays are not considered.

In terms of roundabout simulation model development in VISSIM, data evaluated earlier were used as input parameters in VISSIM. Traffic flow parameters and delays were selected as measures of effectiveness to calibrate and validate the simulation model by comparing the simulation model outputs with those from the actual field. Several scenarios were then created in VISSIM based on varying geometric parameters (i.e. central island diameter, entry width, and circulating width) and traffic flow conditions. The outputs from VISSIM were used to develop a

mathematical model describing the relationship between delays at roundabout, and entry flow rate, circulating flow rate, entry width and circulating roadway width. The mathematical model was then validated using the field's observed data from a different site. Different application graphs were generated based on varying ranges of geometric and traffic flow parameters. This research has some limitations because it is based on the evaluation of VISSIM microsimulation modelling. Moreover, the applicability of the developed model is restricted to delay estimation at urban roundabouts with a low proportion of heavy vehicles.

1.5 Significance of the study

This study investigates and developed a model for estimating delay at an urban roundabout. Since the models developed are based on data collected with varying ranges of traffic flow conditions, geometric parameters as well as under local driver behaviour in Malaysia, it is anticipated that the new method would be valuable in contributing to the Malaysian practice relating to the roundabout operational performance assessment. Because, the newly proposed model in this study is first of its kind meant for delay estimation at urban roundabout, which was developed on Malaysian local condition.

This study's outcomes would serve as a basis to prove the effectiveness of the method's suitability in terms of applicability for estimating delay. Moreover, the developed model would serve as a guide to decision makers regarding urban roundabout's operational performance assessment, particularly to justify expenses relating to the improvement of the subject facility.

1.6 Thesis structure

This thesis is structured into seven (7) chapters, with one of them discussing a particular aspect of the entire research. Chapter one describes the study's background,

problem statement, aim and research objectives, scope of the study, and the significance of the research.

Chapter two contains a comprehensive review and discussions of the existing researches in the literature relating to the roundabout operational performance, estimation of the critical gap, follow-up headway, and estimation methods of roundabout capacity and delays. Besides this, the chapter introduces the current issue regarding the methods applied in estimating the roundabout delay, highlighting both their strengths and weaknesses.

Chapter three describes the research methodology employed in conducting the study, which includes the detailed descriptions of procedures adopted for the various components of the work. This chapter covers two (2) main sections, data collection and data analysis. For the data collection, all data required for this research were described and generated using standard techniques. Likewise, the procedures followed for measuring the relevant input parameters were also described in this chapter. These include estimations of critical gap, follow-up headway, vehicle desired speed, delay, and development of a roundabout model in VISSIM.

Chapter four describes the approach used in analysing the data collected at a two-lane roundabout. Data analysis carried out includes traffic composition at the roundabout, estimation of the critical gap, follow-up headway, vehicle-desired speed, and delay evaluation. The data analyzed in this section are used to build the simulation model in the VISSIM software.

Chapter five presents the detailed description of the procedures followed to build the simulation model in the VISSIM software. It also describes the steps are followed to verify, calibrate, and validate the simulation model.

Chapter six present and discusses all the steps followed to create different scenarios in VISSIM. It also exhibits the influence of roundabout geometric features on delays at the facility. Furthermore, it presents the mathematical model's development process used for the estimation of delay based on roundabout geometric

features and traffic flow parameters. The model was derived from the outputs of the analysis performed in the VISSIM. Moreover, the chapter presents the validation of the developed model using data obtained from a different roundabout site. Subsequently, application graphs were generated to estimate roundabout delays based on varying ranges of geometric features and traffic flow conditions.

Chapter seven presents the summary of the conclusions drawn from the current research and suggestions made for further works in the future.

REFERENCES

- Abdulhai, B., Sheu, J. and Recker, W. (1999) Simulation of ITS on the Irvine FOT Area Using 'Paramics 1.5' Scalable Microscopic Traffic Simulator: Phase I: Model Calibration and Validation, Report UCB-ITS-PRR-99-12.
- Agyeman, S., Abeka, H. and Asiedu Boamah, S. (2015) 'Capacity and Performance Analysis of 3 Roundabouts in Sunyani', *International Journal of Science and Research (IJSR)*, 4(10), pp. 2019–2030.
- Ahmad, A., Rastogi, R. and Chandra, S. (2015) 'Estimation of critical gap on a roundabout by minimizing the sum of absolute difference in accepted gap data', *Canadian Journal of Civil Engineering*, 42(12), pp. 1011–1018.
- Ahmed, H. and Easa, S. M. (2021) 'Multi-objective evaluation model of single-lane roundabouts', *Transportation Research Record*, 2675(10), pp. 395–410.
- Aimsun (2014) 'Aimsun 8 Users' Manual', TSS-Transport Simulation Systems, (July).
- Akçelik, R. (2003) 'A roundabout case study comparing capacity estimates from alternative analytical models', 2nd Urban Street Symposium, Anaheim, (July 2003), pp. 28–30.
- Akcelik, R., Chung, E. and Besley, M. (1997) 'Analysis of roundabout performance by modelling approach flow interactions', *Proceedings of the Third International Symposium on Intersections Without Traffic Signals*, Portland, Oregon, USA, (July), pp. 15–25.
- Akcelik, R. and Troutbeck, R. (1991) 'Implementation of the Australian roundabout analysis method in SIDRA', in *The International Symposium on Highway Capacity*, Karlsruhe, Germany, 24-27 July 1991.
- Al-madani, H. (2016) 'A model to predict capacity of multi-lane roundabouts under high demand flows in Bahrain', *International Journal of Sustainable Development and Planning*, 6 (1)(March), pp. 21–33.
- Al-Masaeid, H. (1995) 'Capacity of One-Way Yield-Controlled Intersections', *Transportation Research Record*, 1484, pp. 9–15.
- Al-Masaeid, H. and Faddah, M. (1997) 'Capacity of roundabouts in Jordan', *Transportation Research Record*, 1572(1), pp. 76–85.

- Al-Masaeid, H. R. (1999) 'Capacity and performance of roundabouts', *Canadian Journal of Civil Engineering*, 26(5), pp. 597–605.
- Al-Obaedi, J. (2019) 'Simulating the Effect of Speed Humps on the U-Turn Traffic', *International Journal of Engineering*, 32(12), pp. 1773–1780.
- Al-Omari, B. and Benekohal, R. F. (1999) 'Hybrid delay models for unsaturated two-way stop controlled intersections', *Journal of Transportation Engineering*, 125(4), pp. 291–296.
- Al-Omari, B. H., Al-Masaeid, H. R. and Al-Shawabkah, Y. S. (2004) 'Development of a delay model for roundabouts in Jordan', *Journal of Transportation Engineering, ASCE*, 130(February), pp. 76–82.
- Alemdar, K. D., Kaya, Ö. and Çodur, M. Y. (2020) 'A GIS and microsimulation-based MCDA approach for evaluation of pedestrian crossings', *Accident Analysis and Prevention*, 148(February).
- Ali Sahraei, M., Che Puan, O., Hosseini, S. M. P. and Almasi, M. H. (2018) 'Establishing a new model for estimation of the control delay at priority junctions in Malaysia', *Cogent Engineering*. Cogent, 5(1), pp. 1–12.
- Alkheder, S., Al-rukaibi, F. and Al-faresi, A. (2020) 'Driver behavior at Kuwait roundabouts and its performance evaluation', *IATSS Research. International Association of Traffic and Safety Sciences*, 44(4), pp. 272–284.
- Almukdad, A., Almallah, M., Hussain, Q., Alhajyaseen, W. K. M., Albeitjali, N. and Alqaradawy, M. (2021) 'Analysis of gap parameters for the estimation of single lane roundabouts' capacity in the State of Qatar', *Procedia Computer Science. Elsevier B.V.*, 184, pp. 250–257.
- Ambadipudi, R. (2009) 'Modeling high-capacity multilane roundabouts', in *Proceedings of 88th TRB Annual Meeting*. Washington, D.C., USA.
- Amin, H. J. and Maurya, A. K. (2015) 'A review of critical gap estimation approaches at uncontrolled intersection in case of heterogeneous traffic conditions', *Journal of Transport Literature*, 9(3), pp. 5–9.
- Anagnostopoulos, A. and Kehagia, F. (2019) 'Turbo-Roundabouts as an Alternative to Roundabouts in terms of Traffic Safety, Capacity and Pollutant Emissions', in the *7th Pan-hellenic Road Safety Conference*, Larissa, Greece.
- Arafat, M., Nafis, S. R., Sadeghvaziri, E. and Tousif, F. (2020) 'A data-driven approach to calibrate microsimulation models based on the degree of saturation

- at signalized intersections’, *Transportation Research Interdisciplinary Perspectives*, 8.
- Arkkelin, D. (2014) *Using SPSS to understand research and data analysis*. Valparaiso University.
- Ashton, W. D. (1971) ‘Gap-acceptance Problems at a Traffic Intersection’, *Journal of the Royal Statistical Society. Series C (Applied Statistics)*, 20(2), pp. 130–138.
- Ashworth R (1970) ‘Analysis and Interpretation of Gap Acceptance Data’, *Transportation Science*, 4(3), pp. 270–280.
- Azam, M., Puan, O. C., Hassan, S. A. and Mashros, N. (2019) ‘Calibration of microsimulation model for tight urban diamond interchange under heterogeneous traffic’, *IOP Conference Series: Materials Science and Engineering*, 527, p. 012077.
- Aziz, A. C., Puan, C. O. and Jing, M. C. (2004) ‘Entry and circulating flow relationship at a roundabout’, *Jurnal Kejuruteraan Awam*, 16(1), pp. 48–60.
- Bains, M. S., Ponnu, B. and Arkatkar, S. S. (2012) ‘Modeling of Traffic Flow on Indian Expressways using Simulation Technique’, *Procedia - Social and Behavioral Sciences*, 43, pp. 475–493.
- Bargegol, I., Najafi, V., Gilani, M., Ghasedi, M. and Ghorbanzadeh, M. (2016) ‘Delay Modeling of Un-signalized Roundabouts Using Neural Network and Regression’, *Computational Research Progress in Applied Science & Engineering*, 2(1), pp. 28–34.
- Barry, C. D. (2012) *Calibration Of The Hcm 2010 Roundabout Capacity Equations For Georgia Conditions*. Master Thesis, Georgia Institute of Technology.
- Behbahani, H., Ziari, H., Amini, A., Najafi Moghaddam Gilani, V. and Salehfard, R. (2016) ‘Investigation of Un-signalized Roundabouts Delay with Adaptive-Network-Based Fuzzy Inference System and Fuzzy Logic’, *Computational Research Progress in Applied Science & Engineering* ©PEARL publication CRPASE, 02(04), pp. 140–149.
- Benhadou, M. (2020) ‘Roundabout Capacity Model Case Study Tangier City’, *International Journal of Innovative Science and Research Technology*, 5(12), pp. 1171–1177.
- Benlagha, N. and Charfeddine, L. (2020) ‘Risk Factors Of Road Accident Severity And The Development Of A New System For Prevention: New Insights From

- China', *Accident Analysis and Prevention*. Elsevier, 136(July 2019), p. 105411.
- Bessa, J. E. and Setti, J. R. (2011) 'Derivation of ATS and PTSF functions for two-lane, rural highways in Brazil', *Procedia-Social and Behavioral Sciences*. Elsevier, 16, pp. 282–292.
- Bloomberg, L. and Dale, J. (2000) 'Comparison of VISSIM and CORSIM Traffic Simulation Models on a Congested Network', *Journal of the Transportation Research Board*. TRB, National Research Council, Washington, D.C., 1727(00), pp. 52–60.
- Brilon, W. (2011) 'Studies on roundabouts in Germany: lessons learned', in 3rd International Conference on Roundabouts, pp. 1–15.
- Brilon, W., Koenig, R. and Troutbeck, R. (1999) 'Useful Estimation Procedures for Critical Gaps', *Third International Symposium on Intersection Without Traffic Signals*, 33, pp. 161–186.
- Brilon, W. and Stuwe, B. (1993) 'Capacity and design of traffic circles in Germany', *Transportation Research Record*, (1398), pp. 61–67.
- Caliendo, C. (2014) 'Delay Time Model at Unsignalized Intersections', *Journal of Transportation Engineering*. American Society of Civil Engineers, 142(2), pp. 548–556.
- Cameron, G. D. B. and Duncan, G. I. D. (1996) 'PARAMICS - Parallel Microscopic Simulation Of Road Traffic', *Journal of Supercomputing*, 10(1), pp. 25–53.
- Chandra, S., Agrawal, A. and Rajamma, A. (2009) 'Microscopic Analysis of Service Delay at Uncontrolled', 135(6), pp. 323–329.
- Chen, X. and Lee, M. S. (2016) 'A Case Study On Multi-Lane Roundabouts Under Congestion: Comparing Software Capacity And Delay Estimates With Field Data', *Journal of Traffic and Transportation Engineering (English Edition)*. Elsevier Ltd, 3(2), pp. 154–165.
- Cheng, J., Yang, X., Deng, W. and Huang, X. (2008) 'Driver's Critical Gap Calibration At Urban Roundabouts: A Case Study In China', *Tsinghua Science and Technology*, 13(2), pp. 237–242.
- Ciuffo, B., Punzo, V. and Torrieri, V. (2008) 'Comparison Of Simulation-Based And Model-Based Calibrations Of Traffic-Flow Microsimulation Models', *Transportation Research Record*, (2088), pp. 36–44.

- Cvitanić, D., Breški, D. and Vidak, B. (2007) 'Review, Testing And Validation Of Capacity And Delay Models At Unsignalized Intersections', *Promet - Traffic - Traffico*, 19(2), pp. 71–82.
- Dahl, J. and Lee, C. (2012) 'Empirical Estimation Of Capacity For Roundabouts Using Adjusted Gap-Acceptance Parameters For Trucks', *Transportation Research Record: Journal of the Transportation Research Board*, 2312(04), pp. 34–45.
- Dey, A. C. and Roy, S. (2018) 'Calibration and Validation of Vissim Model of an Intersection with Modified Driving Behavior Parameters', *international Journal od Advanced Research (IJAR)*, (6(12)), pp. 107–112.
- Diah, M. J., AbdulRahman, M. ., Adnan, M. . and Ling, Hooi, K. (2011) 'Modeling The Relationship Between Geometric Design And Weaving Section Flow Process Of Conventional Roundabouts', *Journal of Transportation Engineering*, 137(12), pp. 980–986.
- Dowling, R. (2007) *Definition, Interpretation, and Calaulation of Traffic Analysis Tools Measures of Effectiveness*, *Traffic Analysis Toolbox Volume VI*. Federal Highway Administration, Washington, DC.
- Dowling, R., Skabardonis, A. and Alexiadis, V. (2004) *Guidelines for applying traffic microsimulation modeling software*, *Traffic analysis toolbox, volume III*. Federal Highway Administration, Washington, DC.
- Durrani, U., Lee, C. and Maoh, H. (2016) 'Calibrating The Wiedemann's Vehicle-Following Model Using Mixed Vehicle-Pair Interactions.', *Transportation Research Part C: Emerging Technologies*. Elsevier Ltd, 67, pp. 227–242.
- Dutta, M. and Ahmed, M. A. (2018) 'Gap Acceptance Behavior Of Drivers At Uncontrolled T-Intersections Under Mixed Traffic Conditions', *Journal of Modern Transportation*. Springer Berlin Heidelberg, 26(2), pp. 119–132.
- Eboli, L., Forciniti, C. and Mazzulla, G. (2020) 'Factors Influencing Accident Severity: An Analysis By Road Accident Type', *Transportation Research Procedia*. Elsevier B.V., 47, pp. 449–456.
- Eisenman, S. M. and Mahmassani, H. S. (2004) 'A Mesoscopic Approach To the Simulation of Roundabouts', in the 84th Annual Meeting of the Transportation Research Board. Washington, D.C: Transportation Research Record.
- Essa, M. and Sayed, T. (2016) 'A comparison between PARAMICS and VISSIM in estimating automated field-measured traffic conflicts at signalized intersections', *Journal of Advanced Transportation*, 50(5), pp. 897–917.

- Eva, P. and Andrea, K. (2017) 'Case Study : Capacity Characteristics Comparison Of Single-Lane Roundabout And Turbo-Roundabouts', *Procedia Engineering*. Elsevier, 192(2017), pp. 701–706.
- Fang, C. F. and Castaneda, H. (2018) 'Computer Simulation Modeling of Driver Behavior at Roundabouts', *International Journal of Intelligent Transportation Systems Research*, 16(1), pp. 66–77.
- Ferrara, A., Sacone, S. and Siri, S. (2018) 'Microscopic and mesoscopic traffic models', in *Freeway traffic modelling and control*. Springer, pp. 113–143.
- Field, A. (2009) *Discovering Statistics Using SPSS, Thrid Edition*. sage publications.
- Fitzpatrick, K. A. Y. (1991) 'Gaps Accepted at Stop-Controlled Intersections', *Transportation Research Record*, 1303 (11), pp. 103–112.
- Flannery, A., Kharoufeh, J. P., Gautam, N. and Elefteriadou, L. (2000) 'Estimating Delay At Roundabouts', In *TRB Annual Conference Proceedings*, (703), pp. 1–23.
- Flannery, A., Kharoufeh, J. P., Gautam, N. and Elefteriadou, L. (2005) 'Queuing delay models for single-lane roundabouts', *Civil Engineering and Environmental Science*, 22(3), pp. 133–150.
- Florida Department of Transportation (2014) *Traffic Analysis Handbook*.
- Fortuijn, L. G. H. (2010) 'Turbo Roundabouts', *Transportation Research Record: Journal of the Transportation Research Board*, 2130(1), pp. 83–92.
- Gallelli, V., Iuele, T., Vaiana, R. and Vitale, A. (2017) 'Investigating the transferability of calibrated microsimulation parameters for operational performance analysis in roundabouts', *Journal of Advanced Transportation*, 2017.
- Gallelli, V. and Vaiana, R. (2008) 'Roundabout Intersections: Evaluation Of Geometric And Behavioural Features With Vissim', *TRB National Roundabout Conference*, pp. 1–19.
- Gastaldi, M., Meneguzzer, C., Rossi, R., Lucia, L. Della and Gecchele, G. (2014) 'Evaluation Of Air Pollution Impacts Of A Signal Control To Roundabout Conversion Using Microsimulation', *Transportation Research Procedia*, 3(April 2016), pp. 1031–1040.
- Gattis, J. L. and Low, S. T. (1999) 'Gap acceptance at atypical stop-controlled intersections', *Journal of Transportation Engineering*, 125 (3), pp. 201–207.

- Gazder, U., Alhalabi, K. and AlAzzawi, O. (2020) ‘Calibration of autonomous vehicles in PTV VISSIM’, IET Conference Publications, 2020(CP777), pp. 39–42.
- Gazzarri, A., Martello, M. T., Pratelli, A. and Souleyrette, R. R. (2013) ‘Gap Acceptance Parameters for HCM 2010 Roundabout Capacity Model Applications in Italy’, in *Intersections Control and Safety. Transportation Systems & Traffic Engineering*. WitPress, Southampton. Boston, pp. 309–320.
- Gerber, S. B. and Finn, K. V. (2013) *Using SPSS for Windows: Data analysis and graphics*. Springer.
- Ghani, A. R. A., Sanik, M. E., Hamid, N. B., Mokhtar, M., Johan, N. H. S., Razak, N. H. A. A., Neemat, S. A., Razali, N. F., Rahman, N. K. A. and Amin, H. M. (2019) ‘Performance analysis of roundabouts at Bandar Maharani Bandar Di Raja, Johor, Malaysia’, *International Journal of Innovative Technology and Exploring Engineering*, 8(8), pp. 300–303.
- Giuffrè, O., Grana, A., Marino, S. and Galatioto, F. (2016) ‘Passenger Car Equivalent for Heavy Vehicles Crossing Turbo-roundabouts’, *Transportation Research Procedia*. Elsevier, 14(2016), pp. 4190–4199.
- Giuffrè, O., Granà, A., Tumminello, M. L. and Sferlazza, A. (2017) ‘Estimation of Passenger Car Equivalents for single-lane roundabouts using a microsimulation-based procedure’, *Expert Systems with Applications*, 79, pp. 333–347.
- Giuffrè, O., Granà, A., Tumminello, M. L. and Sferlazza, A. (2018) ‘Capacity-Based Calculation Of Passenger Car Equivalents Using Traffic Simulation At Double-Lane Roundabouts’, *Simulation Modelling Practice and Theory*, 81, pp. 11–30.
- Guerrieri, M., Mauro, R., Parla, G. and Tollazzi, T. (2018) ‘Analysis of kinematic parameters and driver behavior at turbo roundabouts’, *Journal of Transportation Engineering Part A: Systems*, 144(6), pp. 1–12.
- Guerrieri, M., Mauro, R. and Tollazzi, T. (2019) ‘Turbo-Roundabout : Case Study Of Driver Behavior And Kinematic Parameters Of Light And Heavy Vehicles’, *Journal of Transportation Engineering Part A: Systems*, 145(6), pp. 1–11.
- Guo, R. J., Wang, X. J. and Wang, W. X. (2014) ‘Estimation of critical gap based on raff’s definition’, *Computational Intelligence and Neuroscience*, 2014.

- Guo, R., Liu, L. and Wang, W. (2019) Review of roundabout capacity based on gap acceptance, *Journal of Advanced Transportation*.
- Hagring, O., Roupail, N. M. and Sørensen, H. A. (2003) ‘Comparison Of Capacity Models For Two-Lane Roundabouts’, in *Transportation Research Record*, pp. 114–123.
- Hamed, M. M., Member, Easa, S. M. and Batayneh, R. R. (1997) ‘Disaggregate Gap-Acceptance Model For Unsignalized T-Intersections’, *Journal of transportation engineering*, 123(1), pp. 36–42.
- Hamim, O. F., Hossain, M. S. and Hadiuzzaman, M. (2021) ‘Developing empirical model with graphical tool to estimate and predict capacity of rural highway roundabouts’, *International Journal of Transportation Science and Technology*. Tongji University and Tongji University Press, (xxxx).
- Hammond, S. (2014) *The Effect of Additional Lane Length on Roundabout Delay*, Ph.D Thesis. University of Rhode Island.
- Hassan, S. A. (2013) *Improving Pedestrian At Signalised Crossing*. PhD Thesis. University Of Southampton.
- Hatami, H. and Aghayan, I. (2017) ‘Traffic efficiency evaluation of elliptical roundabout compared with modern and turbo roundabouts considering traffic signal control’, *Promet - Traffic - Traffico*, 29(1), pp. 1–11.
- Hazim, N., Bazlamit, S. M., Salem, Z. A., Alghazawi, O. and Odeh, I. (2019) ‘Determinations Of Critical Gap And Follow-Up Time At Roundabouts In Jordan’, *Roads and Bridges - Drogi i Mosty*, 18(3), pp. 227–234.
- Hidas, P. (2005) ‘A Functional Evaluation Of The AIMSUN, PARAMICS And VISSIM Microsimulation Models’, *Road & Transport Research*, 14(4), p. p.45.
- Highways Agency England (2007) *Geometric Design Of Roundabouts*, Design Manual For Roads And Bridges. Highways Agency, England- UK.
- Hossain, E. and Hossain, S. Q. (2016) ‘Development of a delay model for roundabouts in khulna metropolitan city, bangladesh’, in *Proceedings of the 3rd International Conference on Civil Engineering for Sustainable Development*, pp. 76–82.
- HPU (2011) *Highway planning unit, Malaysian highway capacity manual*. Ministry of Works Malaysia.
- Hussain, E. and Ali, M. S. (2017) ‘Calibration and Validation of VISSIM for signalized intersection of Karachi Calibration and Validation of

- microsimulation software for intersection of Karachi’, in 9th International Civil Engineering Congress (ICEC-2017). Karachi.
- Ibijola, S. and Ben-Edigbe, J. (2018) ‘Effects Of Rainfall On Driver Behaviour And Gap Acceptance At Multilane Roundabouts’, *The Open Transportation Journal*, 12(1), pp. 192–202.
- Islam, M. and Mannering, F. (2020) ‘A Temporal Analysis Of Driver-Injury Severities In Crashes Involving Aggressive And Non-Aggressive Driving’, *Analytic Methods in Accident Research*. Elsevier Ltd, 27, p. 100128.
- Kang, N. and Nakamura, H. (2016) ‘An Analysis Of Heavy Vehicle Impact On Roundabout Entry Capacity In Japan’, *Transportation Research Procedia*. Elsevier, 15, pp. 308–318.
- Kennedy, J. V (2008) ‘the Uk Standards for Roundabouts and Mini-Roundabouts’, National Roundabout Conference 2008.
- Khoda Bakhshi, A. and Ahmed, M. M. (2021) ‘Accounting for human-related unobserved heterogeneity in the safety performance of connected vehicles: An incorporation of Bayesian hierarchical negative binomial into simulated work zone warning application’, *IATSS Research*. International Association of Traffic and Safety Sciences, (xxxx).
- Kim, J. and Elefteriadou, L. (2010) ‘Estimation of capacity of two-lane two-way highways using simulation model’, *Journal of Transportation Engineering*. American Society of Civil Engineers, 136(1), pp. 61–66.
- Kimber, R. ., Daly, P., Barton, J. and Giokas, C. (1986) ‘Predicting Time-Dependent Distributions of Queues and Delays for Road Traffic at Roundabouts and Priority Junctions’, *Journal of the Operational Research Society*, 37(1), pp. 87–97.
- Kimber, R. M. (1980) *The Traffic Capacity Of Roundabouts*, (No. TRRL LR942 Monograph).
- Kimber, R. M. (1989) ‘Gap-Acceptance and Empiricism in Capacity Prediction’, *Transportation Science*, 23(2), pp. 100–111.
- Kimber, R. M. and Hollis, E. M. (1977) ‘Flow/delay relationships for major/minor priority junctions’, *Traffic engineering & control*, 18.
- Kwakwa, O. and Adams, C. (2016) ‘Assessment of turbo and multilane roundabout alternatives to improve capacity and delay at a single lane roundabout using

- microsimulation model Vissim : A case study in Ghana', *American Journal of Civil Engineering and Architecture*, 4(4), pp. 106–116.
- Kyte, B. Y. M. and Marek, J. (1989) 'Collecting Traffic Data At Intersections', *ITE Journal (Institute of Transportation Engineers)*, 33, pp. 33–36.
- Kyte, M., Clemow, C., Mahfood, N., Kent Lall, B. and Kristy, O. (1991) 'Capacity And Delay Characteristics Of Two-Way Stop-Controlled Intersections', *Transportation Research Record*, 1320, pp. 160–167.
- Lakouari, N., Oubram, O., Bassam, A., Hernandez, P. S. E., Marzoug, R. and Ez-Zahraouy, H. (2020) 'Modeling And Simulation Of CO2 Emissions In Roundabout Intersection', *Journal of Computational Science. Elsevier*, 40, p. 101072.
- Lee, C. (2015) 'Developing Passenger-Car Equivalents For Heavy Vehicles In Entry Flow At Roundabouts', *Journal of Transportation Engineering*, 141(8), pp. 1–7.
- Lee, D., Hwang, S., Ka, E. and Lee, and C. (2018) 'Evaluation of the Rain Effects on Gap Acceptance Behavior at Roundabouts by a Logit Model', *Journal of Advanced Transportation*, 2018, p. 11.
- Leemann, N., Santel, Gerko, Z. and Zurich (2009) 'Two-Lane Roundabouts', in 9th Swiss transport Research Conference- Monte Verita.
- Li, J. (2012) Two-lane highway simulation and analysis. University of Florida.
- Li, J. and Washburn, S. S. (2011) 'Implementing Two-lane Highway Simulation Modeling into CORSIM1', *Procedia-Social and Behavioral Sciences. Elsevier*, 16, pp. 293–305.
- Li, Z., DeAmico, M., Chitturi, M. V, Bill, A. R. and Noyce, D. A. (2013) 'Calibrating Vissim Roundabout Model Using A Critical Gap And Follow-Up Headway Approach', in 16th International Conference Road Safety on Four Continents. Beijing, China, pp. 1–15.
- Lu, W., Vandebona, U., Kiyota, M. and Wang, Y. (2020) 'Estimation of Traffic Delay at an Unconventional Roundabout by Computer Simulation', in *Proceedings of 2020 IEEE 3rd International Conference on Information Systems and Computer Aided Education, ICISCAE 2020*, pp. 295–302.
- Ma, Q., Zeng, H., Wang, Q. and ullah, S. (2021) 'Traffic Optimization Methods of Urban Multi-leg Intersections', *International Journal of Intelligent Transportation Systems Research*, 19(2), pp. 417–428.

- Macioszek, E. (2020) 'Roundabout entry capacity calculation-A case study based on roundabouts in Tokyo, Japan, and Tokyo surroundings', *Sustainability (Switzerland)*, 12(4).
- Macioszek, E. and Sierpiński, G. (2018) 'The Comparison Of Models For Follow-Up Headway At Roundabouts', in *Scientific And Technical Conference Transport Systems Theory And Practice*. Springer, pp. 16–26.
- Madanat, S. M., Cassidy, M. J. and Wang, M. (1994) 'Probabilistic delay model at stop-controlled intersection', *Journal of Transportation Engineering*, 120(1), pp. 21–36.
- Mądział, M., Campisi, T., Jaworski, A., Kuszewski, H. and Woś, P. (2021) 'Assessing vehicle emissions from a multi-lane to turbo roundabout conversion using a microsimulation tool', *Energies*, 14(15), pp. 1–21.
- Mahmassani, H. and Sheffi, Y. (1981) 'Using Gap Sequences To Estimate Gap Acceptance Functions', *Transportation Research Part B*, 15(3), pp. 143–148.
- Manjunatha, P., Vortisch, P. and Mathew, T. V (2013) 'Methodology For The Calibration Of VISSIM In Mixed Traffic', in *Transportation research board 92nd annual meeting (Vol. 11)*. Washington, DC, United States.
- Maryland State Administration (1995) *Roundabout Design Guidelines*. State Highway Administration.
- Mason, O. H. N. M., Fitzpatrick, K. A. Y. and DOUGLAS, W. H. (1990) 'Field Observations of Truck Operational Characteristics Related to Intersection Sight Distance', *Transportation Research Record*, 1280, pp. 163–172.
- Mathew, S., Dhamaniya, A., Arkatkar, S. S. and Joshi, G. (2017) 'Roundabout Capacity In Heterogeneous Traffic Condition: Modification Of HCM Equation And Calibration', *Transportation Research Procedia*. Elsevier, 27(2017), pp. 985–992.
- Ministry of Works Malaysia (1987) *Arahan Teknik (Jalan) 11/87–A Guide to the Design of at-Grade Intersections*, Cawangan Jalan, Ibu Pejabat JKR.
- Mitrovic, N., Dakic, I. and Stevanovic, A. (2018) 'Using Analytical Models To Calibrate A Dual-Roundabout Intersection In Microsimulation', *Put i saobraćaj*, 64(2), pp. 13–19.
- Mohan, M. and Chandra, S. (2016) 'Review And Assessment Of Techniques For Estimating Critical Gap At Two-Way Stop-Controlled Intersections', *European Transport-trasporti Europei*, 16(August), pp. 1–18.

- Musa, M. F., Hassan, S. A. and Mashros, N. (2020) 'The impact of roadway conditions towards accident severity on federal roads in Malaysia', *PLoS ONE*, 15(7 July), pp. 1–12.
- Mwesige, G. and Tindiwensi, D. (2011) 'Estimating The Critical Gap And Follow-Up Headway At Roundabouts In Uganda', *Second International Conference on Advances in Engineering and Technology*, (January 2011), pp. 471–477.
- Negi, V., Gaddam, H. K. and Rao, K. R. (2021) 'Driver Gap Acceptance Characteristics at Roundabouts and Meta-analysis of Recent Studies in India', *Transportation in Developing Economies*. Springer International Publishing, 7(1), pp. 1–13.
- Nikolic, G., Pringle, R. and Bragg, K. (2010) 'Evaluation Of Analytical Tools Used For The Operational Analysis Of Roundabouts', in *Proceedings of the Annual Conference of the Transportation Association of Canada*.
- Oketch, T., Delsey, M. and Robertson, D. (2004) 'Evaluation Of Performance Of Modern Roundabouts Using PARAMICS Microsimulation Model', in *Transportation Association of Canada (TAC) Annual Conference and Exhibition, 2004, Quebec, Ontario, Canada*, pp. 1–13.
- Oregon Department of Transportation (2011) *Protocol For Vissim Simulation Oregon Department Of Transportation*.
- Osei, K. K., Adams, C. A., Ackaah, W. and Oliver-Commey, Y. (2021) 'Signalization options to improve capacity and delay at roundabouts through microsimulation approach: A case study on arterial roadways in Ghana', *Journal of Traffic and Transportation Engineering (English Edition)*. Elsevier Ltd, 8(1), pp. 70–82.
- Otković, I. I., Tollazzi, T. and Šraml, M. (2013) 'Calibration Of Microsimulation Traffic Model Using Neural Network Approach', *Expert Systems with Applications*, 40(15), pp. 5965–5974.
- Pajecki, R., Ahmed, F., Qu, X., Zheng, X., Yang, Y. and Easa, S. (2019) 'Estimating Passenger Car Equivalent of Heavy Vehicles at Roundabout Entry Using Micro-Traffic Simulation', *Frontiers in Built Environment*, 5.
- Patel, C. and Khode, B. . (2016) 'Capacity Estimation Approaches for Roundabouts : A Review', *International Journal of Science Technology & Engineering*, 2(08), pp. 305–310.

- Peterson, R. W., Lewis, S. J., Fugal, K. J. and Lancaster, R. D. (2008) 'Modeling Roundabouts: Lessons Learned in Idaho', in National Roundabout Conference, Transportation Research Board. Washington, D.C., USA.
- Pollatschek, M. A., Polus, A. and Livneh, M. (2002) 'A Decision Model For Gap Acceptance And Capacity At Intersections', *Transportation Research Part B: Methodological*, 36, pp. 649–663.
- Polus, A., Lazar, S. and Livneh, M. (2003) 'Critical Gap As A Function Of Waiting Time In Determining Roundabout Capacity', *Journal of Transportation Engineering, ASCE*, 129(5), pp. 504–509.
- Polus, A. and Shmueli, S. (1997) 'Analysis And Evaluation Of The Capacity Of Roundabouts', *Transportation Research Record*, 1572(1), pp. 99–104.
- Pompigna, A., Guerrieri, M. and Mauro, R. (2020) 'New extensions and applications of the modified chumanov model for calculating entry capacity of single-lane roundabouts', *Sustainability (Switzerland)*, 12(15).
- PTV (2013) 'PTV VISSIM 6 User Manual', Karlsruhe, Germany.
- Puan, O. C., Ismail, C. R., Hainin, M. R., Minhans, A. and Nor, N. S. M. (2015) 'Midblock U–turn facilities on multilane divided highways: An assessment of driver's merging gap and stop delays', *Jurnal Teknologi*, 76(14), pp. 1–8.
- Puan, O. C., Muhamad, N. S. and Sien, P. T. (2015) 'Assessment Of Delays At Roundabout', *Jurnal Teknologi*, 76(14), pp. 67–76.
- Puan, O. C., Nabay, M. M. and Ibrahim, M. N. (2014) 'Effect of vehicular traffic volume and composition on carbon emission', *Jurnal Teknologi*, 70(4), pp. 17–20.
- Qu, X., Ren, L., Wang, S. and Oh, E. (2014) 'Estimation Of Entry Capacity For Single-Lane Modern Roundabouts: Case Study In Queensland, Australia', *Journal of Transportation Engineering*, 140(7).
- Raff, M. S. and Hart, J. W. (1950) 'A volume warrant for urban stop signs', Eno foundation for highway traffic control: Saugatuck, Connecticut.
- Rakha, H., Hellinga, B., Aerde, M. Van and Perez, W. (1996) 'Systematic Verification , Validation and Calibration of Traffic Simulation Models', in 75th Annual Meeting of the Transportation Research Board, Washington, DC. Washington, DC.

- Rao, A. M. and Rao, K. R. (2015) 'Microscopic simulation to evaluate the traffic congestion mitigation strategies on urban arterials', EUROPEAN TRANSPORT-TRASPORTI EUROPEI, (58).
- Rao, L., Owen, L. and Goldsman, D. (1998) 'Development and Application of a Validation Framework for Traffic Simulation Models', in 1998 Winter Simulation Conference. Proceedings (Cat. No. 98CH36274) IEEE, pp. 1079–1086.
- Robinson, B. and Rodegerts, L. (2000) 'Capacity And Performance Of Roundabouts: A Summary Of Recommendations In The FHWA Roundabout Guide', in Proceedings of 4th International Symposium on Highway Capacity, pp. 422–433.
- Robinson, B. W., Rodegerdts, L., Scarborough, W. and Kittelson, W. (2000) Roundabouts: An Informational Guide, (FHWA-RD-00-067; Project 2425). Federal Highway Administration United States.
- Rodegerdts, L. A. (2010) Roundabouts: An informational guide. Transportation Research Board.
- Roess, R. P., Prassas, E. S. and McShane, W. R. (1998) Traffic engineering. third edit, Australian Surveyor. third edit. Pearson/Prentice Ha.
- Rrecaj, A. A. and Bombol, K. M. (2015) 'Calibration and Validation of the VISSIM Parameters - State of the Art', Tem Journal-Technology Education Management Informatics, 4(3), pp. 255–269.
- S-Paramics (2009) Paramics Microsimulation. Edinburgh/UK.
- Sahraei, M. A. (2018) Modelling of traffic control delays at priority junctions using artificial neural network. PhD Thesis. Universiti Teknologi Malaysia.
- Sahraei, M. A. and Akbari, E. (2019) 'Implementing the equilibrium of probabilities to measure critical gap at priority junctions', Journal of Testing and Evaluation, 47(2), pp. 1062–1074.
- Sahraei, M. A. and Akbari, E. (2020a) 'Effect of motorcycle on the critical gap at priority junctions', Australian Journal of Civil Engineering. Taylor & Francis, 18(2), pp. 140–152.
- Sahraei, M. A. and Akbari, E. (2020b) 'Review and evaluation of methods for estimating delay at priority junctions', Australian Journal of Civil Engineering. Taylor & Francis, 18(2), pp. 126–139.

- Sahraei, M. A., Kuşkan, E. and Çodur, M. Y. (2021) 'Application of Dimensionless Method to Estimate Traffic Delays at Stop-Controlled T-Intersections', in *transformation of Transportation*, pp. 31–48.
- Sahraei, M. A., Puan, O. C. and Al-Muz-Zammil Yasin, M. (2014) 'Minor road traffic delays at priority junctions on low speed roads in suburban areas', *Jurnal Teknologi*, 70(4), pp. 97–102.
- Saidallah, M., El Fergougui, A. and Elalaoui, A. E. (2016) 'A Comparative Study Of Urban Road Traffic Simulators', in *MATEC Web of Conferences*.
- Saplioglu, M. and Karasahin, M. (2013) 'Predicting Critical Gap Using Fuzzy Logic Method At Unsignalised Urban Intersections', in *AWERProcedia Information Technology & Computer Science*, pp. 1556–1564.
- Schroeder, B.J., Cunningham, C.M., Findley, D.J., Hummer, J.E. and Foyle, R.S. (2010) *ITE Manual Of Transportation Engineering Studies*. (2nd ed). Institute of Transportation Engineers.
- Shaaban, K. and Hamad, H. (2018) 'Group Gap Acceptance: A New Method to Analyze Driver Behavior and Estimate the Critical Gap at Multilane Roundabouts', *Journal of Advanced Transportation*, 2018, pp. 1–10.
- Shaaban, K. and Hamad, H. (2020) 'Critical Gap Comparison Between One-, Two-, And Three-Lane Roundabouts In Qatar', *Sustainability (Switzerland)*, 12(10), pp. 1–14.
- Shaaban, K. and Kim, I. (2015) 'Comparison of SimTraffic and VISSIM Microscopic Traffic Simulation Tools in Modeling Roundabouts', *Procedia Computer Science*. Elsevier, 52, pp. 43–50.
- Siddharth, S. M. P. and Ramadurai, G. (2013) 'Calibration of VISSIM for Indian Heterogeneous Traffic Conditions', *Procedia - Social and Behavioral Sciences*. Elsevier, 104, pp. 380–389.
- Silva, A. B., Santos, S., Vasconcelos, L., Seco, Á. and Silva, J. P. (2014) 'Driver Behavior Characterization In Roundabout Crossings', *Transportation Research Procedia*. Elsevier, 3(July), pp. 80–89.
- Simpson, S. A. and Matthias, J. S. (2000) 'Validation of left-turn delay at two-way stop-controlled intersections', *Transportation Research Record*, (1710), pp. 181–188.

- Sofia, G. G., Al-Haddad, A. H. and Al-Haydari, I. S. (2012) ‘Development of Delay Models for Roundabouts’, *Journal of Engineering and Development*, 16(1), pp. 75–91.
- Sun, D., Zhang, L. and Chen, F. (2013) ‘Comparative study on simulation performances of CORSIM and VISSIM for urban street network’, *Simulation Modelling Practice and Theory*. Elsevier B.V., 37, pp. 18–29.
- Tanner, J. C. (1962) ‘A Theoretical Analysis Of Delays At An Uncontrolled Intersection’, *Biometrika*, 49(1), pp. 163–170.
- Tanyel, S., Çalışkanelli, S. P., Aydin, M. M. and Utku, S. B. (2013) ‘An Investigation Of Heavy Vehicle Effect On Traffic Circles’, *Turkish Chamber of Civil Engineers Digest 2013*, 24(4), pp. 1675–1700.
- Tanyel, S., Çelik, K., Özuysal, M. and Çalışkanelli, S. P. (2013) ‘Different Approaches To Minimum Delay Prediction At Single-Lane Traffic Circles In İzmir, Turkey’, *Canadian Journal of Civil Engineering*, 40(3), pp. 274–284.
- Tian, Z., Troutbeck, R., Kyte, M., Brilon, W., Vandehey, M., Kittelson, W. and Robinson, B. (2000) ‘A further investigation on critical gap and follow-up time’, *Transportation Research Circular E-C018: 4th International Symposium on Highway Capacity*, (Trb 1997), pp. 397–408.
- Tian, Z., Vandehey, M., Robinson, B. W., Kittelson, W., Kyte, M., Troutbeck, R., Brilon, W. and Wu, N. (1999) ‘Implementing The Maximum Likelihood Methodology To Measure A Driver’s Critical Gap’, *Transportation Research Part A: Policy and Practice*, 33(3–4), pp. 187–197.
- Toledo, T. and Koutsopoulos, H. N. (2015) ‘Statistical Validation of of Traffic Simulation Models’, *Transportation Research Record*. TRB, National Research Council, Washington, D.C., 1876(1)(August 2015), pp. 142–150.
- TRB (2000) ‘Highway Capacity Manual’, National Research Council, Washington, DC.
- TRB (2010) *Highway Capacity Manual*, National Research Council, Washington, DC.
- Troutbeck, R. (2014) ‘Estimating The Mean Critical Gap’, *Transportation Research Record*, 2461, pp. 76–84.
- Troutbeck, R. J. (1984) ‘Capacity And Delays At Roundabouts A Literature Review’, *Australian Road Research Board*, 14(4), pp. 205–216.
- Troutbeck, R. J. (1992) *Estimating The critical Acceptance Gap From Traffic Movements*. Queensland University of Technology.

- Trueblood, M. and Dale, J. (2003) 'Simulating Roundabouts With VISSIM', in 2nd Urban Street Symposium (Anaheim, California), pp. 1–11.
- Tupper, S. M. and Hurwitz, D. S. (2011) 'Connecting Gap Acceptance Behavior With Crash', in 3rd International Conference on Road Safety and Simulation Purdue University Transportation Research Board, pp. 1–18.
- Vaiana, R., Gallelli, V. and Capiluppi, G. (2007) 'Roundabout intersections: analysis for scenarios by microsimulation', 4th International SIIV Congress.
- Vaiana, R., Gallelli, V. and Iuele, T. (2012) 'Simulation Of Observed Traffic Conditions On Roundabouts By Dedicated Software', *Procedia - Social and Behavioral Sciences*, 53, pp. 741–753.
- Vaiana, R., Gallelli, V. and Iuele, T. (2013) 'Methodological approach for evaluation of roundabout performances through microsimulation', *Applied Mechanics and Materials*, 253–255(PART 1), pp. 1956–1966.
- Vasconcelos, L., Seco, Á. and Silva, A. B. (2013) 'Comparison Of Procedures To Estimate Critical Headways At Roundabouts', *Promet- Traffic & Transportation*, 25, pp. 43–54.
- Virginia Department of Transportation (2020) VDOT Vissim User Guide.
- Wang, W. and Yang, X. (2012) 'Research On Capacity Of Roundabouts In Beijing', *Procedia - Social and Behavioral Sciences*, 43, pp. 157–168.
- Wardrop, J. G. (1957) 'The Traffic Capacity Of Weaving Sections Of Roundabouts', in *Proceedings of the First International Conference on Operational Research*. Oxford English University Press.
- Washington State Department of Transportation (2014) Protocol for VISSIM Simulation.
- Wei, T., Shah, H. R. and Ambadipudi, R. (2012) 'VISSIM Calibration For Modeling Single-Lane Roundabouts: Capacity-Based Strategies', in *Transportation Research Board, 91st Annual Meeting. TRB*, pp. 1–16.
- Wiedemann, R. and Reiter, U. (1992) *Microscopic Traffic Simulation: The Simulation System MISSION, Background And Actual State, Project ICARUS (V1052) Final Report*.
- Wu, N. (2006) 'A New Model For Estimating Critical Gap And Its Distribution At Unsignalized Intersections Based On The Equilibrium Of Probabilities', in *Proceeding of the 5th international symposium on highway capacity and quality of service*. Yokohama, Japan.

- Wu, N. (2012) 'Equilibrium of probabilities for estimating distribution function of critical gaps at unsignalized intersections', *Transportation Research Record*, 2286(2286), pp. 49–55.
- Xiao, H., Ambadipudi, R., Hourdakis, J. and Michalopoulos, P. (2005) *Methodology For Selecting Microscopic Simulators : Comparative Evaluation Of AIMSUN and VISSIM, Final Report Human-Centered Technology To Enhance Safety And Mobility*.
- Xu, F. and Tian, Z. (2008) 'Driver Behavior And Gap-Acceptance Characteristics At Roundabouts In California', *Transportation Research Record*., 2071, pp. 117–124.
- Yap, Y. H., Gibson, H. M. and Waterson, B. J. (2013) 'An International Review of Roundabout Capacity Modelling', *Transport Reviews*, 33(5), pp. 593–616.
- Yu, M. and Fan, D. W. (2017) 'Calibration Of Microscopic Traffic Simulation Models Using Metaheuristic Algorithms', *International Journal of Transportation Science and Technology*. Tongji University and Tongji University Press, 6(1), pp. 63–77.
- Zeng, Q., Hao, W., Lee, J. and Chen, F. (2020) 'Investigating The Impacts Of Real-Time Weather Conditions On Freeway Crash Severity: A Bayesian Spatial Analysis', *International Journal of Environmental Research and Public Health*, 17(8).
- Zhang, Y., Sun, D. J. and Kondyli, A. (2017) 'An empirical framework for intersection optimization based on uniform design', *Journal of Advanced Transportation*, 2017.
- Zhaowei, Q., Duan, Y., Hu, H. and Song, and X. (2014) 'Capacity And Delay Estimation For Roundabouts Using Conflict Theory', *The Scientific World Journal*.
- Zhaowei, Q., Yuzhou, D., Xianmin, S. and Yan, X. (2014) 'Review and outlook of roundabout capacity', *Journal of Transportation Systems Engineering and Information Technology*. China Association for Science and Technology, 14(5), pp. 15–22.
- Zheng, D., Chitturi, M. V., Bill, A. R. and Noyce, D. A. (2012) 'Critical Gaps and Follow-Up Headways At Congested', *Transportation Research Board 91st Annual Meeting*, (608).

Zubaidi, H. A., Anderson, J. C. and Hernandez, S. (2020) 'Understanding Roundabout Safety Through The Application Of Advanced Econometric Techniques', International Journal of Transportation Science and Technology. Tongji University and Tongji University Press.

LIST OF PUBLICATIONS

Azhari, S.F., Puan, O.C., Hassan, S.A., Mashros, N., Warid, M.N. and Lopa, R.S., 2019, May. Estimation of critical gap at small roundabout. In *IOP Conference Series: Materials Science and Engineering* (Vol. 527, No. 1, p. 012072). IOP Publishing.

Azhari, S.F., Hassan, S.A. and Puan, O.C., 2020, July. Relationship Between Delay, Accepted Gap and Circulating Flow at Roundabout. In *IOP Conference Series: Materials Science and Engineering* (Vol. 884, No. 1, p. 012037). IOP Publishing.