

MESOSCALE LAMINA FATIGUE DAMAGE MODEL FOR  
FIBER-REINFORCED POLYMER COMPOSITE LAMINATES

AZISYAHIRAH AZIZAN

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Faculty of Engineering  
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## **DEDICATION**

*To Mak & Abah*

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## ABSTRACT

Carbon fiber-reinforced polymer (CFRP) composite laminates used as load-bearing structures, such as skin of aircraft wings and wind turbine blades, are likely to experience fatigue loading. The resulting complex stresses could cause fatigue damage in the laminas in the form of matrix cracking, interface delamination, and fiber fracture. The prediction of the reliability of these structures requires an accurate constitutive damage model of the composite material. However, the previous available damage models are based on stress control condition and limited to low cycle fatigue loading conditions. In this respect, the research proposes and examines a new universal damage-based material fatigue model of unidirectional lamina. The mesoscale model incorporates the observed degradation of the lamina strength and stiffness properties in defining the material damage under cyclic loading conditions. Hashin's stress-based criteria for damage under monotonic loading are extended and used to describe the fatigue damage accumulation process. The normalized model is employed to describe the fatigue degradation of the strength and stiffness properties. The model acknowledges the effects of mean stress on the damage and fracture process. It is observed that the shear strength of the CFRP composite lamina is the first to degrade when compared to other properties. The predicted fatigue damage evolution characteristics are examined for a typical material point in the CFRP composite lamina throughout the fatigue loading. For this purpose, a finite element (FE) model of a CFRP composite laminate plate with a through central hole is subjected to tension-tension cyclic stressing ( $\kappa=0.1$ ) in transverse fiber direction. Since cycle-by-cycle life calculations are impractical given the large number of anticipated fatigue cycles involved, a load-cycle block sequence is introduced to address the computational efficiency of the fatigue life prediction routine. The number of load cycles represented by each block is dictated by the rate of the property degradation. The size of a load cycle block is determined by the residual property curve that exhibits the shortest fatigue life,  $N_f$  under the operating fluctuating load cycles. Nonlinear characteristic evolution of the fatigue damage with the applied stress cycles is demonstrated. The critical level of the fatigue damage, determined based on the total dissipated energy of fracture, denotes the nucleation of the fatigue crack through the separation of the material point. From the case study, with the operating stresses of  $\sigma_{22}^{max}=18.85$  MPa and  $\tau_{12}^{max}=1.30$  MPa, the accumulated matrix tension fatigue damage at the critical point reaches  $g_{MT} = 1.0$  after  $n^d = 1.93 \times 10^3$  cycles have elapsed. The collection of the separated material points throughout the applied fatigue cycles represents the propagated fatigue crack. The calculation routine is readily implemented in any standard FEA software for damage-based fatigue life prediction of fiber-reinforced polymer (FRP) composite laminate structures. The unified fatigue damage model developed in this thesis is significant for industrial sectors, dealing with FRP composite design, fabrication, reliability prediction, and failure analysis of load-bearing structures.

## ABSTRAK

Lapisan komposit polimer yang diperkuat dengan gentian karbon (CFRP) yang digunakan sebagai struktur penahan beban, seperti kulit sayap pesawat dan bilah turbin angin, cenderung untuk mengalami kelesuan. Tegasan kompleks yang terhasil boleh menyebabkan kerosakan akibat kelesuan dalam lapisan lamina dalam bentuk keretakan matriks, pelekangan antara muka, dan keretakan gentian. Ramalan kebolehharian struktur komposit ini memerlukan model konstitutif kerosakan yang tepat. Walau bagaimanapun, model kerosakan yang tersedia sebelum ini adalah berdasarkan keadaan kawalan tegasan dan terhadap kepada keadaan pembebanan kelesuan kitaran rendah. Dalam hal ini, penyelidikan mencadangkan dan meneliti model baru semesta kelesuan bahan yang dibangunkan berasaskan kerosakan dari ekaarah lamina. Model skala meso menggabungkan penurunan kekuatan lamina dan sifat kekukuhan yang diperhatikan dalam menentukan kerosakan bahan dalam keadaan pembebanan berkitar. Kriteria Hashin yang berdasarkan tegasan di bawah pembebanan berkitar dikembangkan dan digunakan untuk menggambarkan proses penumpukan kerosakan akibat kelesuan. Model ternormal digunakan untuk menggambarkan penurunan sifat kekuatan dan kekukuhan akibat kelesuan. Model ini merangkumi kesan tegasan min terhadap proses kerosakan dan kepatahan. Telah diperhatikan bahawa kekuatan ricih pada CFRP komposit lamina adalah yang pertama merosot jika dibandingkan dengan sifat lain. Ciri-ciri evolusi kerosakan kelesuan yang diramalkan diperiksa pada titik tertentu pada bahan dalam lamina CFRP komposit sepanjang pembebanan kelesuan. Untuk tujuan ini, model FE dari plat CFRP komposit lamina berserta lubang pada tengah plat dikenakan tegasan tegangan-tegangan berkitar ( $\kappa=0.1$ ) pada arah melintang gentian. Oleh kerana pengiraan jangka hayat kitaran demi kitaran tidak praktikal memandangkan bilangan besar kitaran kelesuan yang terlibat, urutan blok kitaran beban diperkenalkan untuk menangani kecekapan rutin komputasi untuk ramalan jangka hayat akibat kelesuan. Jumlah kitaran beban yang ditunjukkan oleh setiap blok ditentukan oleh kadar penurunan sifat kekuatan bahan. Blok kitaran beban ditentukan oleh baki kekuatan bahan dengan jangka hayat terpendek ( $N_f$ ) di bawah bebanan kelesuan. Evolusi tidak lurus menggambarkan kerosakan akibat kelesuan dengan kitaran tegasan yang berlaku ditunjukkan. Tahap kritikal kerosakan kelesuan, ditentukan berdasarkan jumlah tenaga patah yang hilang, menunjukkan penukleusan retak akibat kelesuan. Daripada kajian kes di bawah operasi tegasan  $\sigma_{22}^{max}=18.85$  MPa dan  $\tau_{12}^{max}=1.30$  MPa, kerosakan kelesuan dalam bentuk tegangan matriks terkumpul pada titik kritikal memenuhi persamaan  $g_{MT}=1.0$  selepas melalui  $n^d=1.93 \times 10^3$  kitaran. Pengumpulan titik bahan yang terpisah sepanjang kitaran kelesuan yang berlaku mewakili retakan akibat kelesuan tersebar. Rutin pengiraan mudah dilaksanakan dalam mana-mana perisian standard FEA untuk ramalan yang tepat bagi jangka hayat bahan daripada struktur komposit polimer lamina bertetulang gentian (FRP) akibat kelesuan. Model kerosakan bersatu akibat kelesuan yang dibangunkan dalam tesis ini adalah penting untuk sektor perindustrian yang berkaitan dengan industri pembuatan FRP komposit, fabrikasi dan analisis kegagalan struktur penahan beban.

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## LIST OF ABBREVIATIONS

3D	-	Three-dimensional
AFP	-	Automated fiber replacement
ASTM	-	American Society for Testing and Materials
ATL	-	Automated tape laying
CDM	-	Continuum damage mechanics
CFRP	-	Carbon-fiber reinforced polymer
CTRM	-	Composite Technology Research Malaysia
CZM	-	Cohesive zone model
FE	-	Finite element
FEM	-	Finite element modeling
FRP	-	Fiber-reinforced polymer
GFRP	-	Glass-fiber reinforced composite laminates
HLU	-	Hand lay-up
RFI	-	Resin film infusion
RP	-	Reference point
RTM	-	Resin transfer molding
SC8R	-	8-node hexahedron, general-purpose, finite membrane strains element
UAV	-	Unmanned aerial vehicle
UD	-	Unidirectional
UHMW	-	Ultra-high molecular weight polyethylene
VIP	-	Vacuum Infusion Process



## LIST OF SYMBOLS

$d_{FC}$	-	Damage indicator in fiber damage under compression under quasi-static loading.
$d_{FT}$	-	Damage indicator in fiber damage under tension under quasi-static loading.
$d_{MC}$	-	Damage indicator in matrix damage under compression under quasi-static loading.
$d_{MT}$	-	Damage indicator in matrix damage under tension under quasi-static loading.
$E$	-	Young's modulus
$\hat{E}$	-	Normalized stiffness
$\hat{E}_{11}$	-	Normalized longitudinal stiffness
$\hat{E}_{22}$	-	Normalized transverse stiffness
$G$	-	Shear modulus
$g_{FC}$	-	Damage indicator in fiber damage under compressive fatigue loading.
$g_{FT}$	-	Damage indicator in fiber damage under tensile fatigue loading.
$g_{MC}$	-	Damage indicator in matrix damage under compressive fatigue loading.
$g_{MT}$	-	Damage indicator in matrix damage under tensile fatigue loading.
$\hat{G}_{12}$	-	Normalized shear stiffness
$n$	-	Number of cycles
$\hat{N}$	-	Normalized number of cycles
$N_f$	-	Number of cycles to failure
$P_{cyclic}$	-	Cyclic load
$P_{max}$	-	Maximum load
$P_{min}$	-	Minimum load
$\kappa$	-	Stress-ratio

$R$	-	Residual strength
$\hat{R}$	-	Normalized strength
$S_1$	-	Interface shear strength for sliding shear mode
$S_2$	-	Interface shear strength for tearing shear mode
$S^L$	-	Longitudinal shear strength
$S^T$	-	Transverse shear strength
$\hat{S}^L$	-	Normalized longitudinal shear strength
$\hat{S}^T$	-	Normalized transverse shear strength
$T$	-	Interface tensile strength
$U_x$	-	Displacement in x-axis
$U_y$	-	Displacement in y-axis
$U_z$	-	Displacement in z-axis
$UR_x$	-	Rotation about x-axis
$UR_y$	-	Rotation about y-axis
$UR_z$	-	Rotation about z-axis
$X^C$	-	Longitudinal compressive strength
$X^T$	-	Longitudinal tensile strength
$\hat{X}^C$	-	Normalized longitudinal compressive strength
$\hat{X}^T$	-	Normalized longitudinal tensile strength
$Y^C$	-	Compressive tensile strength
$Y^T$	-	Transverse tensile strength
$\hat{Y}^C$	-	Normalized transverse compressive strength
$\hat{Y}^T$	-	Normalized transverse tensile strength
$\alpha$	-	Contribution of shear stress to the fiber tension mode of failure
$\gamma$	-	Shear strain
$\varepsilon$	-	Strain
$\varepsilon_f$	-	Strain to failure
$\sigma$	-	Nominal, true or Cauchy stress tensor
$\sigma^a$	-	Amplitude stress
$\sigma^m$	-	Mean stress
$\sigma^{max}$	-	Maximum stress

- $\tau$  - Shear stress
- $\nu$  - Poisson's ratio
- $\chi$  - Life parameter

# CHAPTER 1

## INTRODUCTION

### 1.1 Research Background

FRP composite material is used for applications in various industries, such as aeronautical, automotive, marine, and advanced engineering applications. This is due to the high strength-to-weight ratio of FRP composite that makes them desirable for structural applications than conventional material. In the aerospace and automotive industries, the aim can be accomplished by substituting metal-based alloys with lighter materials such as carbon fiber-reinforced polymer (CFRP) composite. This may explain the significant increase in the use of CFRP composite material which is less than 20% in 1987 (A320), to over 50% in 2013 (A350 XWB) [1]. Besides, FRP composite material provides corrosion resistance in the marine environment and therefore requires less maintenance. Nowadays, racing powerboats such as superyachts made of composite are becoming more common for long-lasting performance and safety. The 48M Supersport is the largest superyacht constructed out of FRP composite which the fuel efficiency is optimized by 50% due to weight reduction[2]. Apart from that, CFRP composites provide design flexibility through the sequencing of pre-impregnated laminates for tailored strength and stiffness properties in particular loading directions. Thanks to these advantages, the wind industry is growing rapidly during the last half of the twentieth century and continues to grow to meet the demand for larger wind turbine rotor blades.

The fact that could not be avoided is that the composite components are subjected to different loading types, both static and fatigue, as well as the harsh operating environment. This necessitates investigations, particularly into fatigue and fracture analysis of the structure. Fatigue is the most frequent cause of structural failures and should be accounted for in any structural design process. In fact, in the last decades, fiber-reinforced polymer (FRP) composite has attracted increasing

attention, especially in fatigue [3]. Under fatigue loading conditions, the FRP composite laminate simultaneously experiences multiple damage mechanisms, including intra- and interlaminar. The laminate consists of plies of the lamina and the interfaces between the laminas. In order to reduce the complexity, the effect of fatigue loading is treated separately in laminas and interfaces. Therefore, it is of paramount importance to understand the mechanism associated with fatigue damage and introduce a predictive model to predict the damage in FRP composite laminate.

Fatigue damage models are necessary to be well developed by adapting the damage mechanics approach to predict damage development in the laminated composite structure during service lifetime. In the FRP composite laminates, the development of damage is depicted through the degradation of material properties. However, the variety of laminate design configurations makes it impractical to determine degradation properties through experimentation alone. Thus, it is more desirable to predict the material performance during fatigue loading conditions by modeling behavior in response to the applied load. An accurate fatigue damage model for the laminated composite could facilitate design improvement of FRP composite structure. The fatigue model should be able to predict the fatigue behavior of the laminate for any layup configuration for structural reliability assessment.

Consequently, this research work complements the development of damage-based fatigue model for FRP composite laminates. The emphasis is on the fatigue failure of the laminas. The fatigue model of the interfaces is being addressed separately. Ultimately, the fatigue damage model for lamina and interface is implemented in the reliability prediction of FRP composite laminates, where the interaction of interface and lamina damage is captured under general loading conditions.

## 1.2 Statement of Research Problem

The damage development during fatigue loading conditions in a FRP composite lamina is predicted using a damage model. In this study, the unified damage model is developed based on the degradation of mechanical properties of the material. The evolution of fatigue damage is described through the degradation of fracture energy. The modeling concept for the FRP composite laminates has been studied and available the open literature [4, 5] based on stress controlled condition. However, the approach presented in this thesis is illustrated for constant displacement during the fatigue loading. It follows that the effect of damage is observed through the level of stress diminishing during the loading cycles. In addition, in a multidirectional laminate, the significant failure mechanism is addressed by the competition between the weak interfaces and continuously degrading matrix properties of the lamina. The approach is to address the issues separately. In this study, the damage-based fatigue model is developed for the quantitative and physically-based description of fatigue damage development of the lamina. Developing a unified damage model allows a better prediction of fatigue behavior of the laminate, particularly for the lamina. Such model caters for the damage prediction in any layup configuration of the laminates. Since the model is accounts for the non-linear properties degradation, an incremental calculation procedure is introduce to address the accumulated damage throughout the fatigue loading. This approach addresses the central question of *“How to correctly and efficiently predict the reliability and failure response of CFRP composite lamina under cyclic loading condition.”*

## 1.3 Research Objectives

This research aims to develop a new damage-based fatigue model of unidirectional FRP composite lamina. The specific objectives are:

- (a) To establish characteristic residual properties of the lamina due to fatigue loading conditions.

- (b) To develop a new damage model for fatigue of UD lamina based on cyclic property degradation.
- (c) To quantify the characteristic evolution of the lamina damage under cyclic loading conditions

#### **1.4 Scope of Study**

The scopes of study cover the following:

1. Lamina damage model is developed based on equivalent UD lamina at mesoscale.
2. Mechanical destructive tests are conducted on CFRP composite lamina  $[0^\circ]_s$  for properties extraction. The tests are conducted according to American Society for Testing and Materials (ASTM) standards. These tests are conducted at room temperature and laboratory air/humidity environment under static loading.
3. Property degradation modes are developed. Test data in item 2 are used in the model.
4. Incremental fatigue damage is calculated based on load cycle-block approach.
5. Fatigue damage evolution characteristic is illustrated through a case example of 16-ply CFRP composite laminate with a straight-through hole. Computational efficiency is considered in fatigue damage calculations. This would be practical in addressing reliability of composite structures.
6. FE simulation using SIMULIA Abaqus ver. 6.12 commercial software.

## **1.5 Significance of the Outcomes**

The degradation of residual fatigue properties dictates the fatigue damage accumulation in the FRP composite lamina. The properties degradations are obtained through the normalization of residual properties to the static properties. Thus, the developed methodology can be extrapolated to any set of properties for carbon-based FRP composite under various stress ratios without reproducing the experimental tests. In addition, the methodology can be adopted for any FRP composite laminate layup configuration. Due to the high number of fatigue cycles involved, a load-cycle block approach is introduced to address the efficiency issue in fatigue damage prediction. The establishment of methodology and predictive model will fulfill the industrial requirement, especially reducing the number of experimental tests. This is significant for all industrial sectors, including aerospace, automotive, marine, and advanced engineering applications.

## **1.6 Thesis Layout**

All chapters in this thesis had been arranged to establish a model for predicting fatigue damage in FRP composite lamina. The methodology for predicting the fatigue lamina damage was explained in this thesis. Therefore, the content of each chapter had been specified to explain the objectives and scope of the research as follows.

Chapter 1 describes a summary background of composite laminates. Then the problem statement, scope, and objectives of the research are defined. The limits of what this study is restricted to are being highlighted.

Chapter 2 summarizes previous researchers' findings and literature regarding CFRP composite laminates properties and behavior under static and fatigue loading. This includes the previous research on related static and fatigue damage models for FRP composite laminate. A review of existing damage models for cyclic loading applications is presented to bring the reader up to date with the current literature on the topic.



Chapter 3 details about research methodology of the current work. A methodology on process of constructing the new lamina fatigue damage model is explained. The foundation of extracting fatigue degradation properties through quasi-static tests is elaborated. The details on the finite element (FE) simulation for the case study are described.

Chapter 4 describes the characteristic of the cyclic degradation properties. The normalized strength approach is adapted in order to obtain properties degradation for fatigue loading. Also, the applicability of this method for carbon-based material is presented in this chapter. As a result, nine normalized properties degradation curves are generated, including residual strength and stiffness properties.

Chapter 5 elaborates the extended theory for the lamina damage model for CFRP composite laminates under cyclic loading conditions. A set of new fatigue damage criteria is proposed to predict damage specifically in a FRP composite lamina. The characteristic of the damage model for lamina damage is explained here.

Chapter 6 discuss the fatigue damage evolution in CFRP composite lamina based specific case study. The newly developed fatigue damage model for the lamina is explained through the numerical value resulted from the case study. Detailed analysis of damage calculation is given in this chapter. The energy-based concept is used to discuss the evolution of fatigue damage to nucleation at a material point.

Chapter 7 summarizes the main conclusion related to the methodology to obtain the damage parameters and the newly extended lamina damage model under cyclic damage conditions. The main contributions that have been addressed in the form of research objectives were concluded in this chapter. Additional work was recommended for further advanced research.

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