

ASSESSING FORECASTING PERFORMANCE ON GOLD DATA USING
ARTIFICIAL NEURAL NETWORK BASED MODELS

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ASSESSING FORECASTING PERFORMANCE ON GOLD DATA
USING ARTIFICIAL NEURAL NETWORK BASED MODELS

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ABSTRACT

Gold is the most stable commodity when compared to oil, crypto currency and even stock bonds. It is to gold that men turn to in the midst of political and monetary vulnerability, a place of refuge that gives versatile store of value, the common insurance hedge against bankruptcy and chaos. Forecasting gold price and gold demand is an important step to ensure that gold remains as a valuable form of investment or asset instead of being a liability. Large gold bullions and gold authorities do forecasting with a large set of data but this is not the case for a private investor or consumer since these data are not made easily available to the public. In this research a model was developed to conduct a forecast with a limited set of data and the model is then tested using a large set of data. The quarterly world gold demand from 2010 to 2017 obtained from worldgoldcouncil.org were used as the limited data set and the daily world gold price within 2017 obtained from the London Bullion Market (LBMA) portal were used as the large data set. Artificial Neural Network (ANN) is the most common model for forecasting with a limited data set, but in this study the Multilayer Perceptron (MLP) model is developed with a Wavelet decomposition as well as bootstrapping. Both sets of data were fitted into the ANN model, Bootstrap Artificial Neural Network (BANN) model, Wavelet Artificial Neural Network (WANN) model and finally Wavelet Bootstrap Artificial Neural Network (WBANN) model. It is found that for the limited data set, the best model for the limited data set with the lowest value of Mean Absolute Percentage Error (MAPE) and Root Mean Squared Error (RMSE) is the WBANN model with 20.19 and 232.58, MAPE and RMSE values respectively. Meanwhile the best model for the large data set was also the WBANN model with 0.89, 12.58 MAPE and RMSE values respectively. The accuracy index for the large data set corresponds with that from the limited data set models. Thus, WBANN model is the best model for limited data forecasting.

ABSTRAK

Emas adalah komoditi yang paling stabil jika dibandingkan dengan minyak, mata wang kripto dan juga bon saham. Emaslah yang orang beralih kepada di tengah-tengah kelemahan politik dan kewangan, suatu tempat perlindungan yang memberikan harga kedai yang bernilai, lindung nilai insurans biasa terhadap kebangkrapan dan huru-hara. Ramalan harga emas dan permintaan emas adalah satu langkah penting untuk memastikan emas kekal sebagai satu bentuk pelaburan atau aset yang bernilai dan bukan liabiliti atau. Bulion emas yang besar dan pihak berkuasa emas melakukan ramalan dengan set data yang besar tetapi ini tidak berlaku untuk pelabur swasta atau pengguna awam kerana data ini tidak mudah didapati kepada orang ramai. Dalam kajian ini model untuk menjalankan ramalan dengan satu set data terhad telah dibangunkan dan model ini kemudian diuji menggunakan set data yang besar. Suku tahunan permintaan emas dunia 2010-2017 yang diambil dari worldgoldcouncil.org telah digunakan sebagai set data terhad dan harga harian dunia emas tahun 2017 yang diperolehi daripada portal London Bullion Market (LBMA) telah digunakan sebagai set data yang besar. Artificial Neural Network (ANN) adalah model yang paling biasa untuk meramal dengan satu set data yang terhad, tetapi dalam kajian ini yang model Multilayer Perceptron (MLP) dibangunkan dengan penguraian Wavelet serta Bootstrap. Kedua-dua set data telah dimautkan ke dalam model ANN, model Bootstrap Artificial Neural Network (BANN), model Wavelet Artificial Neural Network (WANN) dan model Wavelet Bootstrap Artificial Neural Network (WBANN). Didapati bahawa untuk set data yang terhad, model yang terbaik dengan nilai terendah Mean Absolute Percentage Error (MAPE) dan Root Mean Squared Error (RMSE) adalah model WBANN dengan masing-masing menghasilkan 20.19 dan 232.58 nilai MAPE dan RMSE. Sementara itu model yang terbaik untuk set data yang besar juga adalah model WBANN dengan masing-masing menghasilkan 0.89, 12.58 nilai MAPE dan RMSE. Indeks ketetapan untuk set data yang besar sepadan dengan yang dari model set data yang terhad. Oleh itu, model WBANN adalah model terbaik untuk ramalan data yang terhad.

TABLE OF CONTENTS

	TITLE	PAGE
	DECLARATION	ii
	DEDICATION	iv
	ACKNOWLEDGEMENT	v
	ABSTRACT	vi
	ABSTRAK	vii
	TABLE OF CONTENTS	viii
	LIST OF TABLES	xi
	LIST OF FIGURES	xiii
	LIST OF ABBREVIATIONS	xv
	LIST OF SYMBOLS	xvi
	LIST OF APPENDIX	xvii
CHAPTER 1	INTRODUCTION	1
1.1	Introduction	1
1.2	Research Background	1
1.3	Problem Statement	3
1.4	Research Objectives	3
1.5	Scope of the Study	4
	1.5.1 Scope of Data	4
	1.5.2 Scope of Model	4
1.6	Significance of Findings	5
1.7	Research Framework	5
CHAPTER 2	LITERATURE REVIEW	7
2.1	Introduction	7
2.2	Gold	7
2.3	Gold Chronicle	8
2.4	Gold Demand	10
2.5	Large Data Forecasting for Gold Price	12

2.6	Hybrid Model in Time Series Forecasting	14
2.7	Forecasting Price Changes With Neural Network	15
2.8	Limited Data Forecasting in General Applications	17
2.9	Conclusion	19
CHAPTER 3	RESEARCH METHODOLOGY	21
3.1	Introduction	21
3.2	Research Framework	21
3.3	Artificial Neural Network (ANN) Model	22
3.3.1	Multilayer Perceptron	25
3.4	Bootstrapping	27
3.4.1	Bootstrap Artificial Neural Network (BANN)	29
3.5	Wavelet Analysis	32
3.5.1	Continuous Wavelet Transform (CWT)	33
3.5.2	Discrete Wavelet Transform (DWT)	34
3.5.3	Multiresolution Analysis (MRA)	36
3.5.4	Wavelet Artificial Neural Network (WANN)	39
3.6	Wavelet Bootstrap Artificial Neural Network (WBANN)	42
3.7	Descriptive Statistics	43
3.8	Ljung-Box Test	44
3.9	Auto-correlation and Partial Auto-correlation Functions (ACF & PACF)	45
3.10	Model Accuracy	46
3.11	Conclusion	47
CHAPTER 4	Limited Data Forecasting and Analysis	49
4.1	Introduction	49
4.2	Descriptive Statistics	49
4.3	Forecasting With Artificial Neural Network (ANN)	54
4.4	Forecasting with Bootstrap Artificial Neural Network (BANN)	57
4.5	Forecasting with Wavelet Artificial Neural Network (WANN)	59
4.6	Forecasting with Wavelet Bootstrap Artificial Neural Network (WBANN)	67

4.7	Conclusion	69
CHAPTER 5	Large Set Data Forecasting and Analysis	73
5.1	Introduction	73
5.2	Artificial Neural Network (ANN)	74
5.3	Bootstrap Artificial Neural Network (BANN)	76
5.4	Wavelet Artificial Neural Network (WANN)	78
5.5	Wavelet Bootstrap Artificial Neural Network (WBANN)	82
5.6	Limited Data vs Large Data	84
5.7	Conclusion	85
CHAPTER 6	CONCLUSION	87
6.1	Introduction	87
6.2	Summary	87
6.3	Conclusion	89
6.4	Recommendations for Future Research	90
REFERENCES		93

LIST OF TABLES

TABLE NO.	TITLE	PAGE
Table 2.1	Gold Throughout Time	9
Table 4.1	Quarterly World Gold Demand 2011-2017	50
Table 4.2	Mean, Standard Deviation & Variance of Data	50
Table 4.3	Skewness and Kurtosis Value of Data	50
Table 4.4	ANN Number of Hidden Nodes and their Respective MSE	55
Table 4.5	Fitted Values of MLP ANN Model	57
Table 4.6	MAPE and RMSE of Fitted MLP ANN Model	57
Table 4.7	Forecasted Values for Quarter of 2017 using MLP ANN Model	57
Table 4.8	Fitted Bootstrap Artificial Neural Network Values	58
Table 4.9	MPAE and RMSE of BANN Model	59
Table 4.10	Forecasted Values of the BANN Model	59
Table 4.11	Wavelet MRA with Db20 of 3 Level Decomposition Output	61
Table 4.12	Wavelet Coefficients	61
Table 4.13	MSE of ANN Model for Each Decomposed Data	64
Table 4.14	Table 4.12 Fitted MLP ANN Decomposition Values (Part 1)	65
Table 4.15	Fitted WANN Model Values	65
Table 4.16	MAPE and RMSE of WANN Model	65
Table 4.17	Forecasted Values of WANN Model	67
Table 4.18	Fitted Wavelet Bootstrap Artificial Neural Network Values	68
Table 4.19	MAPE and RMSE of WBANN Model	68
Table 4.20	Forecasted Values of WBANN Model	69
Table 4.21	Performance Index of Each Method Used	70
Table 5.1	ANN Structure with Different Number of Hidden Neurons and Their Respective MSEs	75
Table 5.2	MAPE and RMSE of ANN Model	76

Table 5.3	MAPE and RMSE of BANN Model	77
Table 5.4	ANN Model with Various Number of Hidden Neurons for Each Component of the DWT	79
Table 5.5	MAPE and RMSE of WANN Model	79
Table 5.6	MAPE and RMSE of WBANN Model	83
Table 5.7	Error of Limited and Large Data	84

LIST OF FIGURES

FIGURE NO.	TITLE	PAGE
Figure 2.1	World Gold Council Gold Price	9
Figure 3.1	Research Framework	23
Figure 3.2	A Neuron of the Human Brain (Daniel Graupe, 2007)	24
Figure 3.3	Artificial Neuron with Inputs and Single Output (Priddy, Keller and Society of Photo-optical Instrumentation Engineers., 2005)	25
Figure 3.4	Simple MLP Model (Shao, 2018)	26
Figure 3.5	ANN MLP Model with Weighted Inputs and Embedded Transfer Function (Priddy et al., 2005)	27
Figure 3.6	Bootstrapping Algorithm (<i>15.3 - Bootstrapping</i> , 2018)	28
Figure 3.7	Bootstrap Artificial Neural Network Structure (Ferrario, Pedroni, Zio and Lopez-Caballero, 2017)	31
Figure 3.8	Wavelet Decomposition and Reconstruction (Misiti, Misiti, Oppenheim and Poggi, 2010)	36
Figure 3.9	Structure of Wavelet Artificial Neural Network with Output Expression (Alexandridis and Zapranis, 2013)	41
Figure 3.10	Flow Chart of Wavelet Artificial Neural Network Model for Forecasting Univariate Time Series (Mohammed and Ibrahim, 2012)	42
Figure 3.11	Wavelet Bootstrap Artificial Neural Network Structure (Rafiei, Niknam and Khooban, 2016)	43
Figure 4.1	Histogram of World Gold Demand	51
Figure 4.2	Time Series Plot of Quarterly World Gold Demand 2010-2017	51
Figure 4.3	Linear Trend of Quarterly World Gold Demand 2010-2017	52
Figure 4.4	Autocorrelation Function (ACF) Test of Data	53
Figure 4.5	Partial Autocorrelation Function (PACF) Test on Data	53
Figure 4.6	Output of the Ljung-Box Test for Independence	54
Figure 4.7	Multilayer Perceptron Model (MLP) of a Feedforward ANN	56

Figure 4.8	Fitted MLP ANN Model (Red=Fitted, Black=Actual, Blue=Forecast)	56
Figure 4.9	Bootstrap Artificial Neural Network Time Series (Black=Actual, Red=Model, Blue=Forecast)	58
Figure 4.10	Details 1 (d1) Decomposition of Data	62
Figure 4.11	Details 2 (d2) Decomposition of Data	62
Figure 4.12	Details 3 (d3) Decomposition of Data	63
Figure 4.13	Approximation 3 (a3) Decomposition of Data	63
Figure 4.14	Fitted and Forecasted Plot of WANN Model (Red=Fitted, Blue=Forecast)	66
Figure 4.15	Plotted WBANN Model and Forecast (Red=WBANN, Blue=Forecast)	69
Figure 5.1	Daily London Bullion Market (LBMA) AM Gold Price of 2017	74
Figure 5.2	Daily London Bullion Market (LBMA) AM Gold Price of 2017	76
Figure 5.3	Fitted and Forecasted of BANN Model with 100 Resampling	77
Figure 5.4	Fitted and Forecasted Plot of WANN model	78
Figure 5.5	Detail 1(D1) Component of Wavelet Decomposition of LBMA Gold Price	80
Figure 5.6	Detail 2(D2) Component of Wavelet Decomposition of LBMA Gold Price	81
Figure 5.7	Detail 3(D3) Component of Wavelet Decomposition of LBMA Gold Price	81
Figure 5.8	Approximation 3(A3) Component of Wavelet Decomposition of LBMA Gold Price	82
Figure 5.9	Fitted and Forecasted Outcome of WBANN Model	83

LIST OF ABBREVIATIONS

MLP	-	Multilayer Perceptron
ANN	-	Artificial Neural Network
WANN	-	Wavelet Artificial Neural Network
BANN	-	Bootstrap Artificial Neural Network
WBANN	-	Wavelet Bootstrap Artificial Neural Network
MRA	-	Multiresolution Analysis
DWT	-	Discrete Wavelet Transform
CWT	-	Continuous Wavelet Transform

LIST OF SYMBOLS

w	-	Weight
x	-	Onput
Z	-	Output
S	-	Total number of resamples
$f_{NN}(x, w_S)$	-	ANN output
ψ	-	Wavelet
$\psi_{a,b}(t)$	-	Mother wavelet
a	-	Scaling parameter
b	-	Translation parameter

LIST OF APPENDICES

APPENDIX	TITLE	PAGE
Appendix A	R Software Code	103
Appendix B	Wavelet Decomposition Comparison	115
Appendix C	Fitted Values from ANN Model for Daily Gold Price	117

CHAPTER 1

INTRODUCTION

1.1 Introduction

This chapter presents the introduction. It begins with stating and elaborating the background of data for the research and followed by the problem statement. The problem statement will give a much clearer aim for this study. Objective of this study will also be presented in this chapter. Objectives are a derivation of the aim of this study, what were done to achieve the main goal. What this study encompasses is stated in the scope of study. Scope of data as well as scope of model used is explained there. Lastly, significance of study or importance of this study is elaborated.

1.2 Research Background

Compared to crude oil, crypto currency or even stock bond, gold is considered as one the most stable commodity. Nonetheless, being a commodity prices of gold still fluctuates from time to time. Thus, methods of forecasting future gold price is constantly being developed with the aim of finding the most accurate model to predict the price of future gold. In this study a model for forecasting gold price and gold demand using neural network with a hybridization a discrete wavelet transform decomposition will be explored. This method of study is also known as demand forecast research.

As the case of other commodities in the market around the world, price of gold

are most dependent on the concept of supply and demand. Demand is the amount or quantity of a product in which the buyers desire, while supply is the amount or quantity that the market are able to offer. The concept states that as the demand for a certain product; for instance gold, is high and supply is abundant, prices of gold will drop. But in the case of high demand but inadequate supply, the prices of gold will soar.

Forecasting the demand of gold may allow mining companies, as well as commodity market to take into account the demand of gold worldwide as well as the amount of gold in the reserves. With high demand of gold, but low reserve volume, prices of gold are going to soar and vice versa. If forecasted values are accurate enough, mining process as well as gold reserve authorities could plan production or mining and selling of gold. Thus lowering chances of shortage in the reserve.

There have been previous studies on gold demand. Most of the issues faced when forecasting a commodity whether it is price of gold or demand of gold are the accuracy of the model. Another problem faced was limited data resources. Since only certified authorities have the data on gold price and gold demand, not much has been released to the public. This study aims to overcome that problem by modelling a forecast with limited data length.

According to Abu (2016), a data set of length 4 to 30 is considered as a limited data. Unlike normal length data, a limited data cannot be modeled using the common practise of forecasting. A few of the most common forecasting model are the Auto Regressive Integrated Moving Average (ARIMA) model, exponential smoothing, extrapolation and trend estimation. These models mentioned require a large amount of data to operate. Thus in this study a model that can accomodate a limited data set will be explored.

The limited data set used in this study are the quarterly world demand of gold from 2010 to 2017. The data is then fitted into a suitable mode and to further verify the accuracy of the model, the model is then fitted into a larger data set which is the price

of gold. Thus, this study will conclude accuracy of those model and forecasted world gold demand.

1.3 Problem Statement

Gold is a commodity that have been used since ancient times. Prices and demands of gold continues to rise even to this day. Gold demand data is scarced, leading to a limited amount of data. While the data for gold price is abundant, leading to a large amount of data. Which brings us to the problem statement:

- (a) What model can accomodate both large and limited data set?
- (b) How to adopt a limited data set to the neural network model?
- (c) Which neural network model would best fit the data set?
- (d) Is the large data set better for forecasting than the limited data set?

1.4 Research Objectives

Objectives of this study are as follows:

- (a) To identify the best neural network model by determining the number of hidden neurons used.
- (b) To expand limited data set by bootstrapping and wavelet decomposition.
- (c) To replicate the results of the first and second objective with a larger data set.
- (d) To conduct a comparative study on forecasting with limited data set and large data set.
- (e) To determine the best hybrid model out of ANN, BANN, WANN and WBANN for limited and large data set by evaluating the error index of each model.

1.5 Scope of the Study

Scope of this study will be explained in two parts. The first part is on the data used, while second part will be on the model and methods used.

1.5.1 Scope of Data

There will be two types of data used in this study. First is the limited data set, which is taken from the worldcouncil.org website. Limited data set used are the data of quarterly world gold demand in tonnes by worldgoldcouncil.com from first quarter of 2010 to fourth quarter of 2017. While a normal length of 249 data set were taken from lbma.org.uk. Which is the London Bullion Market web site. Daily gold prices of USD per troy ounce in the London Bullion Market from January 2017 to December 2017 were used for this study.

1.5.2 Scope of Model

This study uses a number of models. First model is an Artificial Neural Network Model (ANN), more specifically a Multilayer Perceptron model (MLP). MLP is a class of feed forward artificial neural network. This will be discussed further with details in Chapter 3 Next, Bootstrap Artificial Neural Network (BANN). BANN is a hybrid model which will bootstrap ANN model outputs. Those average bootstrap values are taken as the next value for the fitted model. Wavelet Artificial Neural Network (WANN) will decompose the time series data in component which will be obtained using filters. Those components are then fitted into the ANN model, then final fitted WANN model is achieved by adding those components up. And lastly, Wavelet Bootstrap Artificial Neural Network (WBANN) will encompass both the BANN and WANN model.

1.6 Significance of Findings

Findings of this research can forecast gold demand and gold prices using a hybrid Wavelet Bootstrap Artificial Neural Network model. These findings are important as they pave the way for other research opportunities and ideas. Encompassing a limited data set and a large data set, this research is important as the findings of this research may prove that researchers will no longer be restricted with having a large set of data to do forecasting. With the developed model of Wavelet Bootstrap Artificial Neural Network, it shows that the possibilities of research using an ANN model are endless. It may prove that machine learning is a great tool for forecasting.

1.7 Research Framework

This thesis consists of six chapters. The first chapter is the introduction to this research. The background of the problem, scope of study, research objectives as well as the significance of this study are presented in this chapter. Chapter 1 also contains the framework of this research, where the construction of the thesis is explained.

Chapter 2 is the literature review. Past research or study on the topic of gold and time series forecasting are presented in this chapter. An introduction to the history of gold is also present here. The main objective of Chapter 2 is to analyse past studies as well as problems faced by the researchers and methods to overcome them. Methods on forecasting time series are also studied during Chapter 2.

Chapter 3 contains the research methodology of this research. Each method of ANN, Wavelet and Bootstrapping to design the model for forecasting limited length gold demand data as well as large length gold price data is presented in this chapter. Previous studies on each of the methods are also presented in this chapter.

Chapter 4 contains the findings and results obtained by fitting the limited length gold demand data set into the forecasting model of Artificial neural network, Wavelet Artificial Neural Network, Bootstrap Artificial Neural Network and Wavelet Bootstrap Artificial Neural Network. An analysis and a conclusion was made at the end of this chapter.

Chapter 5 replicates the findings of Chapter 4 but with a larger data set, that is the gold price data set. A comparative study between a limited data set forecasting and a large data set forecasting is presented in this chapter as well.

Lastly, Chapter 6 presents the final conclusion of this research. The outcome of the forecasting model for both the limited data set and large data set is presented as well. A summary of the research done and improvements for future researches are also discussed in this chapter.

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