FIRST-PRINCIPLES CALCULATIONS OF STRUCTURAL, ELASTIC, ELECTRONIC AND TRANSPORT PROPERTIES OF VANADIUM-DOPED ZIRCONIUM LEAD CARBIDE MAX PHASE

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DEDICATION

This thesis is dedicated to my wife Mary, Benedict my son and my daughter Esther for their love, prayers, and patience, throughout the Ph.D. journey. They have been a source of inspiration. Remembering my late parents Mr. Bai Summanuwa and Mrs. Kush'da Bai both of blessed memory; may their souls rest in peace with the Lord; their prayers and love have taught me to be sincere and courageous in life. I missed their company and will forever remain indebted to them.

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ABSTRACT

First-principles calculations have been used to systematically investigate the structural, electronic, elastic, thermodynamic, and transport properties of Zr₂PbC MAX phase and its alloys. The V-based alloys $(V_x Zr_{1-x})_2 PbC$, $0 \le x \le 1$ were synthesized by substituting V on the M-site of the MAX phase at a concentration of 0.25, 0.50, 0.75, and 1.00 respectively. Within the density functional theory (DFT), density functional perturbation theory (DFPT), and Boltzmann transport theory, the generalized gradient approximation (GGA: PBE, PBEsol, PW91), the local density approximation (LDA: PZ) exchange-correlation functionals, and the plane-wave pseudopotential method were used. The examined materials crystallized into a hexagonal shape of space group P63/mmc in relaxed and optimized configurations. The calculated electronic bands and density of states show that the studied MAX phases are conductors. The elastic constants show that all studied materials are mechanically stable based on the Born stability criteria for hexagonal crystals, and structurally stable based on the total minimum energy of the relaxed structures. The 100 % replacement of the Zr atoms shows a significant increase in the Seebeck coefficient and the thermoelectric figure of merit of the terminal MAX phase (V₂PbC). Structurally all the studied materials are hard, brittle, and of high directional anisotropy. Calculated properties have been compared with available experimental data and are in good agreement. All four alloys show a significant increase in the electronic, elastic and thermodynamic properties with a decrease in the lattice parameters as the V concentration increases. The terminal alloy V₂PbC has a lower total energy compared to the Zr₂PbC. The transport properties have been calculated in a temperature range of 200 to 800 K by applying GGA (PBE). For the material at 800 K, a rapid decrease in the thermal conductivity with a slow decrease in electrical conductivity leads to an increase in the figure of merit.

ABSTRAK

Pengiraan prinsip pertama telah digunakan untuk menyiasat secara sistematik sifat struktur, elektronik, elastik, termodinamik dan pengangkutan bagi fasa Zr₂PbC MAX dan aloinya. Aloi berasaskan V $(V_x Zr_{1-x})_2 PbC$, $0 \le x \le 1$ telah disintesis dengan menggantikan V pada tapak-M fasa MAX pada kepekatan 0.25, 0.50, 0.75, dan 1.00 masing-masing. Dalam teori fungsian ketumpatan (DFT), teori usikan fungsian ketumpatan (DFPT), dan teori pengangkutan Boltzmann, penghampiran kecerunan umum (GGA: PBE, PBEsol, PW91), penghampiran ketumpatan tempatan (LDA: PZ) fungsian korelasi pertukaran, dan kaedah pseudo-keupayaan gelombang satah telah digunakan. Bahan yang diperiksa menghablur menjadi bentuk heksagon kumpulan ruang P63/mmc dalam konfigurasi santai dan teroptimum. Jalur elektronik yang dikira dan ketumpatan keadaan menunjukkan bahawa fasa MAX yang dikaji adalah konduktor. Pemalar anjal menunjukkan semua bahan yang dikaji adalah stabil secara mekanikal berdasarkan kriteria kestabilan Born untuk kristal heksagon, dan stabil secara struktur berdasarkan jumlah tenaga minimum struktur santai. Penggantian 100% atom Zr menunjukkan peningkatan ketara dalam pekali Seebeck dan angka merit termoelektrik fasa MAX terminal (V₂PbC). Secara struktur semua bahan yang dikaji adalah keras, rapuh, dan anisotropi berarah tinggi dalam arah yang sama. Sifat yang dikira telah dibandingkan dengan data experimen sedia ada dan berada dalam persetujuan yang baik. Keempat-empat aloi menunjukkan peningkatan ketara dalam sifat elektronik, elastik dan termodinamik dengan penurunan dalam parameter kekisi apabila kepekatan V meningkat. Aloi terminal V₂PbC mempunyai jumlah tenaga minimum berbanding dengan Zr₂PbC. Sifat pengangkutan telah dikira dalam julat suhu 200 hingga 800 K dengan menggunakan GGA (PBE). Untuk bahan pada 800 K, penurunan pesat dalam kekonduksian haba dengan penurunan perlahan dalam kekonduksian elektrik membawa kepada peningkatan dalam angka merit.

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LIST OF ABBREVIATIONS

DFT	Density functional theory
GGA	Generalized gradient approximation
LDA	Local density approximation
PBE	Perdew Burke Ernzerhof
ecut	Cut-off kinetic energy
QE	Quantum Espresso
pw	Plane-wave
CB	Conduction band
VB	Valence band
a.m.u.	Atomic mass unit
DFPT	density-functional perturbation theory
K-S	Kohn-Sham
H-K	Hohenberg-Kohn
TDOS	Total density of states
PDOS	Partial density of states
CRTA	Constant Relaxation Time Approximation

LIST OF SYMBOLS

Å	Angstrom
σ_{τ}	Electrical conductivity
τ	Time
σ	Stress tensor
ϵ	Strain tensor
C_{ij}	Elastic constant tensor
ε_0	Ground state energy
ε_{XC}	Exchange correlation energy
eV	Electron volt
Р	Pressure
$S_{ au}$	Seebeck coefficient
\mathcal{E}_{f}	Chemical potential
k_0	Thermal conductivity
k_B	Boltzmann constant
F	Free energy
М	Molecular weight
$N_{ m A}$	Avogadro number
ZT	Figure of merit
BTP2	BoltzTraP2
Ψ	Many electrons wave function
ψ	Single-electron wave function
v	Velocity
Ry	Rydberg
$H_{ m v}$	Vicker's hardness
Γ	Gamma
n	Density
n	Number of atoms
$ heta_{ m D}$	Debye temperature
$C_{\rm v}$	Heat capacity at constant volume
b	Energy bands
S	Entropy
Т	Temperature
K	Kelvin

v_l	Longitudinal sound velocity

- v_t Transverse sound velocity
- v_m Mean sound velocity
- *N*_A Avogadro number

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CHAPTER 1

INTRODUCTION

1.1 Research Background

The growing interest and demand for high-efficiency clean energy sources are critical to developing renewable energy instruments which will alleviate and resolve the energy issue of the world's ever-expanding population [1]–[4] Traditional energy sources are either depleting or endangering the environment [5]–[7]. The majority of materials developed for thermoelectric generators nowadays are bandgap materials, which are prone to wear and tear at high temperatures[8]–[10].

Thermoelectric materials are a kind of new energy material that can directly convert heat energy into electric energy, and vice versa without needing any other energy conversion via the Seebeck effect of solid materials. Improving the thermoelectric performances of existing thermoelectric materials and exploring new thermoelectric materials with excellent performance are eternal research topics in the thermoelectricity field performance of thermoelectric materials can be evaluated by the figure of merit $ZT = (S_{\tau}^2 \sigma_{\tau}/k_{el})T$, where S_{τ} is the Seebeck coefficient, σ_{τ} is the electrical conductivity, k_{el} is the thermal conductivity and T is the temperature [11]. These three parameters for fundamental physical properties of solid are, however, dependent upon each other as a function of the carrier concentration. In particular, S_{τ} and σ_{τ} generally vary reciprocally, making a dramatic improvement in the power factor, $S_{\tau}^2 \sigma_{\tau}$, difficult. Accordingly, semiconducting alloys and compounds with high carrier mobilities have been intensively studied as thermoelectric materials, e.g., Bi₂Te₃[12], PbTe[13], and Si–Ge[14] alloys. A highly covalent character of these materials appears to be responsible for their high mobilities. The efficiency of thermoelectric energy conversion also improves with increasing temperature differences over which the thermoelectric device operates. In recent years, the MAX phases and their derived MXene phases have gradually received the attention of researchers as promising thermoelectric materials due to their unique microstructures and properties [15].

The term MAX phases (also called nanolaminates because of their layered structures, which consist of hexagonal carbide or nitride blocks $M_{n+1}X_n$ refers to ternary nitrides and carbides classified into families of $M_{n+1}AX_n$ (n = 1 to 3) with over 150 different structures that have been widely studied over the last two and a half decades [16]–[25]. They have a layered structure and a distinct set of features bridging the gap between metals and ceramics characteristics [26]–[29]. The group crystallizes to the hexagonal shape of the P6₃/mmc space group, with M representing the early transition d metals like Cr, Hf, Zr, Ta, Nb, Mo, Ti, and V. The A is the p elements from group 12 to16 in the periodic table such as Al, Sn, P, Ge, S, In and Si, while the X is nitrogen (N) and, or carbon (C)[30]–[33].

Due to the metal like characteristics they are categorized as good thermal and electrical conductors, plastically deformable at room temperature, damage tolerant, resistant to thermal shock, and relatively soft whereas as ceramics materials, they are often distinguished by high temperature elastic and mechanical properties, as well as superior corrosion resistance [34]–[38]. They are a new class of materials that have intrigued the academic and commercial interests of many since their reappearance in the 1990s [39], [40]. Several MAX phases, emanating from the integer n = 1 also known as the 211 MAX phases with examples like Zr₂PbC, Cr₂AlC[41], Cr₂GaC, Hf₂InC, Hf₂SC, Mn₂GaC[42], Mo₂GaC, Nb₂AlC, Nb₂AsC[43]–[46], have been synthesized. Others are the 312 MAX phases with n = 2 like Ti₃AlC₂, Ti₃GeC₂, Ti₃SnC₂, Ta₃AlC₂, Ti₃ZnC₂, Zr₃AlC₂, and the 413 MAX phases with n = 3 like Ti₄GaC₃, Ti₄SiC₃, Ti₄GeC₃, Nb₄AlC₃, Ta₄AlC₃[47], (Mo,V)₄AlC₃ are some examples of the various classes of MAX phases to mention just a few that have been synthesized and studied theoretically and experimentally to date[43], [48]–[52].

The well-known potential applications of MAX phase materials include hightemperature applications in the aviation and automobile industries[28] [53], protective and bond-coatings for gas turbines, accident-tolerant fuel cladding in nuclear power plants, solar receivers in concentrated solar power systems, and electrical contacts for catalysis [37], [50], and joining material[28]. The robustness of the compounds to external forces also called their mechanical stability is a property to ensure its sustainability in any application[54]. Stability and hardness are crucial for industrial applications[54], [55].

The pursuit of advanced technologically high-impact qualities, as well as the opportunity to develop materials with new functionalities, has spurred interest in MAX phases formed by substitution or replacement on the M, A, or X sublattices [41], [46], [56]–[62]. The ability to alloy MAX complexes not only helps to improve their properties but also helps to lower the total energy that would otherwise be metastable in their pure condition [63]. There have been quite a number of both theoretical and experimental research aimed at investigating the different ground and elevated state properties like the structural, electronic, thermodynamic, optical, and transport properties of MAX families of compounds [41], [46], [56]–[58].

According to the literature, the majority of studies on bulk Zr₂PbC focus on the effect of pressure and temperature changes on the properties. While several accessible publications on Zr₂PbC and selected literature on similar crystals have explored the effects of substituting different atoms on the M, A, and X sites on the properties of Zr₂PbC and other selected MAX phases [59]–[62], [64]. The majority of the study has concentrated on the structural, electrical, elastic, and thermodynamic properties of the pure and alloy of Zr₂PbC MAX phase. A handful of such works available on the parent Zr₂PbC MAX phase, and the selected literature on similar nanolaminates have, however, studied the effects of substituting different elements like Mn [65], Cr, Mo [66] [19], Ti, V, Mn, Fe, Mo [67] on the M-site; Sn, Bi, Sb[68], Bi[69], and Pb[70] on the A-site., and C, N [46], respectively, on the X site to investigate the properties.

1.2 Problem Statement

The current state of research on thermoelectric materials limits their engineering uses in thermoelectric devices. Discovering novel thermoelectric materials are continual research areas that need closer attention [71]. MAX phases and their MXene phase counterparts have all it takes to be the alternative thermoelectric materials due to their enormous high-temperature adaptability, and structural and mechanical stability. To harness the thermoelectric potentials in MAX phases, relevant substitution elements of the early transition metals like vanadium V on the M site will enhance the thermoelectric figure of merit by maximizing the Seebeck coefficient, electrical conductivity, and minimizing the electronic thermal conductivity to meet the ever-expanding global energy challenges. Several MAX phases, most notably Ti₃SiC₂ [72], [73], Cr₂AlC, Nb₂AlC [74], Ti₃AlC₂ [75], have been found to possess very low Seebeck coefficients[76], [77]. Previous works of literature on Zr₂PbC[24], [78], Ti₂AlC, V₂AlC, Cr₂AlC, and Nb₂AlC [74] [74], and other MAX phases have focussed mostly on the use of different substitution elements on the M, A, and X-site which has raised the hope to investigate the thermoelectric properties of MAX phases.

Therefore, this has motivated expansive research in the past decade toward the development of novel thermoelectric MAX phases. However, despite many recent studies of these MAX phases several of their physical properties like the Seebeck coefficient issue have not been encouraging due to low values [72], [73][74][75]. This work aims at enhancing the electrical, elastic, thermodynamic, and thermoelectric properties of the parent Zr₂PbC MAX phase using V as a replacement element to enhance the Seebeck coefficient, and electrical conductivity and simultaneously lower the electronic thermal conductivity. Understanding these fundamental properties is of great importance for thermoelectric performance and future technological applications.

1.3 Research Objectives

This thesis investigates the properties of the parent Zr₂PbC MAX phase by employing V as the substituting element on the M-site at a concentration of $(V_x Zr_{1-x})_2$ PbC, $0.25 \le x \le 1.00$, using GGA and LDA exchange functionals, respectively. The specific objectives are to:

- (a) Determine the structural, electronic, elastic, and thermoelectric properties of Zr_2PbC MAX phase.
- (b) Evaluate the structural and electronic properties of $(V_x Zr_{1-x})_2 PbC$.
- (c) Compute the elastic properties of $(V_x Zr_{1-x})_2 PbC$
- (d) Calculate the thermoelectric coefficients of $(V_x Zr_{1-x})_2 PbC$ using GGA XC functional within a temperature range of 200 to 800 K.

1.4 Scope of Research

The structural, electronic, elastic, thermodynamic, and transport properties of $(V_x Zr_{1-x})_2 PbC$, $0 \le x \le 1$, MAX phase have been investigated using the density functional theory (DFT)[79] plane-wave method, density functional perturbation theory(DFPT) [80], and Boltzmann transport theory (BTE) [81], [82], respectively. The GGA (PBE, PBEsol, PW91) [83], and LDA(PZ) [84] exchange functionals, respectively have been used to study the structural, electronic, elastic, and thermodynamic properties of the bulk Zr₂PbC, the V-containing MAX phase using an average converged k-mesh of $14 \times 14 \times 14$ and cut-off energy of 500 Ry. While thermoelectric properties: Seebeck, power factor, electrical and thermal conductivities have been calculated using GGA(PBE) using cut-off energy of 500 Ry and a dense k-mesh of $30 \times 30 \times 30$ within a temperature of 200 to 800 K.

1.5 Significance of Study

Thermoelectricity has recently gained recognition due to its capacity to transform waste heat into energy while emitting no toxic toxins. The rebirth of research into thermoelectric materials began in the early 1990s [15]. Thermoelectric materials are environmentally friendly for power generation and refrigeration, thus providing a solution for energy crisis and pollution; however, the thermoelectric conversion efficiency is low and mainly limited by the performance of thermoelectric materials. New concepts and technologies were applied recently to enhance ZT, but accompanied difficulties need to be solved. There is still a long way between high thermoelectric performance and high thermoelectric conversion efficiency. Building a device that could reach the theoretical efficiency is not a trivial pursuit, but a huge development project by itself considering the tremendous practical challenges involved, suitable low resistance hot side, and cold side metal contacts, optimizing assembly of modules, etc. The development of thermoelectric materials and devices needs connected efforts involving physicists, chemists, materials scientists, and theory scientists[11].

This work is an effort to enhance the thermoelectric coefficients and other properties of Zr₂PbC by substituting the Zr atoms with V atoms. research on MAX phases has intrigued the interest of many people and continues to do so due to their unusual hybrid metal/ceramic capabilities coming from their structure and atomic arrangement, and they are being evaluated for several applications[85], [86]. The simplicity with which MAX phases may be machined to high tolerance is also a key factor to consider when designing tools for dry drilling concrete surfaces in civil engineering tasks. This may bring the materials close to the market. Other applications include electrodes, free-cutting elements[26], exhaust gas filters for automobiles, corrosion-resistant materials, surface coatings materials, and microelectronics[87].

REFERENCES

- A. Jain *et al.*, "Commentary: The materials project: A materials genome approach to accelerating materials innovation," *APL Mater.*, vol. 1, no. 1, 2013, doi: 10.1063/1.4812323.
- [2] H. J. Goldsmid, Optimisation and selection of semiconductor thermoelements, vol. 121. 2016.
- [3] D. J. Singh, "Thermopower of SnTe from Boltzmann transport calculations," *Funct. Mater. Lett.*, vol. 3, no. 4, pp. 223–226, 2010, doi: 10.1142/S1793604710001299.
- [4] D. Li *et al.*, "Recent Progress of Two-Dimensional Thermoelectric Materials," *Nano-Micro Lett.*, vol. 12, no. 1, p. 36, Dec. 2020, doi: 10.1007/s40820-020-0374-x.
- [5] S. Ahmad, R. Ahmad, M. Bilal, and N. U. Rehman, "DFT studies of thermoelectric properties of R–Au intermetallics at 300 K," *J. Rare Earths*, vol. 36, no. 2, pp. 197–202, 2018, doi: 10.1016/j.jre.2017.08.004.
- [6] A. Gaul and T. Advisor, "A Theoretical Study of Enhancing Thermoelectric Efficiency in Pnictogen-Chalcogen Alloys via Doping, Strain, and Nanostructuring," Rensselaer Polytechnic Institute Troy, New York March, 2018.
- M. Ohtaki, T. Tsubota, K. Eguchi, and H. Arai, "High-temperature thermoelectric properties of (Zn_{1-x}Al_x)O," *J. Appl. Phys.*, vol. 79, no. 3, pp. 1816–1818, 1996, doi: 10.1063/1.360976.
- [8] H. Salehi, P. Amiri, and R. Z. Hasanabad, "Ab-initio Study of Electronic, Optical, Dynamic and Thermoelectric Properties of CuSbX₂(X = S, Se) Compounds," vol. 3, no. 2, 2018.
- [9] M. Hammi, O. El Rhazouani, M. Arejdal, and A. Slassi, "Ab initio study of semi-classic transport coefficients of SnO₂ thermoelectric material," *Chinese J. Phys.*, vol. 55, no. 1, pp. 187–194, 2017, doi: 10.1016/j.cjph.2016.10.016.
- S. D. Guo, "Thermoelectric properties of half-Heusler ZrNiPb by using first principles calculations," *RSC Adv.*, vol. 6, no. 53, pp. 47953–47958, 2016, doi: 10.1039/c6ra08461c.

- [11] X. Zhang and L. Zhao, "Thermoelectric materials: Energy conversion between heat and electricity," *J. Mater.*, vol. 1, no. 2, pp. 92–105, Jun. 2015, doi: 10.1016/j.jmat.2015.01.001.
- [12] M. Scheele, N. Oeschler, K. Meier, A. Kornowski, C. Klinke, and H. Weller, "Synthesis and thermoelectric characterization of Bi₂Te₃ nanoparticles," *Adv. Funct. Mater.*, vol. 19, no. 21, pp. 3476–3483, 2009, doi: 10.1002/adfm.200901261.
- [13] Y. Pei, A. Lalonde, S. Iwanaga, and G. J. Snyder, "High thermoelectric figure of merit in heavy hole dominated PbTe," *Energy Environ. Sci.*, vol. 4, no. 6, pp. 2085–2089, 2011, doi: 10.1039/c0ee00456a.
- [14] Y. Shiraki and N. Usami, *Silicon germanium nanostructures*. Woodhead Publishing Limited, 2011.
- [15] J. Mao, Z. Liu, and Z. Ren, "Size effect in thermoelectric materials," *npj Quantum Mater.*, vol. 1, no. November, pp. 1–9, 2016, doi: 10.1038/npjquantmats.2016.28.
- [16] M. W. Barsoum *et al.*, "Thermal properties of Ti₃SiC₂," *J. Phys. Chem. Solids*, vol. 60, pp. 429–439, 1999.
- [17] X. He, Y. Bai, Y. Li, C. Zhu, and M. Li, "Ab initio calculations for properties of MAX phases Ti₂InC, Zr₂InC, and Hf₂InC," vol. 149, pp. 564–566, 2009, doi: 10.1016/j.ssc.2008.12.047.
- [18] Z. J. Lin, M. J. Zhuo, Y. C. Zhou, M. S. Li, and J. Y. Wang, "Structural characterization of a new layered-ternary Ta₄AlC₃ ceramic," *J. Mater. Res.*, vol. 21, no. 10, pp. 2587–2592, 2006, doi: 10.1557/jmr.2006.0310.
- P. A. Burr, D. Horlait, and W. E. Lee, "Experimental and DFT investigation of (Cr,Ti)₃AlC₂ MAX phases stability," *Mater. Res. Lett.*, vol. 5, no. 3, pp. 144– 157, May 2017, doi: 10.1080/21663831.2016.1222598.
- [20] X. K. Qian, X. D. He, Y. B. Li, Y. Sun, H. Li, and D. L. Xu, "Cyclic oxidation of Ti₃AlC₂ at 1000 – 1300 ° C in air," vol. 53, pp. 290–295, 2011, doi: 10.1016/j.corsci.2010.09.033.
- [21] F. Sultana, M. M. Uddin, M. A. Ali, M. M. Hossain, S. H. Naqib, and A. K. M. A. Islam, "First principles study of M₂InC (M = Zr, Hf and Ta) MAX phases: The effect of M atomic species," *Results Phys.*, vol. 11, no. May, pp. 869–876, 2018, doi: 10.1016/j.rinp.2018.10.044.
- [22] W. J. Chen et al., "Experimental realization of photonic topological insulator

in a uniaxial metacrystal waveguide," *Nat. Commun.*, vol. 5, pp. 1–8, 2014, doi: 10.1038/ncomms6782.

- [23] W. Jeitschko and H. Nowotny, "Die Kristallstruktur yon Ti₃SiC₂ ein neuer Komplexearbid-Typ," *Monatshefte für Chemie - Chem. Mon.*, vol. 98, no. 2, pp. 329–337, Mar. 1967, doi: 10.1007/BF00899949.
- [24] W. Jeitschko, H. Nowotny, and F. Benesovsky, "Ti₂A1N, eine stickstoffhaltige H-Phase," *Monatshefte für Chemie*, vol. 94, no. 6, pp. 1198– 1200, 1963, doi: 10.1007/BF00905710.
- [25] P. Eklund, M. Beckers, U. Jansson, H. Högberg, and L. Hultman, "The M_{n+1}AX_n phases: Materials science and thin-film processing," *Thin Solid Films*, vol. 518, no. 8, pp. 1851–1878, Feb. 2010, doi: 10.1016/j.tsf.2009.07.184.
- [26] R. Arróyave, A. Talapatra, T. Duong, W. Son, and M. Radovic, "Out-of-plane ordering in quaternary MAX alloys: an alloy theoretic perspective," *Mater. Res. Lett.*, vol. 6, no. 1, pp. 1–12, Jan. 2018, doi: 10.1080/21663831.2017.1380723.
- [27] W. Yu *et al.*, "Solid solution effects in the Ti₂Al(C_xN_y) MAX phases: Synthesis, microstructure, electronic structure and transport properties," *Acta Mater.*, vol. 80, pp. 421–434, Nov. 2014, doi: 10.1016/j.actamat.2014.07.064.
- [28] J. Gonzalez-Julian, "Processing of MAX phases: From synthesis to applications," *Journal of the American Ceramic Society*, vol. 104, no. 2. pp. 659–690, 2021, doi: 10.1111/jace.17544.
- [29] P. Eklund, J. Rosen, and P. O. Å. Persson, "Layered ternary M_{n+1}AX_n phases and their 2D derivative MXene: An overview from a thin-film perspective," *J. Phys. D. Appl. Phys.*, vol. 50, no. 11, 2017, doi: 10.1088/1361-6463/aa57bc.
- [30] Y. Bai, N. Srikanth, C. K. Chua, and K. Zhou, "Density Functional Theory Study of Mn + 1AXn Phases : A Review Density Functional Theory Study of M n + 1 AX n Phases : A Review," *Crit. Rev. Solid State Mater. Sci.*, vol. 0, no. 0, pp. 1–52, 2019, doi: 10.1080/10408436.2017.1370577.
- [31] A. S. Ingason *et al.*, "A Nanolaminated Magnetic Phase: Mn₂GaC," *Mater. Res. Lett.*, vol. 2, no. 2, pp. 89–93, Apr. 2014, doi: 10.1080/21663831.2013.865105.
- [32] P. Eklund, J. Rosen, and P. O. Å. Persson, "Layered ternary M_{n+1}AX_n phases and their 2D derivative MXene: an overview from a thin-film perspective," J.

Phys. D. Appl. Phys., vol. 50, no. 11, p. 113001, Mar. 2017, doi: 10.1088/1361-6463/aa57bc.

- [33] R. Khatun, M. A. Rahman, K. M. Hossain, M. Z. Hasan, M. Rasheduzzaman, and S. Sarker, "Physical properties of MAX phase Zr₂PbC under pressure: Investigation via DFT scheme," *Phys. B Condens. Matter*, vol. 620, no. July, p. 413258, Nov. 2021, doi: 10.1016/j.physb.2021.413258.
- [34] I. Zhirkov, L. Landälv, E. Göthelid, M. Ahlgren, P. Eklund, and J. Rosen, "Effect of Si on DC arc plasma generation from Al-Cr and Al-Cr-Si cathodes used in oxygen," J. Appl. Phys., vol. 121, no. 8, 2017, doi: 10.1063/1.4976862.
- [35] M. W. Barsoum, "The M_{n+1}AX_n phases: A new class of solids," *Prog. Solid State Chem.*, vol. 28, no. 1–4, pp. 201–281, Jan. 2000, doi: 10.1016/S0079-6786(00)00006-6.
- [36] T. El-Raghy, M. W. Barsoum, A. Zavaliangos, and S. R. Kalidindi, "Processing and mechanical properties of Ti₃SiC₂: II, Effect of grain size and deformation temperature," *J. Am. Ceram. Soc.*, vol. 82, no. 10, pp. 2855–2860, 1999, doi: 10.1111/j.1151-2916.1999.tb02167.x.
- [37] W. H. K. Ng *et al.*, "The Ti₃AlC₂ MAX Phase as an Efficient Catalyst for Oxidative Dehydrogenation of n-Butane," pp. 1–7, 2018, doi: 10.1002/anie.201702196.
- [38] M. Yoshida, Y. Hoshiyama, J. Ommyoji, and A. Yamaguchi, "Reaction mechanism for the synthesis of Ti₃AlC₂ through an intermediate carbide of Ti₃AlC from elemental Ti, Al, andC powder mixture," *J. Ceram. Soc. Japan*, vol. 118, no. 1373, pp. 37–42, 2010, doi: 10.2109/jcersj2.118.37.
- [39] M. Barsoum, "The MAX Phases: Unique New Carbide and Nitride Materials," no. November, 2001, doi: 10.1511/2001.28.736.
- [40] J. Wang and Y. Zhou, "Recent Progress in Theoretical Prediction, Preparation, and Characterization of Layered Ternary Transition-Metal Carbides," *Annu. Rev. Mater. Res.*, vol. 39, no. 1, pp. 415–443, Aug. 2009, doi: 10.1146/annurev-matsci-082908-145340.
- [41] J. C. Schuster, H. Nowotny, and C. Vaccaro, "The ternary systems: CrAlC, VAIC, and TiAlC and the behavior of H-phases (M₂AlC)," *J. Solid State Chem.*, vol. 32, no. 2, pp. 213–219, Apr. 1980, doi: 10.1016/0022-4596(80)90569-1.

- [42] A. S. Ingason *et al.*, "A Nanolaminated Magnetic Phase : Mn₂GaC," vol. 3831, 2014, doi: 10.1080/21663831.2013.865105.
- [43] C. Anirudh, V. K. A. V, and U. N. Kempaiah, "Max Phase Materials- Review of an Exciting Class of Ternary Carbides and Nitrides," *Int. J. Emerg. Tech. Adv. Eng.*, vol. 4, no. 8, pp. 624–630, 2014, [Online]. Available: www.ijetae.com.
- [44] V. A. Gorshkov, A. V. Karpov, D. Y. Kovalev, and A. E. Sychev, "Synthesis, Structure and Properties of Material Based on V₂AlC MAX Phase," *Phys. Met. Metallogr.*, vol. 121, no. 8, pp. 765–771, 2020, doi: 10.1134/S0031918X20080037.
- [45] B. Velasco, E. Gordo, L. Hu, M. Radovic, and S. A. Tsipas, "Influence of porosity on elastic properties of Ti₂AlC and Ti3SiC2 MAX phase foams," *J. Alloys Compd.*, vol. 764, pp. 24–35, Oct. 2018, doi: 10.1016/j.jallcom.2018.06.027.
- [46] M. W. Barsoum, M. Ali, and T. El-Raghy, "Processing and characterization of Ti₂AlC, Ti₂AlN, and Ti₂AlC_{0.5}N_{0.5}," *Metall. Mater. Trans. A Phys. Metall. Mater. Sci.*, vol. 31, no. 7, pp. 1857–1865, 2000, doi: 10.1007/s11661-006-0243-3.
- [47] B. Manoun, S. K. Saxena, T. El-Raghy, and M. W. Barsoum, "High-pressure x-ray diffraction study of Ta₄AlC₃," *Appl. Phys. Lett.*, vol. 88, no. 20, pp. 2004–2007, 2006, doi: 10.1063/1.2202387.
- [48] B. Anasori *et al.*, "Experimental and theoretical characterization of ordered MAX phases Mo₂TiAlC₂and Mo₂Ti₂AlC₃," *J. Appl. Phys.*, vol. 118, no. 9, p. 094304, 2015, doi: 10.1063/1.4929640.
- [49] L. J. Liu, L. Lian, and J. Yu, "Stability, mechanical properties and anisotropic elastic properties of Ga_xMg_y compounds," *Mater. Res.*, vol. 22, no. 2, pp. 1– 11, 2019, doi: 10.1590/1980-5373-MR-2018-0624.
- [50] M. Atikur Rahman, "Study on Structural, Electronic, Optical and Mechanical Properties of MAX Phase Compounds and Applications Review Article," *Am. J. Mod. Phys.*, vol. 4, no. 2, p. 75, 2015, doi: 10.11648/j.ajmp.20150402.15.
- [51] M. Dahlqvist, J. Lu, R. Meshkian, Q. Tao, L. Hultman, and J. Rosen, "Prediction and synthesis of a family of atomic laminate phases with Kagomélike and in-plane chemical ordering," *Science Advances*, vol. 3, no. 7. 2017, doi: 10.1126/sciadv.1700642.

- [52] A. S. Ingason *et al.*, "Magnetic MAX phases from theory and experiments; a review," vol. 28, no. 43, 2016.
- [53] Z. M. Sun, "Progress in research and development on MAX phases: A family of layered ternary compounds," *Int. Mater. Rev.*, vol. 56, no. 3, pp. 143–166, 2011, doi: 10.1179/1743280410Y.0000000001.
- [54] G. Surucu, "Investigation of structural, electronic, anisotropic elastic, and lattice dynamical properties of MAX phases borides: An Ab-initio study on hypothetical M₂AB (M = Ti, Zr, Hf; A = Al, Ga, In) compounds," *Mater. Chem. Phys.*, vol. 203, pp. 106–117, 2018, doi: 10.1016/j.matchemphys.2017.09.050.
- [55] A. Gencer and G. Surucu, "Electronic and Lattice Dynamical Properties of Ti₂SiB MAX Phase," no. July, 2018.
- [56] M. W. Barsoum et al., "Thermal and electrical properties of Nb₂AlC,(Ti,Nb)₂AlC and Ti₂AlC," Metall. Mater. Trans. A Phys. Metall. Mater. Sci., vol. 33, no. 9, pp. 2775–2779, 2002, doi: 10.1007/s11661-002-0262-7.
- [57] B. Manoun, S. K. Saxena, G. Hug, A. Ganguly, E. N. Hoffman, and M. W. Barsoum, "Synthesis and compressibility of Ti₃(Al,Sn_{0.2})C₂ and Ti₃Al(C_{0.5},N_{0.5})₂," *J. Appl. Phys.*, vol. 101, no. 11, pp. 0–7, 2007, doi: 10.1063/1.2733644.
- [58] H. Yang, B. Manoun, R. T. Downs, A. Ganguly, and M. W. Barsoum, "Crystal chemistry of layered carbide, Ti₃(Si_{0.43}Ge_{0.57})C₂ Hexiong," *J. Phys. Chem. Solids*, vol. 67, no. 12, pp. 2512–2516, 2006, doi: 10.1016/j.jpcs.2006.07.009.
- [59] M. Atikur Rahman, "Study on Structural, Electronic, Optical and Mechanical Properties of MAX Phase Compounds and Applications Review Article," *Am. J. Mod. Phys.*, vol. 4, no. 2, p. 75, 2015, doi: 10.11648/j.ajmp.20150402.15.
- [60] R. Khatun, "Structural, elastic, electronic, optical and thermodynamic properties of MAX phase compound Zr₂PbC under pressure: DFT based investigation," vol. 6, no. April, 2020.
- [61] X. Qian *et al.*, "First-principle studies of properties of ternary layered M₂PbC (M=Ti, Zr and Hf)," *Comput. Mater. Sci.*, vol. 65, pp. 377–382, Dec. 2012, doi: 10.1016/j.commatsci.2012.08.004.
- [62] M. B. Kanoun, S. Goumri-Said, A. H. Reshak, and A. E. Merad, "Electro-

structural correlations, elastic and optical properties among the nanolaminated ternary carbides Zr₂AC," *Solid State Sci.*, vol. 12, no. 5, pp. 887–898, 2010, doi: 10.1016/j.solidstatesciences.2010.01.035.

- [63] D. Horlait, S. Grasso, A. Chroneos, and W. E. Lee, "Attempts to synthesise quaternary MAX phases (Zr,M)₂AlC and Zr₂(AL,A)C as a way to approach Zr₂AlC," *Mater. Res. Lett.*, vol. 4, no. 3, pp. 137–144, 2016, doi: 10.1080/21663831.2016.1143053.
- [64] T. El-Raghy, S. Chakraborty, and M. Barsoum, "Synthesis and characterization of Hf₂PbC, Zr₂PbC and M₂SnC (M=Ti, Hf, Nb or Zr)," *J. Eur. Ceram. Soc.*, vol. 20, no. 14–15, pp. 2619–2625, Dec. 2000, doi: 10.1016/S0955-2219(00)00127-8.
- [65] C. M. Hamm *et al.*, "Structural, magnetic and electrical transport properties of non-conventionally prepared MAX phases V₂AlC and (V/Mn)₂AlC," *Mater. Chem. Front.*, vol. 2, no. 3, pp. 483–490, 2018, doi: 10.1039/c7qm00488e.
- [66] Y. F. Li, Y. C. Ding, B. Xiao, and Y. H. Cheng, "Anisotropic electrical and lattice transport properties of ordered quaternary phases Cr₂TiAlC₂ and Mo₂TiAlC₂: A first principles study," *Phys. Lett. Sect. A Gen. At. Solid State Phys.*, vol. 380, no. 44, pp. 3748–3755, 2016, doi: 10.1016/j.physleta.2016.09.015.
- [67] S. Lin *et al.*, "Alloying effects on structural, magnetic, and electrical/thermal transport properties in MAX-phase Cr_{2-x}M_xGeC (M = Ti, V, Mn, Fe, and Mo)," *J. Alloys Compd.*, vol. 680, pp. 452–461, 2016, doi: 10.1016/j.jallcom.2016.04.197.
- [68] M. A. Ali, M. M. Hossain, N. Jahan, A. K. M. A. Islam, and S. H. Naqib, "Newly synthesized Zr₂AlC, Zr₂(Al_{0.58}Bi_{0.42})C, Zr₂(Al_{0.2}Sn_{0.8})C, and Zr₂(Al_{0.3}Sb_{0.7})C MAX phases: A DFT based first-principles study," *Comput. Mater. Sci.*, vol. 131, pp. 139–145, Apr. 2017, doi: 10.1016/j.commatsci.2017.01.048.
- [69] D. Horlait, S. C. Middleburgh, A. Chroneos, and W. E. Lee, "Synthesis and DFT investigation of new bismuth-containing MAX phases," *Nat. Publ. Gr.*, no. January, pp. 1–9, 2016, doi: 10.1038/srep18829.
- [70] D. Horlait *et al.*, "Attempts to synthesise quaternary MAX phases (Zr,M)₂AlC and Zr₂(Al,A)C as a way to approach Zr₂AlC," vol. 3831, 2016, doi: 10.1080/21663831.2016.1143053.

- [71] C. Liu, Y.-Y. Yang, C.-W. Nan, and Y.-H. Lin, "Thermoelectric properties and prospects of MAX phases and derived MXene phases," *Acta Phys. Sin.*, vol. 70, no. 20, p. 206501, 2021, doi: 10.7498/aps.70.20211050.
- [72] M. Magnuson, M. Mattesini, N. Van Nong, P. Eklund, and L. Hultman, "The electronic-structure origin of the anisotropic thermopower of nanolaminated Ti₃SiC₂ determined by polarized x-ray spectroscopy and Seebeck measurements," vol. 195134, pp. 1–13, 2012.
- [73] M. Magnuson, M. Mattesini, N. Van Nong, P. Eklund, and L. Hultman, "Electronic-structure origin of the anisotropic thermopower of nanolaminated Ti₃SiC₂ determined by polarized x-ray spectroscopy and Seebeck measurements," vol. 195134, pp. 1–8, 2012, doi: 10.1103/PhysRevB.85.195134.
- [74] J. D. Hettinger *et al.*, "Electrical transport, thermal transport, and elastic properties of M₂AlC (M=Ti, Cr, Nb, and V)," no. May 2014, pp. 2–7, 2005, doi: 10.1103/PhysRevB.72.115120.
- [75] T. Scabarozi *et al.*, "Electronic and thermal properties of Ti₃Al(C_{0.5},N_{0.5})₂, Ti₂Al(C_{0.5},N_{0.5}) and Ti₂AlN," *J. Appl. Phys.*, vol. 104, no. 7, pp. 1–7, 2008, doi: 10.1063/1.2979326.
- [76] M. W. Barsoum, "Physical Properties of the MAX Phases," *Encycl. Mater. Sci. Technol.*, no. Table 1, pp. 1–11, 2006, doi: 10.1016/b0-08-043152-6/02058-1.
- [77] B. M. Radovic and M. W. Barsoum, "MAX phases : Bridging the gap between metals and ceramics," *Am. Ceram. Soc. Bull.*, vol. 92, no. 3, pp. 20–27, 2012, [Online]. Available: www.ceramics.org.
- [78] W. Jeitschko, H. Nowotny, and F. Benesovsky, "Carbides of formula T₂MC,"
 J. Less-Common Met., vol. 7, no. 2, pp. 133–138, 1964, doi: 10.1016/0022-5088(64)90055-4.
- [79] W. Son, T. Duong, A. Talapatra, H. Gao, R. Arróyave, and M. Radovic, "Abinitio investigation of the finite-temperatures structural, elastic, and thermodynamic properties of Ti₃AlC₂ and Ti₃SiC₂," *Comput. Mater. Sci.*, vol. 124, pp. 420–427, 2016, doi: 10.1016/j.commatsci.2016.08.015.
- [80] A. Champagne *et al.*, "Phonon dispersion curves in Cr₂AlC single-crystals," *Mater. Res. Lett.*, vol. 6, no. 7, pp. 378–383, Jul. 2018, doi: 10.1080/21663831.2018.1463298.

- [81] G. K. H. Madsen, J. Carrete, and M. J. Verstraete, "BoltzTraP2, a program for interpolating band structures and calculating semi-classical transport coefficients," *Comput. Phys. Commun.*, vol. 231, pp. 140–145, 2018, doi: 10.1016/j.cpc.2018.05.010.
- [82] G. K. H. Madsen and D. J. Singh, "BoltzTraP. A code for calculating bandstructure dependent quantities," *Comput. Phys. Commun.*, vol. 175, no. 1, pp. 67–71, 2006, doi: 10.1016/j.cpc.2006.03.007.
- [83] J. P. Perdew, K. Burke, and M. Ernzerhof, "Generalized Gradient Approximation Made Simple," *Phys. Rev. Lett.*, vol. 77, no. 18, pp. 3865– 3868, Oct. 1996, doi: 10.1103/PhysRevLett.77.3865.
- [84] V. I. Anisimov, F. Aryasetiawan, and A. I. Lichtenstein, "First-principles calculations of the electronic structure and spectra of strongly correlated systems: The LDA + U method," *J. Phys. Condens. Matter*, vol. 9, no. 4, pp. 767–808, 1997, doi: 10.1088/0953-8984/9/4/002.
- [85] P. Eklund, M. Beckers, U. Jansson, H. Högberg, and L. Hultman, "Linköping University Post Print The M_{n+1}AX_n phases : Materials science and thin-film processing," *Mater. Sci. thin-film Process.*, no. 518, pp. 1851–1878, 2010, doi: 10.1016/j.tsf.2009.07.184.
- [86] M. W. Barsoum and M. Radovic, "Elastic and Mechanical Properties of the MAX Phases," Annu. Rev. Mater. Res., vol. 41, no. 1, pp. 195–227, 2011, doi: 10.1146/annurev-matsci-062910-100448.
- [87] M. N. Abdelmalak, "A New Family of Two-Dimensional Materials and its Application as Electrodes for Li-ion Batteries," *Thesis*, no. April, 2014.
- [88] M. Zhang, W. Tian, P. Zhang, J. Ding, Y. Zhang, and Z. Sun, "Microstructure and properties of Ag – Ti₃SiC₂ contact materials prepared by pressureless sintering," *Int. J. Miner. Metall. Mater.*, vol. 25, no. 7, pp. 810–816, 2018.
- [89] Y. Hadji *et al.*, "Microstructure and microindentation of Ti₃SiC₂ Titanium filler brazed joints by tungsten inert gas (TIG) process," *Ceram. Int.*, vol. 43, no. 9, pp. 7290–7294, 2017, doi: 10.1016/j.ceramint.2017.03.028.
- [90] C. Xu *et al.*, "First-principles calculations of Ti₃SiC₂ and Ti₃AlC₂ with hydrogen interstitial," *J. Nucl. Mater.*, vol. 488, pp. 261–266, 2017, doi: 10.1016/j.jnucmat.2016.09.025.
- [91] A. S. Ingason, M. Dahlqvist, and J. Rosen, "Magnetic MAX phases from theory and experiments; A review," *J. Phys. Condens. Matter*, vol. 28, no. 43,

2016, doi: 10.1088/0953-8984/28/43/433003.

- [92] C. Dhakal, S. Aryal, R. Sakidja, and W. Y. Ching, "Approximate lattice thermal conductivity of MAX phases at high temperature," *J. Eur. Ceram. Soc.*, vol. 35, no. 12, pp. 3203–3212, 2015, doi: 10.1016/j.jeurceramsoc.2015.04.013.
- [93] K. Lambrinou, T. Lapauw, and J. Vleugels, "Exploring the Potential of MAX Phases for Select Applications in Extreme Environments," pp. 1–32, 2015.
- [94] D. J. Tallman, "On the Potential of MAX phases for Nuclear Applications," no. June, 2015.
- [95] W. H. K. Ng *et al.*, "The Ti₃AlC₂ MAX Phase as an Efficient Catalyst for Oxidative Dehydrogenation of n-Butane," *Angew. Chemie - Int. Ed.*, vol. 57, no. 6, pp. 1485–1490, 2018, doi: 10.1002/anie.201702196.
- [96] A. S. Ingason *et al.*, "A nanolaminated magnetic phase: Mn₂GaC," *Mater. Res. Lett.*, vol. 2, no. 2, pp. 89–93, 2017, doi: 10.1080/21663831.2013.865105.
- [97] I. Persson *et al.*, "On the organization and thermal behavior of functional groups on Ti₃C₂ MXene surfaces in vacuum," 2D Mater., 2017, doi: 10.1088/2053-1583/aa89cd.
- [98] M. Khazaei *et al.*, "Novel Electronic and Magnetic Properties of Two-Dimensional Transition Metal Carbides and Nitrides," pp. 2185–2192, 2013, doi: 10.1002/adfm.201202502.
- [99] M. Atikur Rahman, "Study on Structural, Electronic, Optical and Mechanical Properties of MAX Phase Compounds and Applications Review Article," *American Journal of Modern Physics*, vol. 4, no. 2. p. 75, 2015, doi: 10.11648/j.ajmp.20150402.15.
- [100] V. Gray, E. H. Kisi, O. Kirstein, and A. P. J. Stamp, "Elastic constants of polycrystalline Ti₃AlC₂ and Ti₃SiC₂ measured using coherent inelastic neutron scattering," no. September, pp. 705–712, 2016, doi: 10.1111/jace.14600.
- [101] M. K. Drulis, H. Drulis, S. Gupta, M. W. Barsoum, M. K. Drulis, and H. Drulis, "On the heat capacities of M_2AlC (M = Ti, V, Cr) ternary carbides," vol. 093502, 2006, doi: 10.1063/1.2191744.
- [102] L. Chaput, G. Hug, P. Pécheur, and H. Scherrer, "Anisotropy and thermopower in Ti₃SiC₂," *Phys. Rev. B Condens. Matter Mater. Phys.*, vol. 71, no. 12, pp. 2–4, 2005, doi: 10.1103/PhysRevB.71.121104.

- [103] S. Fukada-tanaka and Y. Inagaki, "Colour-enhancing protein in blue petals," vol. 407, no. October, pp. 581–582, 2000.
- [104] Y. Zhao, S. Deng, H. Liu, J. Zhang, Z. Guo, and H. Hou, "First-principle investigation of pressure and temperature in fl uence on structural, mechanical and thermodynamic properties of Ti₃AC₂ (A = Al and," *Comput. Mater. Sci.*, vol. 154, no. July, pp. 365–370, 2018, doi: 10.1016/j.commatsci.2018.07.007.
- [105] M. A. Ali and M. W. Qureshi, "Newly synthesized MAX phase Zr₂SeC: DFT insights into physical properties towards possible applications," *RSC Adv.*, vol. 11, no. 28, pp. 16892–16905, 2021, doi: 10.1039/D1RA02345D.
- [106] M. W. Barsoum, T. H. Scabarozi, S. Amini, J. D. Hettinger, and S. E. Lofland,
 "Electrical and thermal properties of Cr₂GeC," *J. Am. Ceram. Soc.*, vol. 94,
 no. 12, pp. 4123–4126, 2011, doi: 10.1111/j.1551-2916.2011.04886.x.
- [107] S. Lin *et al.*, "Magnetic and electrical/thermal transport properties of Mndoped M_{n+1}AX_n phase compounds Cr_{2−x}Mn_x GaC (0 ≤ x ≤ 1)," *J. Appl. Phys.*, vol. 113, no. 5, p. 053502, Feb. 2013, doi: 10.1063/1.4789954.
- [108] S. Aryal, R. Sakidja, M. W. Barsoum, and W. Y. Ching, "A genomic approach to the stability, elastic, and electronic properties of the MAX phases," *Phys. Status Solidi Basic Res.*, vol. 251, no. 8, pp. 1480–1497, 2014, doi: 10.1002/pssb.201451226.
- [109] O. Kirstein, J. F. Zhang, E. H. Kisi, D. P. Riley, M. J. Styles, and A. Paradowska, "Single crystal elastic constants of the MAX phase Ti₃AlC₂ determined by neutron diffraction," *Mater. Sci. Forum*, vol. 638–642, pp. 2417–2422, 2010, doi: 10.4028/www.scientific.net/MSF.638-642.2417.
- [110] Veronica Gray *et al.*, "Mn+1AXn Phonon Density of States: Ti₃AlC₂ and Ti₃SiC₂ Simulation and Experimentation Results," *J. Chem. Chem. Eng.*, vol. 9, no. 4, 2015, doi: 10.17265/1934-7375/2015.04.003.
- [111] H. Wang *et al.*, "First-principles study of vacancies in Ti₃SiC₂and Ti₃AlC₂," *Materials (Basel).*, vol. 10, no. 2, 2017, doi: 10.3390/ma10020103.
- [112] H. Wang, Z. Song, D. Qiao, D. Feng, and J. Lu, "Tribological Behavior of Si₃N₄ / Ti₃SiC₂ Contacts Lubricated by Lithium-Based Ionic Liquids," vol. 2014, 2014.
- [113] A. G. Zhou and M. W. Barsoum, "Kinking nonlinear elastic deformation of Ti₃AlC₂, Ti₂AlC, Ti₃Al(C_{0.5},N_{0.5})₂ and Ti₂Al(C_{0.5},N_{0.5})," J. Alloys Compd., vol.

498, no. 1, pp. 62–70, 2010, doi: 10.1016/j.jallcom.2010.03.099.

- [114] K. Wang, Y. Zhou, C. Yu, M. Xiang, D. Huang, and W. Xu, "Synthesis and strengthening of Ti₃AlC₂," *J. Alloys Compd.*, vol. 654, pp. 120–125, 2016, doi: 10.1016/j.jallcom.2015.09.091.
- [115] K. R. Whittle, M. G. Blackford, R. D. Aughterson, S. Moricca, and G. R. Lumpkin, "Radiation tolerance of M_{n+1}AX_n phases, Ti₃AlC₂ and Ti₃SiC₂," vol. 58, pp. 4362–4368, 2010, doi: 10.1016/j.actamat.2010.04.029.
- [116] J. C. Schuster, H. Nowotny, and C. Vaccaro, "The ternary systems: Cr–Al–C, V–Al–C, and Ti–Al–C and the behavior of H-phases (M₂AlC)," *J. Solid State Chem.*, vol. 32, no. 2, pp. 213–219, 1980, doi: 10.1016/0022-4596(80)90569-1.
- [117] A. Azzouz-Rached, H. Rached, I. Ouadha, D. Rached, and A. Reggad, "The Vanadium-doping effect on physical properties of the Zr₂AlC MAX phase compound," *Mater. Chem. Phys.*, vol. 260, no. September 2020, p. 124189, 2021, doi: 10.1016/j.matchemphys.2020.124189.
- [118] F. L. Meng, Y. C. Zhou, and J. Y. Wang, "Strengthening of Ti₂AlC by substituting Ti with V," *Scr. Mater.*, vol. 53, no. 12, pp. 1369–1372, 2005, doi: 10.1016/j.scriptamat.2005.08.030.
- [119] S. Jin, T. Su, Q. Hu, and A. Zhou, "Thermal conductivity and electrical transport properties of double-A-layer MAX phase Mo₂Ga₂C," *Mater. Res. Lett.*, vol. 8, no. 4, pp. 158–164, 2020, doi: 10.1080/21663831.2020.1724204.
- [120] M. W. Barsoum, H. Yoo, I. K. Polushina, V. Y. Rud, and Y. V Rud, "The phases with the general formula M," *Phys. Rev. B*, vol. 62, no. 15, pp. 194– 198, 2000.
- [121] X. Li, H. Cui, and R. Zhang, "Structural, optical, and thermal properties of MAX-phase Cr₂AlB₂," vol. 13, no. 2, pp. 1–9, 2018.
- [122] H. Mebtouche *et al.*, "First-principles calculations of the structural, electronic, mechanical and thermodynamic properties of MAX phase Mo_{n+1}GeC_n (n = 1–3) compounds," *Mater. Today Commun.*, vol. 25, no. July, p. 101420, 2020, doi: 10.1016/j.mtcomm.2020.101420.
- [123] G. Surucu, K. Colakoglu, E. Deligoz, and N. Korozlu, "First-Principles Study on the MAX Phases $Ti_{n+1}GaN_n$ (n = 1, 2, and 3)," 2016, doi: 10.1007/s11664-016-4607-1.
- [124] A. Gencer and G. Surucu, "Electronic and lattice dynamical properties of

Ti₂SiB MAX phase," *Mater. Res. Express*, vol. 5, no. 7, 2018, doi: 10.1088/2053-1591/aace7f.

- [125] T. H. Scabarozi *et al.*, "Electrical, thermal, and elastic properties of the MAXphase Ti₂SC," *J. Appl. Phys.*, vol. 104, no. 3, pp. 1–6, 2008, doi: 10.1063/1.2959738.
- [126] J. D. Hettinger, S. E. Lofland, P. Finkel, U. States, and J. Palma, "Electrical and Thermal Transport Properties of M₂AlC, where M = Ti, Cr, Nb and V," no. May 2014.
- [127] P. A. Burr, D. Horlait, and W. E. Lee, "Experimental and DFT investigation of (Cr,Ti)₃AlC₂ MAX phases stability," *Mater. Res. Lett.*, vol. 5, no. 3, pp. 144– 157, May 2017, doi: 10.1080/21663831.2016.1222598.
- [128] T. Heine, "Grand Challenges in Computational Materials Science: From Description to Prediction at all Scales," *Front. Mater.*, vol. 1, no. July, pp. 1– 3, 2014, doi: 10.3389/fmats.2014.00007.
- [129] A. Thore, "A theoretical investigation of $Ti_{n+1}AlC_n$ and Mn_2GaC MAX phases: phase stability and materials properties," no. 1693, 2012, doi: 10.1016/j.spmi.2012.04.014.
- [130] K. Capelle, "A Bird 's-Eye View of Density-Functional Theory," vol. 36, no. 4, pp. 1318–1343, 2006.
- [131] N. M. Harrison, "An Introduction to Density Functional Theory," *Technology*, vol. 2, no. 1, pp. 1–26, 1995, doi: 10.1016/S1380-7323(05)80031-7.
- [132] R. F. W. Bader *et al.*, "A very short introduction to density functional theory (DFT)," *J. Chem. Phys.*, vol. 2013, no. 26, pp. 1–26, 2013, doi: 10.1002/9783527610709.
- [133] Y. Asadi and Z. Nourbakhsh, "First principle study of the structural, electronic, vibrational, thermodynamic, linear and nonlinear optical properties of zinc-blende ZnSe and ZnTe semiconductors," *Comput. Condens. Matter*, vol. 19, p. e00372, Jun. 2019, doi: 10.1016/j.cocom.2019.e00372.
- [134] V. I. Anisimov, "First-Principles Calculations of the Electronic Structure and Spectra of Strongly Correlated Systems: LDA + U Method," Spectrosc. Mott Insul. Correl. Met., vol. 9, pp. 106–116, 1995, doi: 10.1088/0953-8984/9/4/002.
- [135] J. L. Bretonnet, "Basics of the density functional theory," *AIMS Mater. Sci.*, vol. 4, no. 6, pp. 1372–1405, 2017, doi: 10.3934/MATERSCI.2017.6.1372.

- [136] L. Gagliardi, D. G. Truhlar, G. L. Manni, R. K. Carlson, C. E. Hoyer, and J. L. Bao, "Multicon fi guration Pair-Density Functional Theory: A New Way To Treat Strongly Correlated Systems," 2017, doi: 10.1021/acs.accounts.6b00471.
- [137] B. N. Plakhutin and B. N. Plakhutin, "Koopmans ' theorem in the Hartree-Fock method . General formulation Koopmans ' theorem in the Hartree-Fock method . General formulation," vol. 094101, 2018, doi: 10.1063/1.5019330.
- [138] N. Argaman and G. Makov, "Density functional theory: An introduction," *Am. J. Phys.*, vol. 68, no. 1, pp. 69–79, 2000, doi: 10.1119/1.19375.
- [139] T. H. Theorem, "Density Functional Theory," *Comput. Chem.*, pp. 42–48, 1964, doi: 10.1002/0471220655.ch5.
- [140] R. Baer, "VI. The Hohenberg-Kohn density functional theory," pp. 1–19.
- [141] T. H. Theorem, "Density Functional Theory," pp. 6–18, 1964.
- [142] A. Non, "The Kohn-Sham method," pp. 1–36.
- [143] F. Sultana, M. M. Uddin, M. A. Ali, M. M. Hossain, S. H. Naqib, and A. K. M. A. Islam, "First principles study of M₂InC (M = Zr, Hf and Ta) MAX phases: The effect of M atomic species," *Results Phys.*, vol. 11, no. August, pp. 869–876, 2018, doi: 10.1016/j.rinp.2018.10.044.
- [144] H. I. Faraoun, F. Z. Abderrahim, and C. Esling, "First principle calculations of MAX ceramics Cr₂GeC, V₂GeC and their substitutional solid solutions," *Comput. Mater. Sci.*, vol. 74, pp. 40–49, 2013, doi: 10.1016/j.commatsci.2013.03.005.
- [145] N. Kaur, V. Srivastava, and S. A. Dar, "GGA based study on electronic structure and thermoelectric properties of Mn₂PtCo full-Heusler compound," *Indian J. Phys.*, Jan. 2021, doi: 10.1007/s12648-020-01941-x.
- [146] Z. P. Yin, A. Kutepov, and G. Kotliar, "Correlation-enhanced electron-phonon coupling: Applications of GW and screened hybrid functional to bismuthates, chloronitrides, and other high-Tcsuperconductors," *Phys. Rev. X*, vol. 3, no. 2, 2013, doi: 10.1103/PhysRevX.3.021011.
- [147] W. Setyawan and S. Curtarolo, "High-throughput electronic band structure calculations: Challenges and tools," *Comput. Mater. Sci.*, vol. 49, no. 2, pp. 299–312, 2010, doi: 10.1016/j.commatsci.2010.05.010.
- [148] R. O. Jones, "PhD:Introduction to Density Functional Theory and Exchange-Correlation Energy Functionals," vol. 31, 2006.

- [149] M. A. L. Marques and E. K. U. Gross, "Time-dependent density functional theory," Annu. Rev. Phys. Chem., vol. 55, no. November, pp. 427–455, 2004, doi: 10.1146/annurev.physchem.55.091602.094449.
- [150] J. P. Perdew, Y. Wang, and M. Carlo, "r'), (2)," vol. 46, no. 20, pp. 947–954, 1992.
- [151] W. Kohn, A. D. Becke, and R. G. Parr, "Density Functional Theory of Electronic Structure," J. Phys. Chem, vol. 100, no. 96, pp. 12974–12980, 1996.
- [152] F. Bloch, "Über die Quantenmechanik der Elektronen in Kristallgittern," Zeitschrift für Phys., vol. 52, no. 7–8, pp. 555–600, 1929, doi: 10.1007/BF01339455.
- [153] H. J. Monkhorst and J. D. Pack, "Special points for Brillonin-zone integrations* Hendrik," *Phys. Rev. B*, vol. 13, no. 12, pp. 5188–5192, 1976, doi: 10.1103/physrevb.13.5188.
- [154] K. C. Bimal, "Quasi-Harmonic And Anharmonic Entropies In Transition Metals University of Texas at El Paso ScholarWorks @ UTEP Open Access Theses & Dissertations Quasi-Harmonic And Anharmonic Entropies In Transition Metals University of Texas at El Paso," no. January 2019, 2020, doi: 10.13140/RG.2.2.31226.24006.
- [155] Charles Kittel, "Introduction to Solid State Physics, 8th Edition," p. 704, 2004,
 [Online]. Available: http://as.wiley.com/WileyCDA/WileyTitle/productCd-EHEP000803.html.
- [156] G. Vasseur, Y. Fagot-Revurat, B. Kierren, M. Sicot, and D. Malterre, "Effect of symmetry breaking on electronic band structure: Gap opening at the high symmetry points," *Symmetry (Basel).*, vol. 5, no. 4, pp. 344–354, 2013, doi: 10.3390/sym5040344.
- [157] G. Shukla, "Impossibility of the simple cubic metal in nature," no. March, 2020.
- [158] T. Lapauw *et al.*, "The double solid solution (Zr, Nb)₂(Al, Sn)C MAX phase: a steric stability approach," *Sci. Rep.*, vol. 8, no. 1, pp. 1–13, 2018, doi: 10.1038/s41598-018-31271-2.
- [159] E. Kogan and V. U. Nazarov, "Symmetry classification of energy bands in graphene," *Phys. Rev. B - Condens. Matter Mater. Phys.*, vol. 85, no. 11, pp. 1–5, 2012, doi: 10.1103/PhysRevB.85.115418.

- [160] J. D. Pack and H. J. Monkhorst, "Special points for Brillouin-zone integrations," *Phys. Rev. B*, vol. 16, no. 4, pp. 1748–1749, Aug. 1977, doi: 10.1103/PhysRevB.16.1748.
- [161] E. Fermi, "Sopra lo Spostamento per Pressione delle Righe Elevate delle Serie Spettrali," *Nuovo Cim.*, vol. 11, no. 3, pp. 157–166, Mar. 1934, doi: 10.1007/BF02959829.
- [162] P. Schwerdtfeger, "The pseudopotential approximation in electronic structure theory," *ChemPhysChem*, vol. 12, no. 17, pp. 3143–3155, 2011, doi: 10.1002/cphc.201100387.
- [163] F. Han, Fundamentals of Semiconductors. 2011.
- [164] L. Lu *et al.*, "Experimental observation of Weyl points," *Science* (80-.)., vol. 349, no. 6248, pp. 622–624, 2015, doi: 10.1126/science.aaa9273.
- [165] A. Bouhemadou, "Structural, electronic and elastic properties of MAX phases M₂GaN (M = Ti, V and Cr)," *Solid State Sci.*, vol. 11, no. 11, pp. 1875–1881, 2009, doi: 10.1016/j.solidstatesciences.2009.08.002.
- [166] F. D. Murnaghan, "The Compressibility of Media Under Extreme Pressure," *Physics (College. Park. Md).*, vol. 30, pp. 244–247, 1944.
- [167] P. Bhardwaj and S. Singh, "First principle calculation of structural, electronic and elastic properties of rare earth nitride," *Mater. Sci. Pol.*, vol. 34, no. 4, pp. 715–720, 2016, doi: 10.1515/msp-2016-0123.
- [168] S. Coh, "Electronic Structure Theory: Applications and Geometrical Aspects,"
 2011, [Online]. Available: http://mss3.libraries.rutgers.edu/dlr/showfed.php?pid=rutgers-lib:35951.
- [169] W. D. Callister, "Materials science and engineering: An introduction (2nd edition)," *Mater. Des.*, vol. 12, no. 1, p. 59, 1991, doi: 10.1016/0261-3069(91)90101-9.
- [170] K. Schwarz, P. Blaha, and G. K. H. Madsen, "Electronic structure calculations of solids using the WIEN2k package for material sciences," *Comput. Phys. Commun.*, vol. 147, no. 1–2, pp. 71–76, 2002, doi: 10.1016/S0010-4655(02)00206-0.
- [171] D. S. Ginley, Handbook of Transparent Conductors. 2011.
- [172] F. Wooten, "Optical Properties of Solids," 1972.
- [173] A. Debernardi and S. Baroni, "Third-order density-functional perturbation theory: A practical implementation with applications to anharmonic couplings

in Si," *Solid State Commun.*, vol. 91, no. 10, pp. 813–816, 1994, doi: 10.1016/0038-1098(94)90654-8.

- [174] A. Urru and A. Dal Corso, "Density functional perturbation theory for lattice dynamics with fully relativistic ultrasoft pseudopotentials: The magnetic case," *Phys. Rev. B*, vol. 100, no. 4, pp. 1–6, 2019, doi: 10.1103/PhysRevB.100.045115.
- [175] A. Dal and C. Sissa, "Thermo pw : Thermodynamics of crystals."
- [176] T. H. K. Barron and M. L. Klein, "Second-order elastic constants of a solid under stress," *Proc. Phys. Soc.*, vol. 85, no. 3, pp. 523–532, 1965, doi: 10.1088/0370-1328/85/3/313.
- [177] G. Grimvall, B. Magyari-Köpe, V. Ozoliņš, and K. A. Persson, "Lattice instabilities in metallic elements," *Rev. Mod. Phys.*, vol. 84, no. 2, pp. 945– 986, Jun. 2012, doi: 10.1103/RevModPhys.84.945.
- [178] D. H. Chung and W. R. Buessem, "The voigt-reuss-hill (vrh) approximation and the elastic moduli of polycrystalline zno, tio2 (rutile), and α-al2o 3," J. *Appl. Phys.*, vol. 39, no. 6, pp. 2777–2782, 1968, doi: 10.1063/1.1656672.
- [179] I. R. Shein and A. L. Ivanovskii, "Elastic properties of superconducting MAX phases from first-principles calculations," *Phys. Status Solidi Basic Res.*, vol. 248, no. 1, pp. 228–232, 2011, doi: 10.1002/pssb.201046163.
- [180] S. F. Pugh, "XCII. Relations between the elastic moduli and the plastic properties of polycrystalline pure metals," *London, Edinburgh, Dublin Philos. Mag. J. Sci.*, vol. 45, no. 367, pp. 823–843, 1954, doi: 10.1080/14786440808520496.
- [181] U. F. Ozyar, E. Deligoz, and K. Colakoglu, "Systematic study on the anisotropic elastic properties of tetragonal XYSb (X Combining double low line Ti, Zr, Hf; Y Combining double low line Si, Ge) compounds," *Solid State Sci.*, vol. 40, pp. 92–100, 2015, doi: 10.1016/j.solidstatesciences.2015.01.001.
- [182] C. S. Man and M. Huang, "A simple explicit formula for the Voigt-Reuss-Hill average of elastic polycrystals with arbitrary crystal and texture symmetries," *J. Elast.*, vol. 105, no. 1–2, pp. 29–48, 2011, doi: 10.1007/s10659-011-9312-y.
- [183] D. Freyer and W. Voigt, "Crystallization and Phase Stability of CaSO₄ and CaSO₄ - Based Salts," *Monatshefte fur Chemie*, vol. 134, no. 5, pp. 693–719, 2003, doi: 10.1007/s00706-003-0590-3.
- [184] R. Hill, "The elastic behaviour of a crystalline aggregate," Proc. Phys. Soc.

Sect. A, vol. 65, no. 5, pp. 349–354, 1952, doi: 10.1088/0370-1298/65/5/307.

- [185] A. J. G. Lunt *et al.*, "Calculations of single crystal elastic constants for yttria partially stabilised zirconia from powder diffraction data," *J. Appl. Phys.*, vol. 116, no. 5, 2014, doi: 10.1063/1.4891714.
- [186] D. H. Chung and W. R. Buessem, "The Voigt-Reuss-Hill approximation and elastic moduli of polycrystalline Mgo, CaF₂, β-ZnS, ZnSe, and CdTe," J. *Appl. Phys.*, vol. 38, no. 6, pp. 2535–2540, 1967, doi: 10.1063/1.1709944.
- [187] S. I. Ranganathan and M. Ostoja-Starzewski, "Universal elastic anisotropy index," *Phys. Rev. Lett.*, vol. 101, no. 5, pp. 3–6, 2008, doi: 10.1103/PhysRevLett.101.055504.
- [188] M. A. S. Ali, M. A. S. Ali, and M. M. Uddin, "Structural, elastic, electronic and optical properties of metastable MAX phase Ti₅SiC₄ compound," *Indian J. Pure Appl. Phys.*, vol. 54, no. 6, pp. 386–390, 2016, [Online]. Available: http://op.niscair.res.in/index.php/IJPAP/article/view/4502.
- [189] J. G. Lee, Computational Materials Science, Second Edi. Boca Raton : CRC Press, Taylor & Francis, 2017., 2017.
- [190] R. V. Goldstein, V. A. Gorodtsov, M. A. Komarova, and D. S. Lisovenko, "Extreme values of the shear modulus for hexagonal crystals," *Scr. Mater.*, vol. 140, pp. 55–58, 2017, doi: 10.1016/j.scriptamat.2017.07.002.
- [191] M. M. Wu, L. Wen, B. Y. Tang, L. M. Peng, and W. J. Ding, "First-principles study of elastic and electronic properties of MgZn₂ and ScZn₂ phases in Mg-Sc-Zn alloy," *J. Alloys Compd.*, vol. 506, no. 1, pp. 412–417, 2010, doi: 10.1016/j.jallcom.2010.07.018.
- [192] R. Yu, X. F. Zhang, L. L. He, and H. Q. Ye, "Topology of charge density and elastic anisotropy of Ti₃SiC₂ polymorphs," *J. Mater. Res.*, vol. 20, no. 5, pp. 1180–1185, 2005, doi: 10.1557/JMR.2005.0145.
- [193] A. Candan, S. Akbudak, Ş. Uğur, and G. Uğur, "Theoretical research on structural, electronic, mechanical, lattice dynamical and thermodynamic properties of layered ternary nitrides Ti2AN (A = Si, Ge and Sn)," *J. Alloys Compd.*, vol. 771, no. August, pp. 664–673, Jan. 2019, doi: 10.1016/j.jallcom.2018.08.286.
- [194] M. A. Ali, M. M. Hossain, N. Jahan, A. K. M. A. Islam, and S. H. Naqib, "Newly synthesized Zr₂AlC, Zr₂(Al_{0.58}Bi_{0.42})C, Zr₂(Al_{0.2}Sn_{0.8})C, and Zr<sub>2(Al_{0.3}Sb_{0.7})C MAX phases: A DFT based first-principles study,"

Comput. Mater. Sci., vol. 131, pp. 139–145, Apr. 2017, doi: 10.1016/j.commatsci.2017.01.048.

- [195] P. K. Jha, "Phonon spectra and vibrational mode instability of MgCNi3," *Phys. Rev. B - Condens. Matter Mater. Phys.*, vol. 72, no. 21, pp. 1–6, 2005, doi: 10.1103/PhysRevB.72.214502.
- [196] G. Surucu, K. Colakoglu, E. Deligoz, and N. Korozlu, "First-Principles Study on the MAX Phases $Ti_{n+1}GaN_n$ (n = 1 , 2 , and 3)," 2016, doi: 10.1007/s11664-016-4607-1.
- [197] P. Wachter, M. Filzmoser, and J. Rebizant, "Electronic and elastic properties of the light actinide tellurides," *Phys. B Condens. Matter*, vol. 293, no. 3–4, pp. 199–223, 2001, doi: 10.1016/S0921-4526(00)00575-5.
- [198] S. Al-Qaisi *et al.*, "Structural, elastic, mechanical and thermodynamic properties of Terbium oxide: First-principles investigations," *Results Phys.*, vol. 7, pp. 709–714, 2017, doi: 10.1016/j.rinp.2017.01.027.
- [199] X. K. Qian, H. Y. Wu, H. P. Zhu, S. H. Ma, and T. Jiang, "First-principles study of a new higher-order max phase of Ti₅Al₂C₃," *J. Ceram. Sci. Technol.*, vol. 7, no. 1, pp. 47–52, 2016, doi: 10.4416/JCST2015-00027.
- [200] M. A. Hadi, M. A. Rayhan, S. H. Naqib, A. Chroneos, and A. K. M. A. M. A. Islam, "Structural, elastic, thermal and lattice dynamic properties of new 321 MAX phases," *Comput. Mater. Sci.*, vol. 170, no. May, p. 109144, 2019, doi: 10.1016/j.commatsci.2019.109144.
- [201] J. Singh, "Boltzmann Transport Theory," Mod. Phys. Eng., 2004.
- [202] P. Engineering, "Electronic transport properties of thermoelectric Zintl," 2016.
- [203] and D. J. S. T. C. Collins, R. N. Euwema, "Self-Consistent Orthogonalized-Plane-Wave Calculations," 1971.
- [204] D. D. Koelling and J. H. Wood, "On the interpolation of eigenvalues and a resultant integration scheme," J. Comput. Phys., vol. 67, no. 2, pp. 253–262, 1986, doi: 10.1016/0021-9991(86)90261-5.
- [205] E. Assmann, P. Wissgott, J. Kuneš, A. Toschi, P. Blaha, and K. Held, "Woptic: Optical conductivity with Wannier functions and adaptive k-mesh refinement," *Comput. Phys. Commun.*, vol. 202, pp. 1–11, 2016, doi: 10.1016/j.cpc.2015.12.010.
- [206] J. Scheidemantel, C. Ambrosch-Draxl, T. Thonhauser, V. Badding, and O. Sofo, "Transport coefficients from first-principles calculations," *Phys. Rev. B* -

Condens. Matter Mater. Phys., vol. 68, no. 12, pp. 1–6, 2003, doi: 10.1103/PhysRevB.68.125210.

- [207] G. K. H. Madsen, J. Carrete, and M. J. Verstraete, "BoltzTraP2, a program for interpolating band structures and calculating semi-classical transport coefficients," *Comput. Phys. Commun.*, vol. 231, no. January, pp. 140–145, 2018, doi: 10.1016/j.cpc.2018.05.010.
- [208] A. Jayaraman, A. Bhat Kademane, and M. Molli, "DFT Study on the Carrier Concentration and Temperature-Dependent Thermoelectric Properties of Antimony Selenide," *Indian J. Mater. Sci.*, vol. 2016, pp. 1–7, 2016, doi: 10.1155/2016/7296847.
- [209] C. F. Zinola, "Density functional theory," *Electrocatal. Comput. Exp. Ind. Asp.*, pp. 117–138, 2010, doi: 10.1201/9781420045451.
- [210] A. Bouhemadou, "Calculated structural and elastic properties of M₂InC (M = Sc, Ti, V, Zr, Nb, Hf, Ta)," *Mod. Phys. Lett. B*, vol. 22, no. 22, pp. 2063–2076, 2008, doi: 10.1142/S0217984908016807.
- [211] P. Giannozzi *et al.*, "QUANTUM ESPRESSO: a modular and open-source software project for quantum simulations of materials," *J. Phys. Condens. Matter*, vol. 21, no. 39, p. 395502, Sep. 2009, doi: 10.1088/0953-8984/21/39/395502.
- [212] C. Malica and A. Dal Corso, "Temperature-dependent atomic B factor: An ab initio calculation," *Acta Crystallogr. Sect. A Found. Adv.*, vol. 75, no. 1996, pp. 624–632, 2019, doi: 10.1107/S205327331900514X.
- [213] O. Motornyi, M. Raynaud, A. Dal Corso, and N. Vast, "Simulation of electron energy loss spectra with the turboEELS and thermo-pw codes," J. Phys. Conf. Ser., vol. 1136, no. 1, 2018, doi: 10.1088/1742-6596/1136/1/012008.
- [214] Y. Zhou, J. R. Chelikowsky, X. Gao, and A. Zhou, "On the Preconditioning Function Used in Planewave DFT Calculations and its Generalization," *Commun. Comput. Phys.*, vol. 18, no. 1, pp. 167–179, 2015, doi: 10.4208/cicp.060314.120215a.
- [215] G. I. Miletić and A. Drašner, "DFT study of the cohesive and structural properties of YNi₅H_xcompounds," *J. Alloys Compd.*, vol. 622, pp. 1041–1048, 2015, doi: 10.1016/j.jallcom.2014.10.106.
- [216] A. Dal Corso, "Elastic constants of beryllium: A first-principles investigation," J. Phys. Condens. Matter, vol. 28, no. 7, 2016, doi:

10.1088/0953-8984/28/7/075401.

- [217] A. D. Corso, "Thermo _ pw a FORTRAN driver for Quantum ESPRESSO routines : progress report 2018," 2018.
- [218] P. Fuentealba, L. v. Szentpály, H. Stoll, F. X. Fraschio, and H. Preuss, "Pseudopotential calculations including core-valence correlation: Alkali compounds," *J. Mol. Struct. THEOCHEM*, vol. 93, no. C, pp. 213–219, 1983, doi: 10.1016/0166-1280(83)80104-3.
- [219] G. K. H. Madsen, J. Carrete, and M. J. Verstraete, "BoltzTraP2, a program for interpolating band structures and calculating semi-classical transport coefficients," *Comput. Phys. Commun.*, vol. 231, pp. 140–145, 2018, doi: 10.1016/j.cpc.2018.05.010.
- [220] G. Pizzi, D. Volja, B. Kozinsky, M. Fornari, and N. Marzari, "thermoelectric and electronic transport properties with," 2013, pp. 1–19.
- [221] G. K. H. Madsen, J. Carrete, and M. J. Verstraete, "BoltzTraP2, a program for interpolating band structures and calculating semi-classical transport coefficients ☆," *Comput. Phys. Commun.*, vol. 231, pp. 140–145, 2018, doi: 10.1016/j.cpc.2018.05.010.
- [222] M. Dahlqvist, A. Thore, and J. Rosen, "Electronic structure, bonding characteristics, and mechanical properties in (W_{2/3}Sc_{1/3})₂AlC and (W_{2/3}Y_{1/3})₂AlC i-MAX phases from first-principles calculations," J. Phys. Condens. Matter, 2018, doi: 10.1088/1361-648X/aacc19.
- [223] J. P. Perdew, K. Burke, and M. Ernzerhof, "Generalized Gradient Approximation Made Simple," *Phys. Rev. Lett*, vol. 77, no. 18, pp. 3865– 3868, 1996.
- [224] N. A. Phatak, S. K. Saxena, Y. Fei, and J. Hu, "Synthesis and structural stability of Ti2GeC," J. Alloys Compd., vol. 474, no. 1–2, pp. 174–179, 2009, doi: 10.1016/j.jallcom.2008.06.073.
- [225] M.- Protocol, C. Cao, Y. Chen, Y. Wu, and E. Deumens, "OPAL: A Multiscale Multicenter Simulation Package Based on MPI-2 Protocol," *Int. J. Quantum Chem.*, vol. 111, no. May, pp. 4020–4029, 2011, doi: 10.1002/qua.
- [226] W. Sailuam, K. Phacheerak, Atipong bootchanont, I. Fongkaew, and S. Limpijumnong, "Elastic and mechanical properties of hydroxyapatite under pressure: A first-principles investigation," *Comput. Condens. Matter*, vol. 24, p. e00481, 2020, doi: 10.1016/j.cocom.2020.e00481.

- [227] M. Li *et al.*, "Element Replacement Approach by Reaction with Lewis Acidic Molten Salts to Synthesize Nanolaminated MAX Phases and MXenes," *J. Am. Chem. Soc.*, vol. 141, no. 11, pp. 4730–4737, 2019, doi: 10.1021/jacs.9b00574.
- [228] A. K. M. A. I. M. A. Rayhan, M. A. Ali, S. H. Naqib, "First-principles Study of Vickers Hardness and Thermodynamic Properties of Ti₃SnC₂ Polymorphs," *J. Sci. Res.*, vol. 7, no. 3, pp. 53–64, 2015, doi: 10.3329/jsr.v7i3.23182.
- [229] F. Mouhat and F. X. Coudert, "Necessary and sufficient elastic stability conditions in various crystal systems," *Phys. Rev. B - Condens. Matter Mater. Phys.*, vol. 90, no. 22, pp. 0–3, 2014, doi: 10.1103/PhysRevB.90.224104.

LIST OF PUBLICATIONS

1. S. T. Ahams, A. Shaari, R. Ahmed, N. F. Abdul Pattah, M. C. Idris & B. U. Haq. (2021) Ab initio Study of the Structure, Elastic, and Electronic Properties of Ti₃(Al_{1-n}Si_n)C₂ Layered Ternary Compounds. *Scientific Reports*. https://doi.org/10.1038/s41598-021-84466-5

2. S. T. Ahams^{*}, A. Shaari, R. Ahmed, N. F. Abdul Pattah, M. C. Idris, B. U Haq. (2021) Theoretical investigation of Zr₂PbC, (V_{0.25}Zr_{0.75})₂PbC, (V_{0.5}Zr_{0.5})₂PbC, V_{0.75}Zr_{0.25})₂PbC, and V₂PbC MAX phases: A DFT based study. *Materials Today Communications* 27 102397.

https://doi.org/10.1016/j.mtcomm.2021.102397.

3. S. T. Ahams^{*}, A. Shaari, R. Ahmed, N. F. Abdul Pattah, M. C. Idris, B. U Haq. (2021) A DFT investigation of the structural, mechanical, thermodynamic, and electronic properties of Zr₂PbC MAX phase. *Solid State Technology* 64(2)4863-4874.

4. S. T. Ahams, A. Shaari, R. Ahmed, N. F. Abdul Pattah, M. C. Idris. (2020) Abinitio Calculations of the Structural and Electronic Properties of Zr₂AC . *Proceedings of Science and Mathematics*, **1**, 41-4641.